Breadth/Depth First Search (BFS/DFS) (Bagian 1)

Bahan Kuliah IF2211 Strategi Algoritmik

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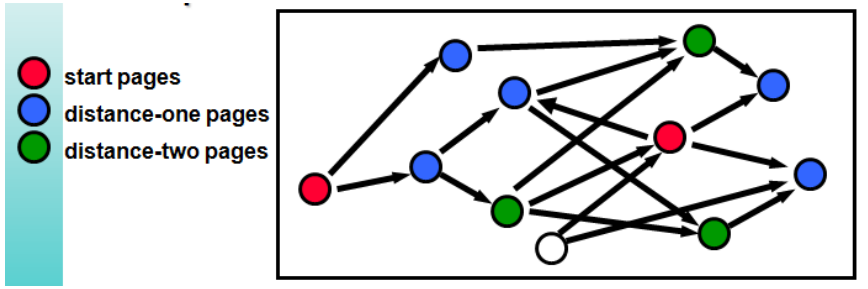
Traversal Graf

- Algoritma traversal graf: mengunjungi simpul dengan cara yang sistematik
  - Pencarian melebar (*breadth first search*/BFS)
  - Pencarian mendalam (*depth first search*/DFS)
  - Asumsi: graf terhubung
- Graf: representasi persoalan

➔ Traversal graf: pencarian solusi

social graph

http://www.oreilly.de/catalog/9780596518172/toc.html



Web page network

Algoritma Pencarian Solusi

- **Tanpa informasi (*uninformed/blind search*)**
  - Tidak ada informasi tambahan
  - Contoh: **DFS, BFS**, *Depth Limited Search*, *Iterative Deepening Search*, *Uniform Cost Search*

- **Dengan informasi (*informed Search*)**
  - Pencarian berbasis heuristik
  - Mengetahui non-goal state “lebih menjanjikan” daripada yang lain
  - Contoh: *Best First Search*, A*

Representasi Graf dalam Proses Pencarian

Dalam proses pencarian solusi, terdapat dua pendekatan:

1. Graf statis: graf yang sudah terbentuk sebelum proses pencarian dilakukan

   - graf direpresentasikan sebagai struktur data

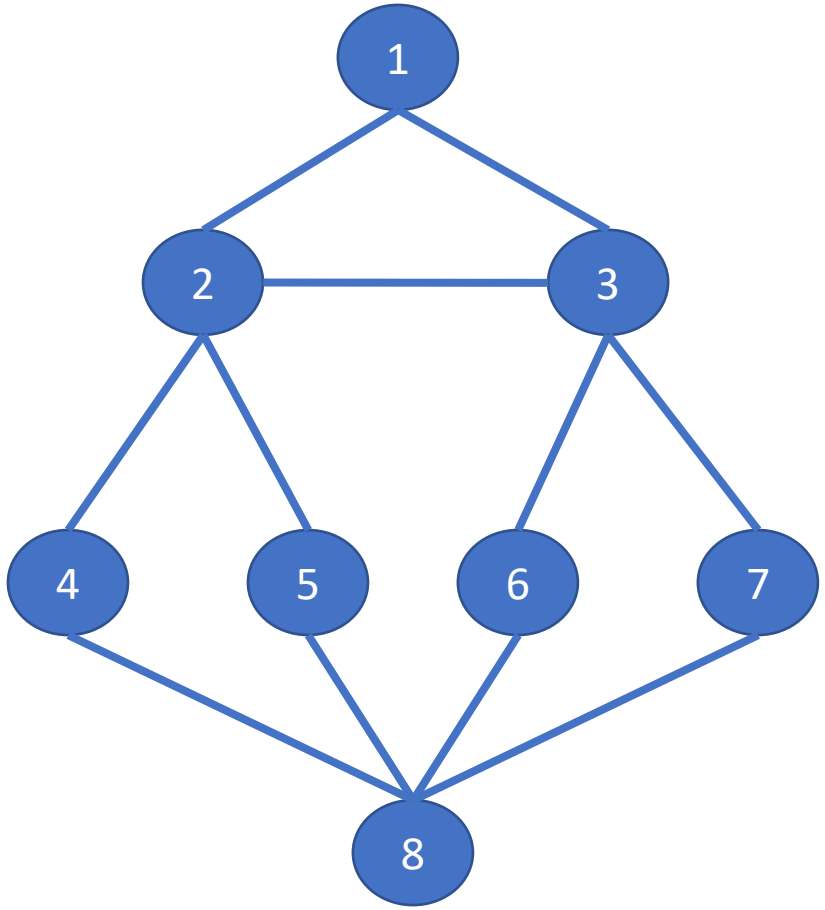
2. Graf dinamis: graf yang terbentuk saat proses pencarian dilakukan

   - graf tidak tersedia sebelum pencarian, graf dibangun selama pencarian solusi

Graf Statis

Pencarian Melebar (BFS)

- Traversal dimulai dari simpul *v*.
- Algoritma:
  1. Kunjungi simpul *v*
  2. Kunjungi semua simpul yang bertetangga dengan simpul *v* terlebih dahulu.
  3. Kunjungi simpul yang belum dikunjungi dan bertetangga dengan simpul-simpul yang tadi dikunjungi, demikian seterusnya.



BFS: Struktur Data

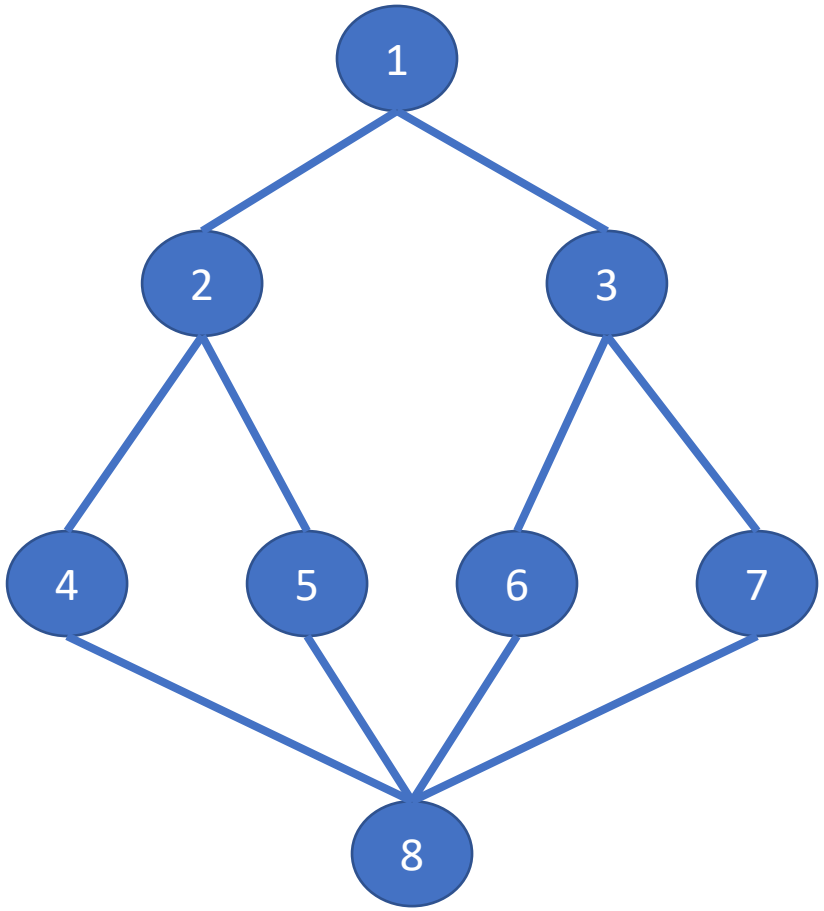
1. Matriks ketetanggaan $A = [a_{ij}]$ yang berukuran nxn,
   a_{ij}= 1, jika simpul *i* dan simpul *j* bertetangga,
   a_{ij}= 0, jika simpul *i* dan simpul *j* tidak bertetangga.

2. Antrian *q* untuk menyimpan simpul yang telah dikunjungi.

3. Tabel Boolean, diberi nama "dikunjungi"
   ```
   dikunjungi : array[1..n] of boolean
   ```
   dikunjungi[i] = *true* jika simpul *i* sudah dikunjungi
   dikunjungi[i] = *false* jika simpul *i* belum dikunjungi

```
procedure BFS(input v:integer)
{ Traversal graf dengan algoritma pencarian BFS.

  Masukan: v adalah simpul awal kunjungan
  Keluaran: semua simpul yang dikunjungi dicetak ke layar
}
Deklarasi
   w : integer
   q : antrian;

   procedure BuatAntrian(input/output q : antrian)
   { membuat antrian kosong, kepala(q) diisi 0 }

   procedure MasukAntrian(input/output q:antrian, input v:integer)
   { memasukkan v ke dalam antrian q pada posisi belakang }

   procedure HapusAntrian(input/output q:antrian,output v:integer)
   { menghapus v dari kepala antrian q }

   function AntrianKosong(input q:antrian) → boolean
   { true jika antrian q kosong, false jika sebaliknya }

Algoritma:
   BuatAntrian(q)          { buat antrian kosong }

   write(v)                { cetak simpul awal yang dikunjungi }
   dikunjungi[v]←true      { simpul v telah dikunjungi, tandai dengan
                             true}
   MasukAntrian(q,v)       { masukkan simpul awal kunjungan ke dalam
                             antrian}

  { kunjungi semua simpul graf selama antrian belum kosong }
   while not AntrianKosong(q) do
        HapusAntrian(q,v)   { simpul v telah dikunjungi, hapus dari
                              antrian }
        for tiap simpul w yang bertetangga dengan simpul v do
              if not dikunjungi[w] then
                 write(w)     {cetak simpul yang dikunjungi}
                 MasukAntrian(q,w)
                 dikunjungi[w]←true
              endif
     endfor
   endwhile
  { AntrianKosong(q) }
```

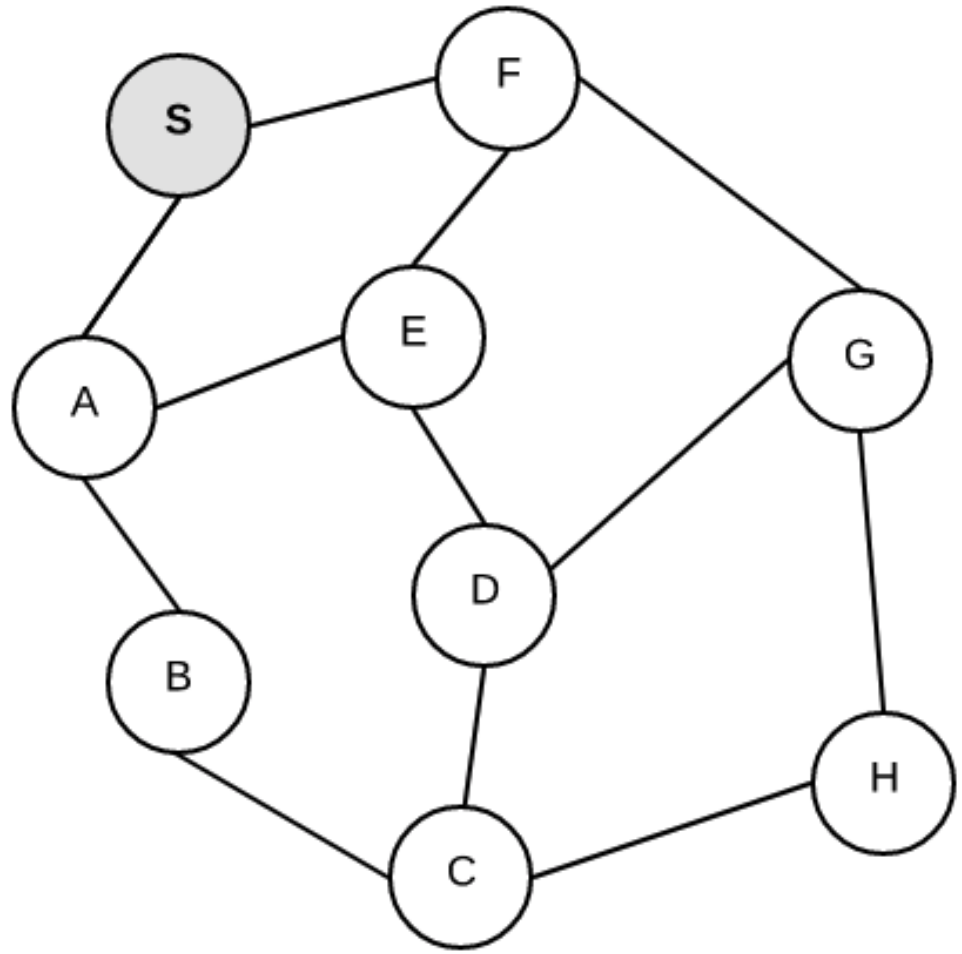
BFS: Ilustrasi

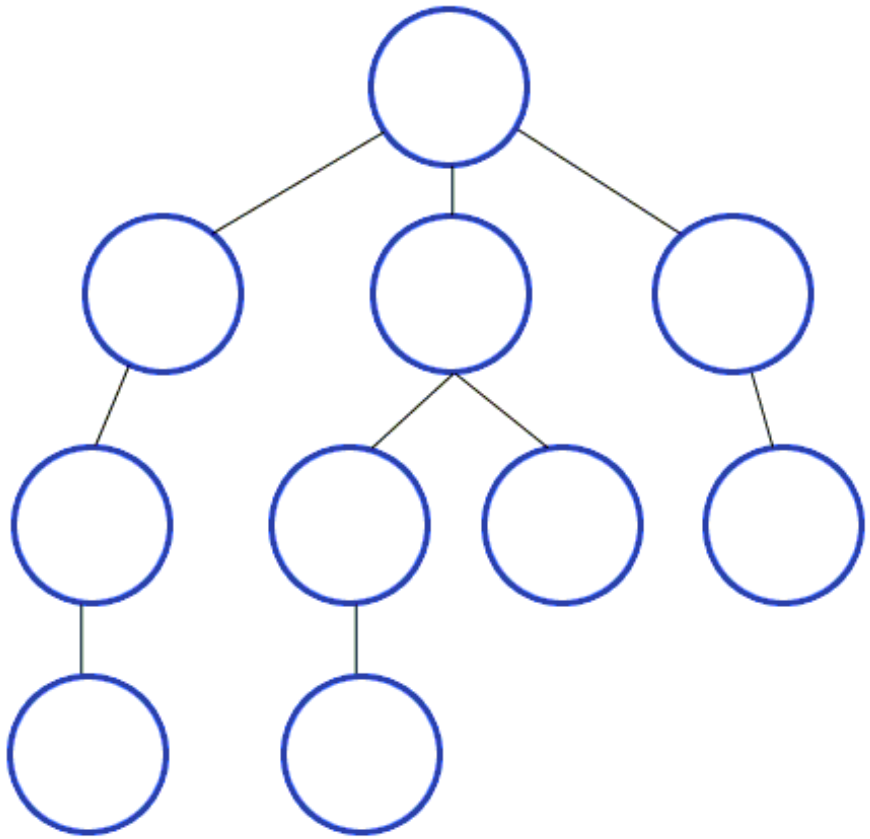


Iterasi	V	Q	dikunjungi							
			1	2	3	4	5	6	7	8
Inisialisasi	1	{1}	T	F	F	F	F	F	F	F
Iterasi 1	1	{2,3}	T	T	T	F	F	F	F	F
Iterasi 2	2	{3,4,5}	T	T	T	T	T	F	F	F
Iterasi 3	3	{4,5,6,7}	T	T	T	T	T	T	T	F
Iterasi 4	4	{5,6,7,8}	T	T	T	T	T	T	T	T
Iterasi 5	5	{6,7,8}	T	T	T	T	T	T	T	T
Iterasi 6	6	{7,8}	T	T	T	T	T	T	T	T
Iterasi 7	7	{8}	T	T	T	T	T	T	T	T
Iterasi 8	8	{}	T	T	T	T	T	T	T	T

Urutan simpul2 yang dikunjungi: 1, 2, 3, 4, 5, 6, 7, 8

Fig 2



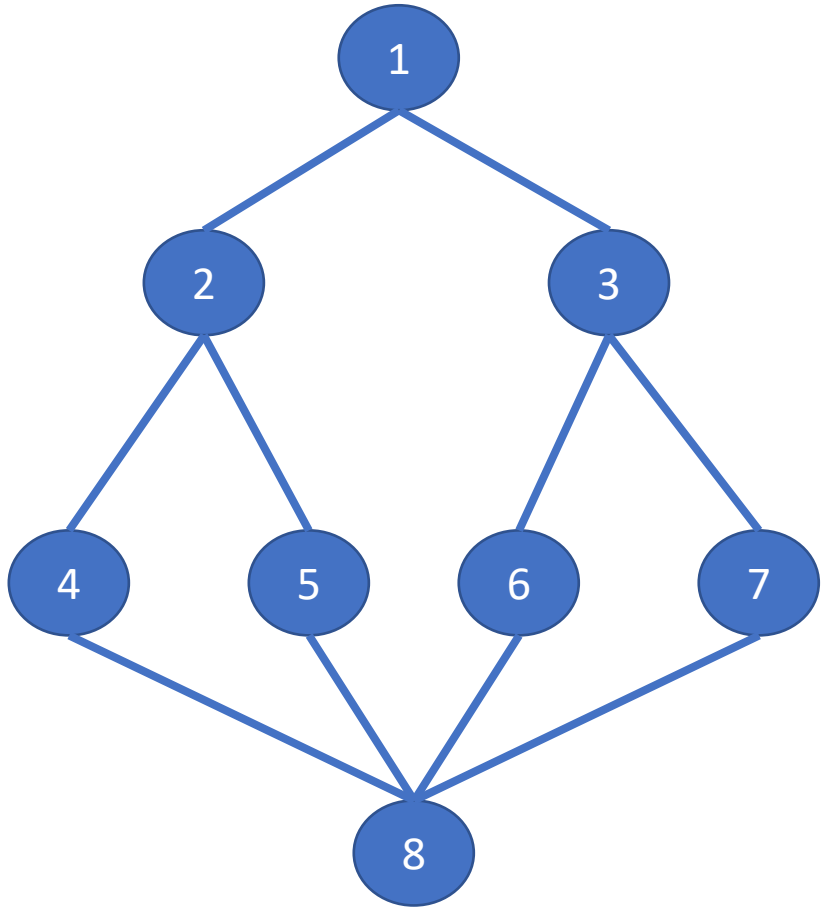


Pencarian Mendalam (DFS)

- Traversal dimulai dari simpul *v*.

- Algoritma:

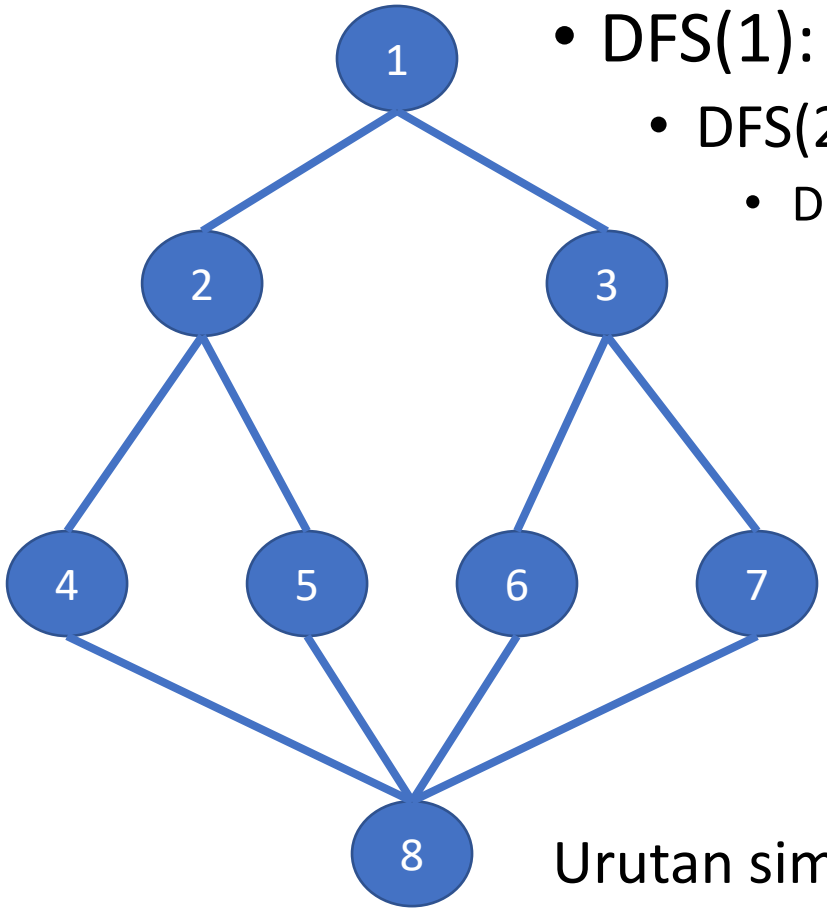
1. Kunjungi simpul *v*
2. Kunjungi simpul w yang bertetangga dengan simpul *v*.
3. Ulangi DFS mulai dari simpul *w*.
4. Ketika mencapai simpul *u* sedemikian sehingga semua simpul yang bertetangga dengannya telah dikunjungi, pencarian dirunut-balik (*backtrack*) ke simpul terakhir yang dikunjungi sebelumnya dan mempunyai simpul w yang belum dikunjungi.
5. Pencarian berakhir bila tidak ada lagi simpul yang belum dikunjungi yang dapat dicapai dari simpul yang telah dikunjungi.



DFS

```
procedure DFS(input v:integer)
{Mengunjungi seluruh simpul graf dengan algoritma pencarian DFS

Masukan: v adalah simpul awal kunjungan
Keluaran: semua simpulyang dikunjungi ditulis ke layar
}
Deklarasi
   w : integer

Algoritma:
   write(v)
   dikunjungi[v]←true
   for w←1 to n do
      if A[v,w]=1 then {simpul v dan simpul w bertetangga }
         if not dikunjungi[w] then
            DFS(w)
         endif
      endif
   endfor
```

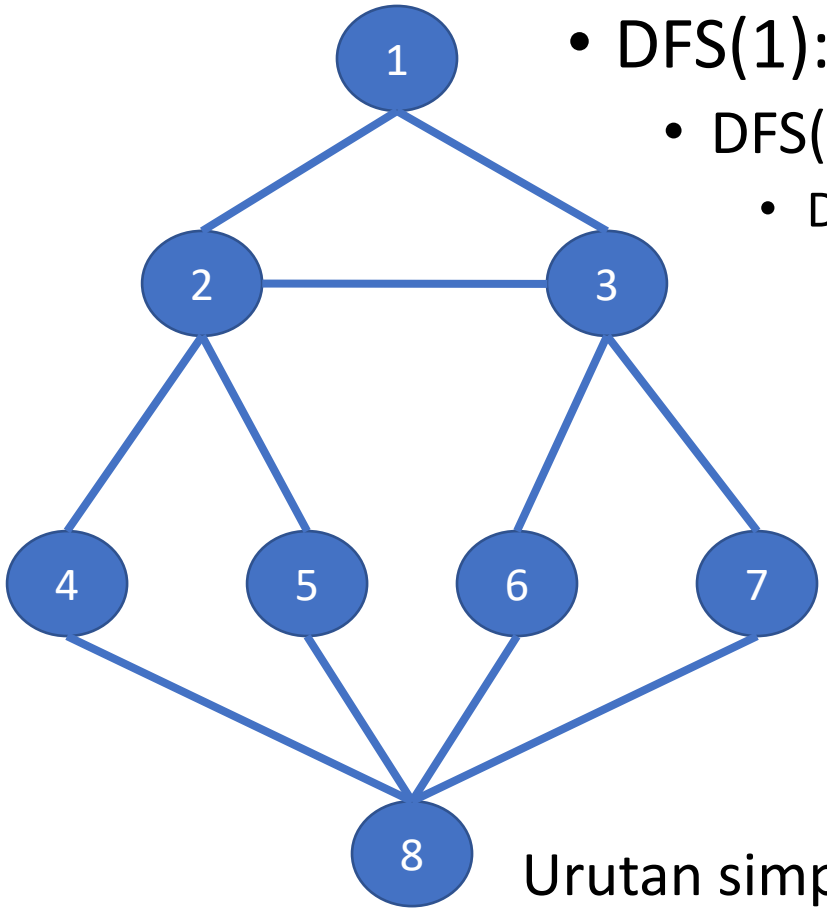
DFS: Ilustrasi 1



- DFS(1): v=1; dikunjungi[1]=true; DFS(2)
  - DFS(2): v=2; dikunjungi[2]=true; DFS(4)
    - DFS(4): v=4; dikunjungi[4]=true; DFS(8)
      - DFS(8): v=8; dikunjungi[8]=true; DFS(5)
        - DFS(5): v=5; dikunjungi[5]=true
        - DFS(6): v=6; dikunjungi[6]=true; DFS(3)
          - DFS(3): v=3; dikunjungi[3]=true; DFS(7)
            - DFS(7): v=7; dikunjungi[7]=true

Urutan simpul2 yang dikunjungi: 1, 2, 4, 8, 5, 6, 3, 7

DFS: Ilustrasi 2

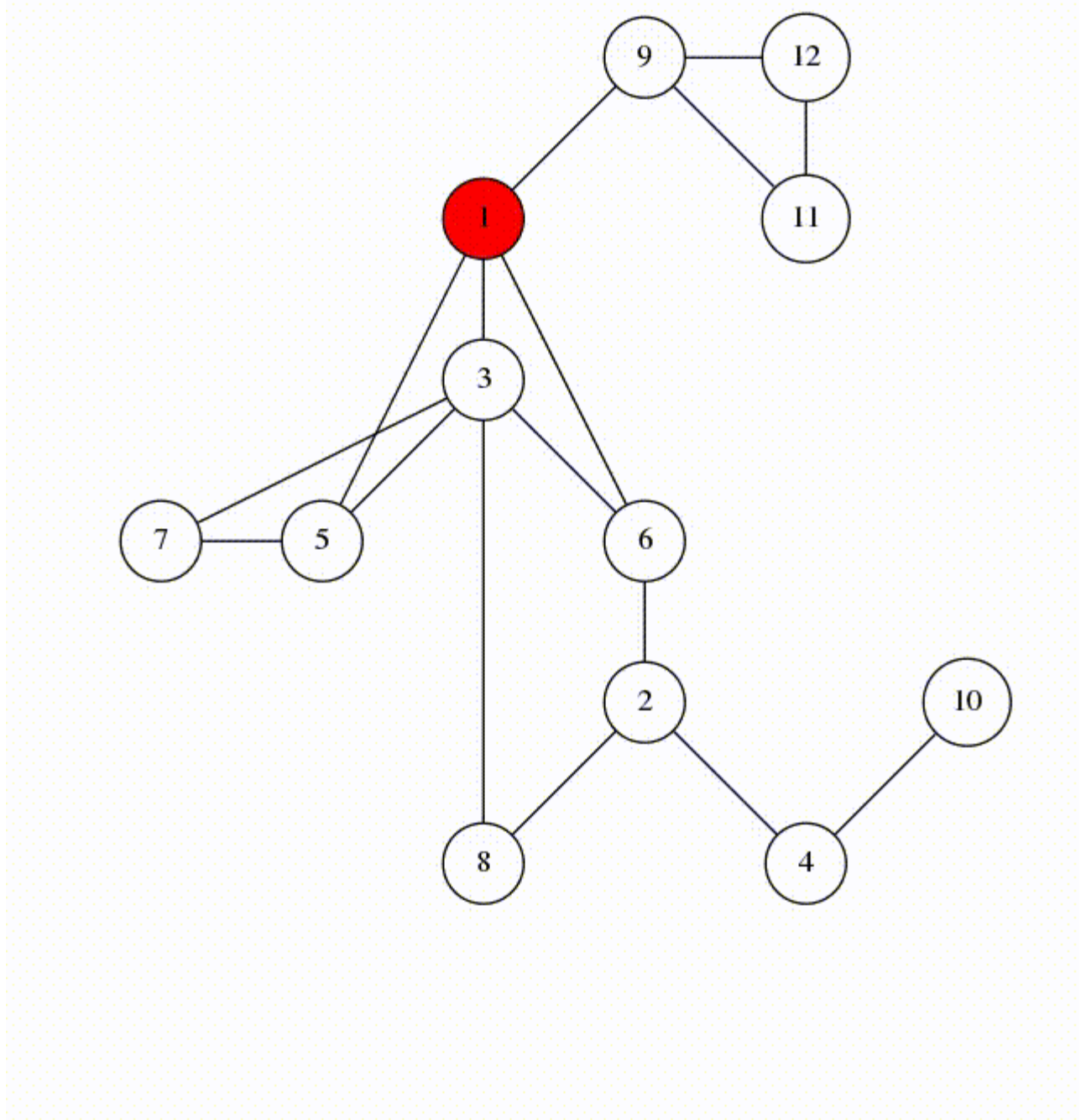


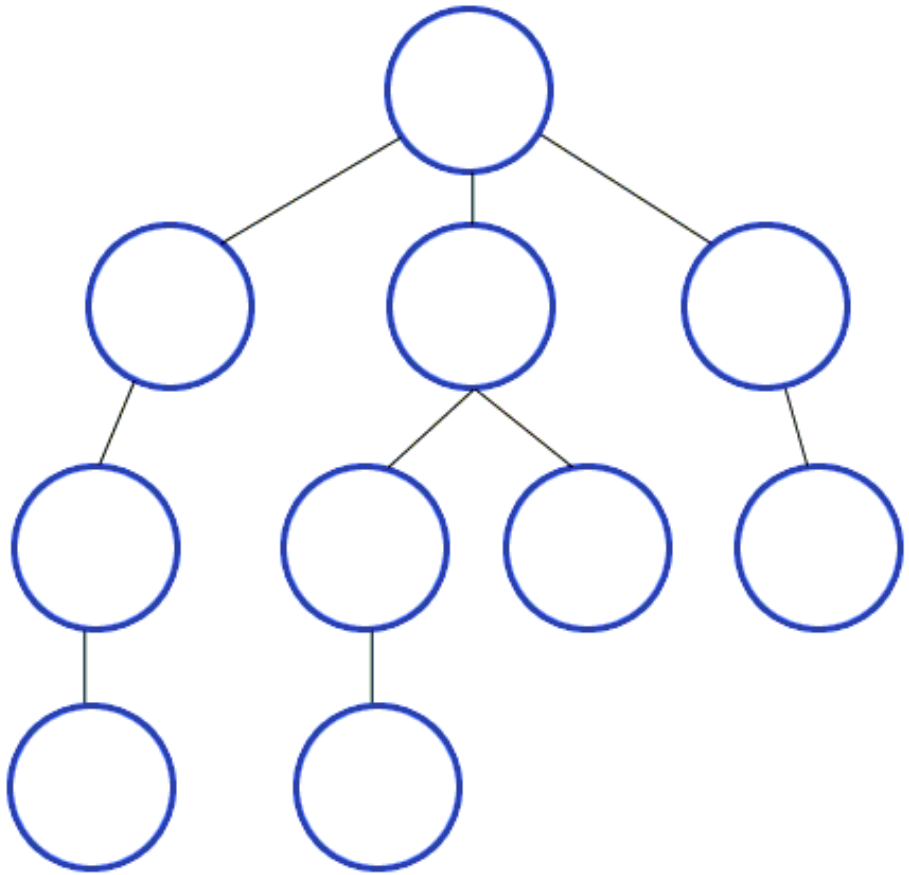
- DFS(1): v=1; dikunjungi[1]=true; DFS(2)
  - DFS(2): v=2; dikunjungi[2]=true; DFS(3)
    - DFS(3): v=3; dikunjungi[3]=true; DFS(6)
      - DFS(6): v=6; dikunjungi[6]=true; DFS(8)
        - DFS(8): v=8; dikunjungi[8]=true; DFS(4)
          - DFS(4): v=4; dikunjungi[4]=true;

        DFS(8): DFS(5)
          - DFS(5): v=5; dikunjungi[5]=true

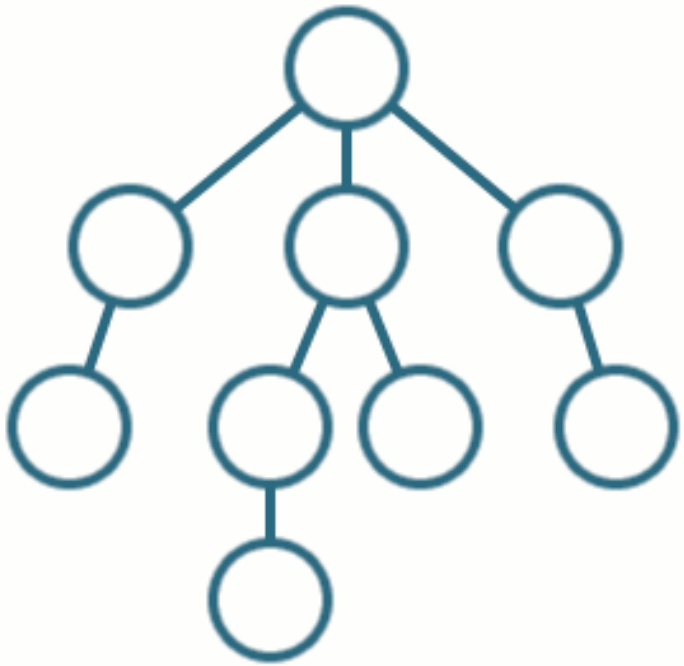
        DFS(8): DFS(7)
          - DFS(7): v=7; dikunjungi[7]=true

Urutan simpul2 yang dikunjungi: 1, 2, 3, 6, 8, 4, 5, 7


9
12
1
11
3
7
5
6
2
10
8
4

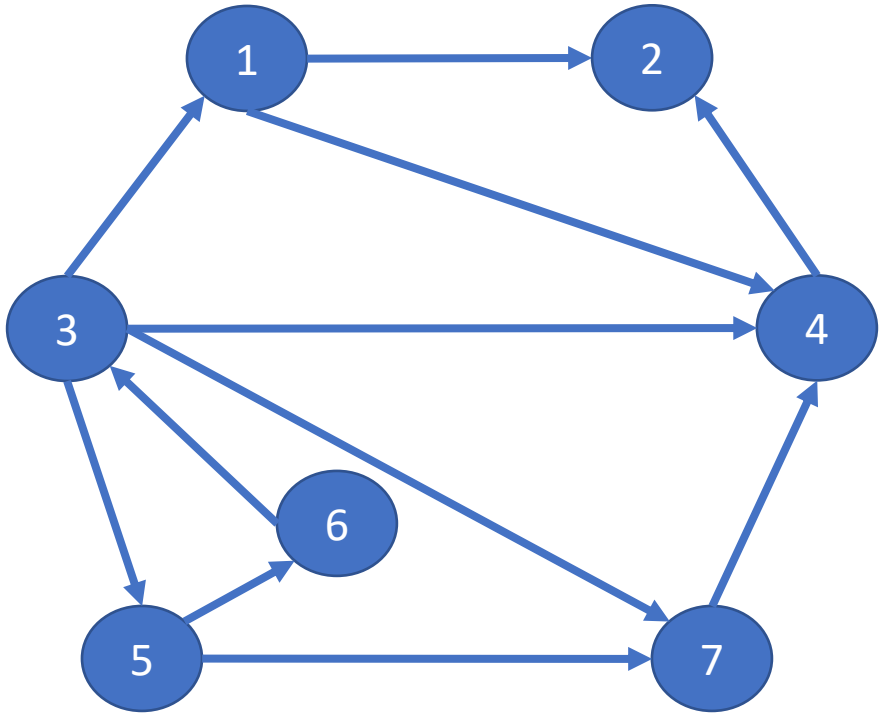


DFS



BFS

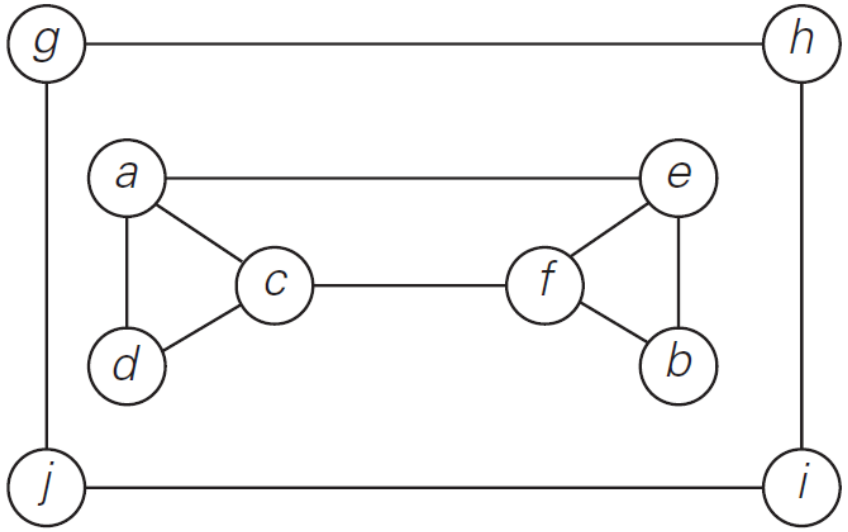
Contoh (hal 113)



- Khusus untuk graf berarah, beberapa simpul mungkin tidak dapat dicapai dari simpul awal. Coba dengan simpul yang belum dikunjungi sebagai simpul awal. (hal 113)

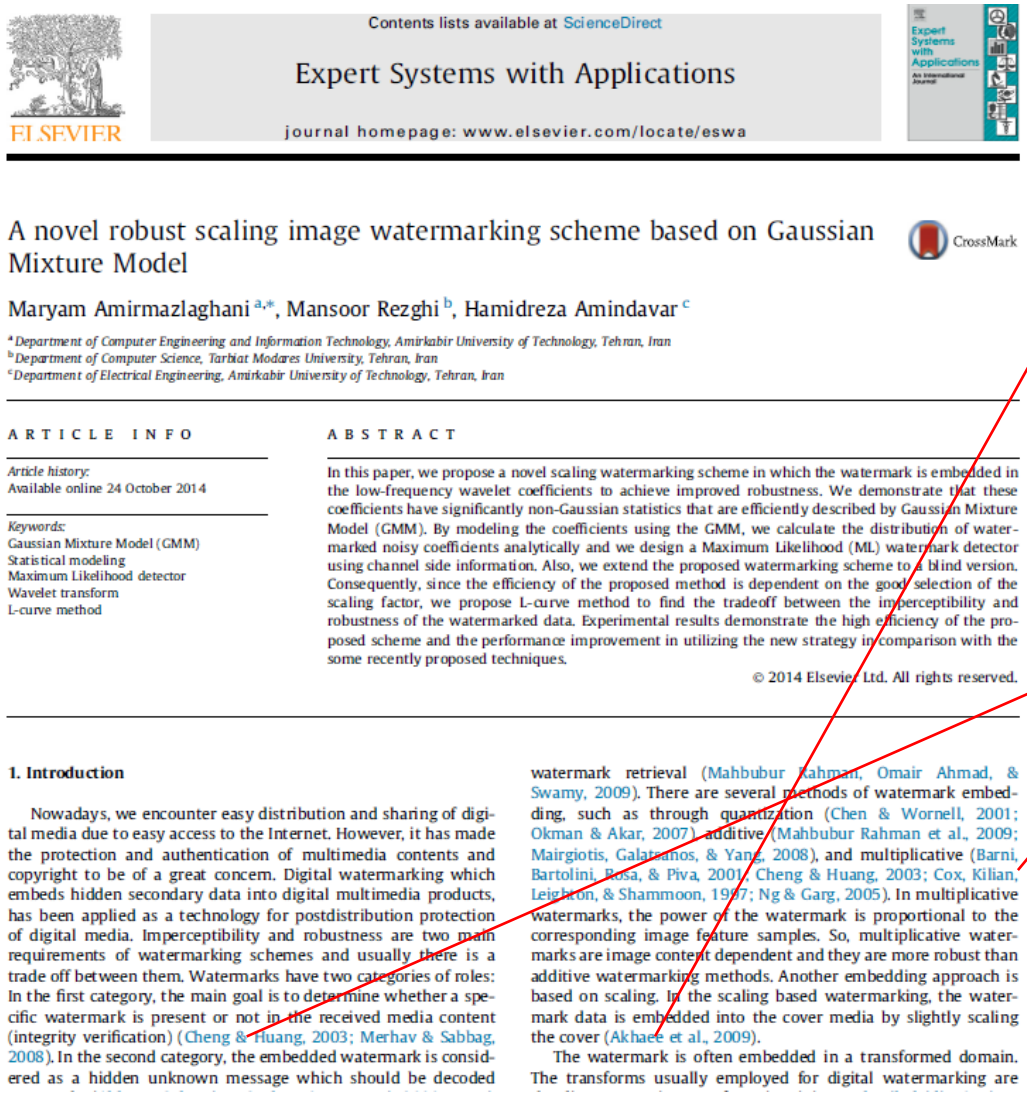
- DFS (1): 1-2-4-3-5-6-7
- BFS (1): 1-2-4-3-5-7-6

Contoh Lain



- Bagaimana penelusuran graf dengan BFS?
- Bagaimana Penelusuran graf dengan DFS

Penerapan BFS dan DFS: Citation Map



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A novel robust scaling image watermarking scheme based on Gaussian Mixture Model

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ABSTRACT

In this paper, we propose a novel scaling watermarking scheme in which the watermark is embedded in the low-frequency wavelet coefficients to achieve improved robustness. We demonstrate that these coefficients have significantly non-Gaussian statistics that are efficiently described by Gaussian Mixture Model (GMM). By modeling the coefficients using the GMM, we calculate the distribution of watermarked noisy coefficients analytically and we design a Maximum Likelihood (ML) watermark detector using channel side information. Also, we extend the proposed watermarking scheme to a blind version. Consequently, since the efficiency of the proposed method is dependent on the good selection of the scaling factor, we propose L-curve method to find the tradeoff between the imperceptibility and robustness of the watermarked data. Experimental results demonstrate the high efficiency of the proposed scheme and the performance improvement in utilizing the new strategy in comparison with the some recently proposed techniques.

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1. Introduction

Nowadays, we encounter easy distribution and sharing of digital media due to easy access to the Internet. However, it has made the protection and authentication of multimedia contents and copyright to be of a great concern. Digital watermarking which embeds hidden secondary data into digital multimedia products, has been applied as a technology for postdistribution protection of digital media. Imperceptibility and robustness are two main requirements of watermarking schemes and usually there is a trade off between them. Watermarks have two categories of roles: In the first category, the main goal is to determine whether a specific watermark is present or not in the received media content (integrity verification) (Cheng & Huang, 2003; Merhav & Sabbag, 2008). In the second category, the embedded watermark is considered as a hidden unknown message which should be decoded watermark retrieval (Mahbubur Rahman, Omair Ahmad, & Swamy, 2009). There are several methods of watermark embedding, such as through quantization (Chen & Wornell, 2001; Okman & Akar, 2007), additive (Mahbubur Rahman et al., 2009; Mairgiotis, Galatsanos, & Yang, 2008), and multiplicative (Barni, Bartolini, Rosa, & Piva, 2001; Cheng & Huang, 2003; Cox, Kilian, Leighton, & Shammoon, 1997; Ng & Garg, 2005). In multiplicative watermarks, the power of the watermark is proportional to the corresponding image feature samples. So, multiplicative watermarks are image content dependent and they are more robust than additive watermarking methods. Another embedding approach is based on scaling. In the scaling based watermarking, the watermark data is embedded into the cover media by slightly scaling the cover (Akhaee et al., 2009).

The watermark is often embedded in a transformed domain. The transforms usually employed for digital watermarking are

References

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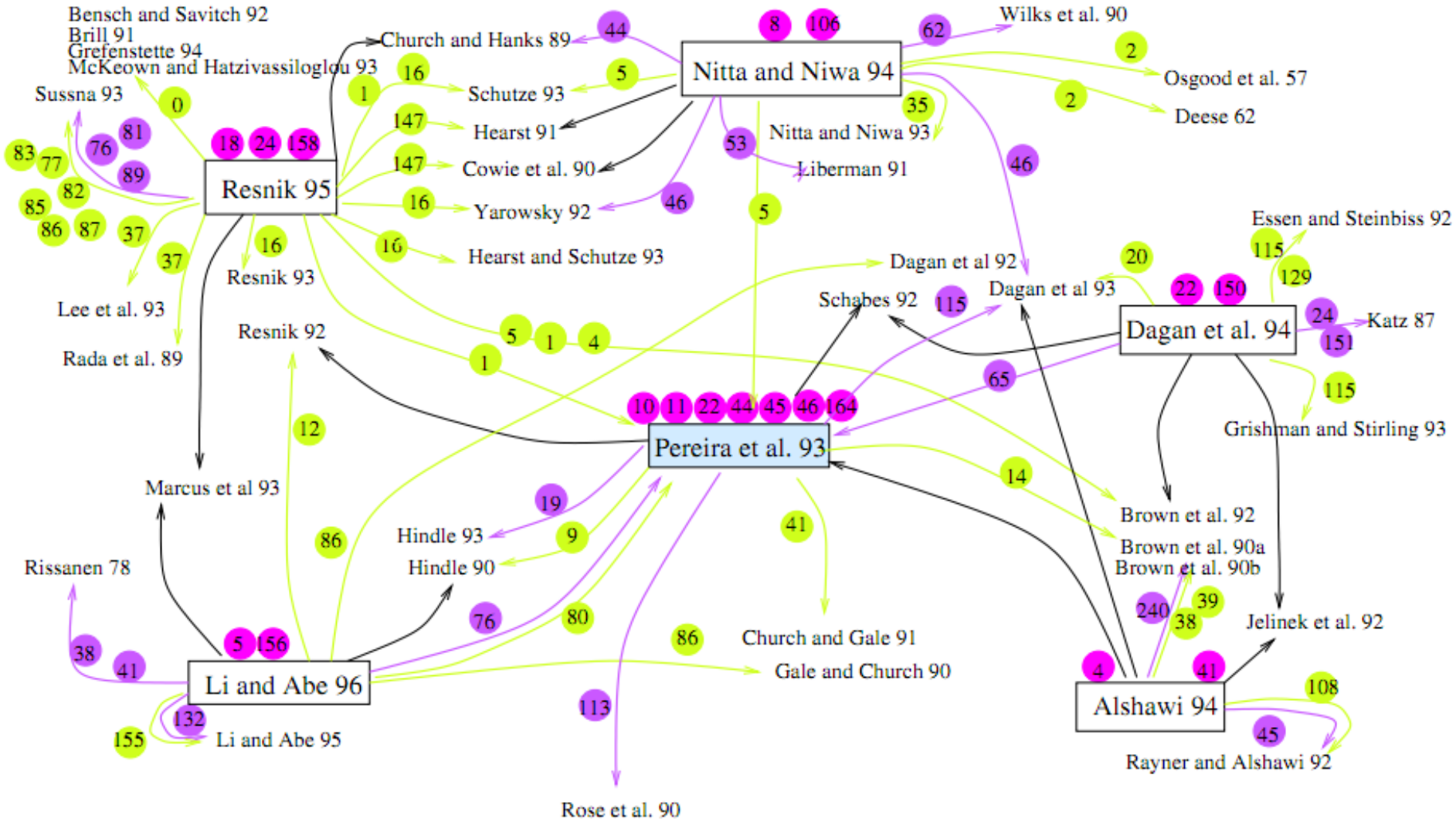
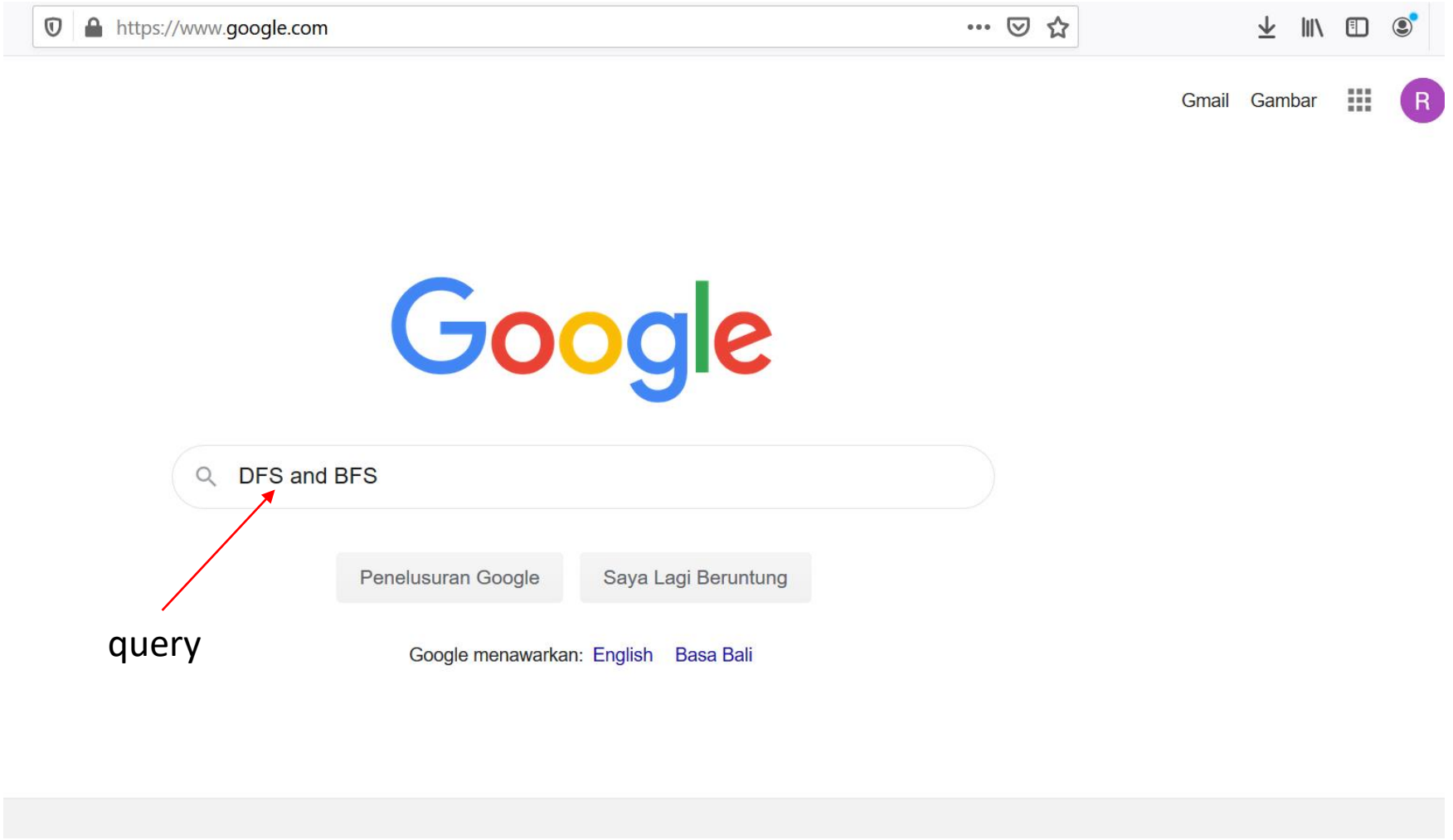
Citation Map:



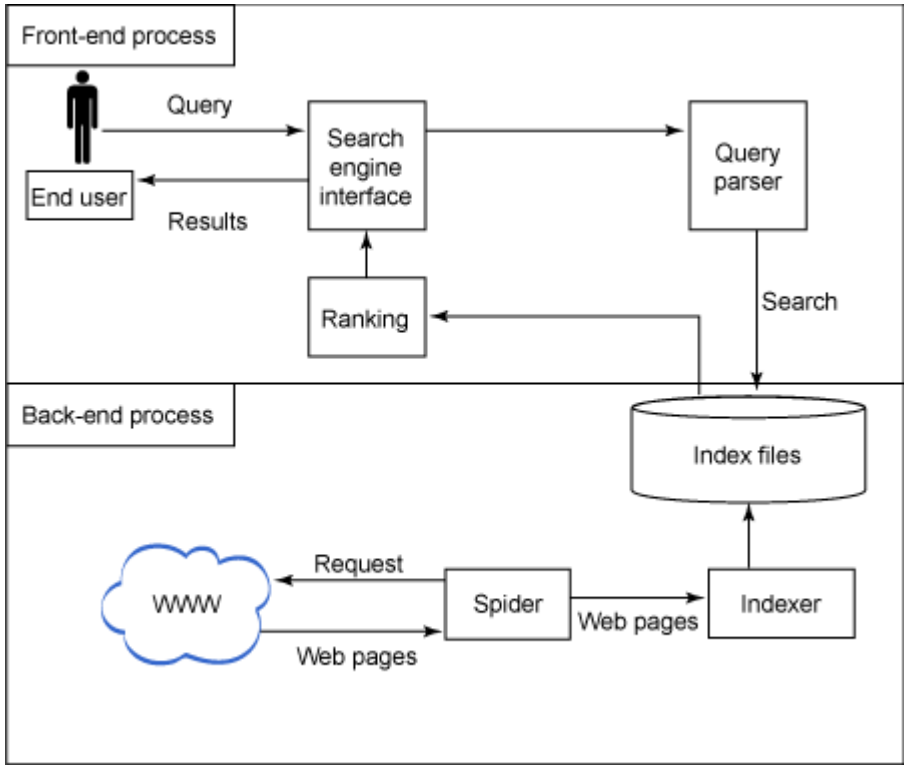
Sumber: Teufel (1999), Argumentative Zoning

Penerapan BFS dan DFS: *Web Spider*



Penerapan BFS dan DFS: *Web Spider*

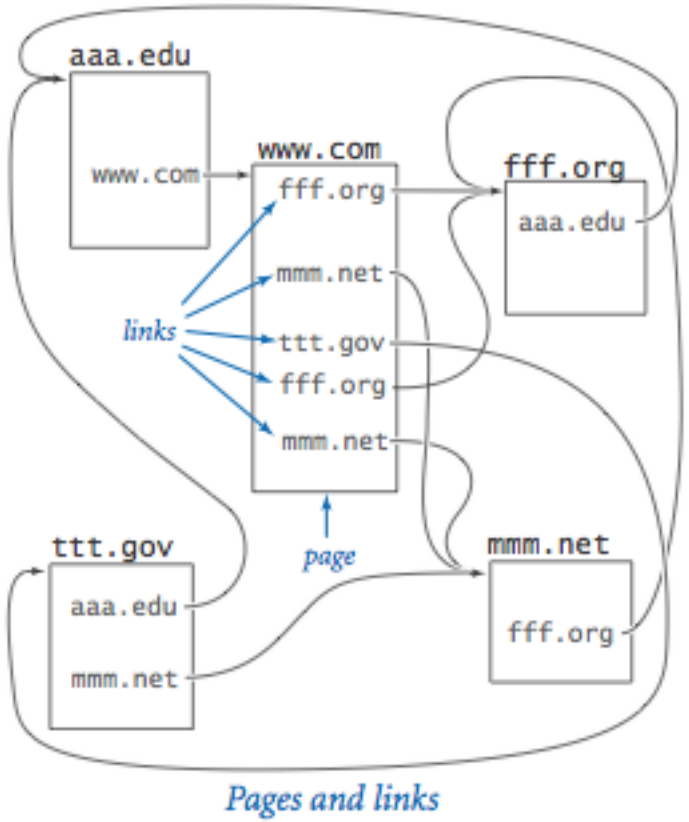
Arsitektur umum mesin pencari



http://www.ibm.com/developerworks/web/library/wa-lucene2/

- Secara periodik, *web spider* menjejalahi internet untuk mengunjungi halaman-halaman web

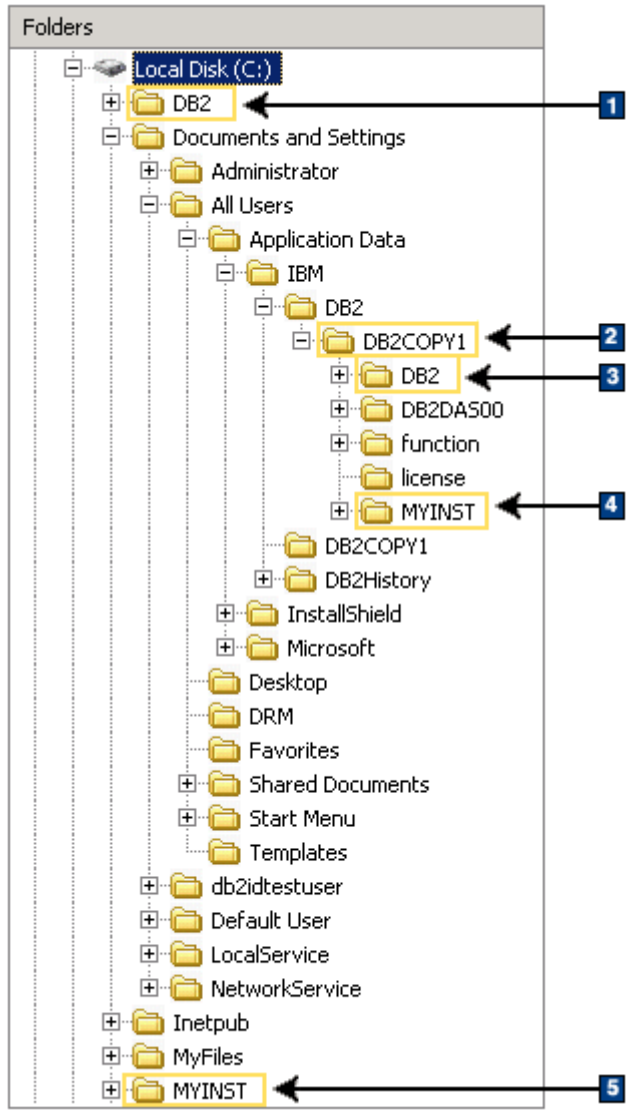
Web Spider: Penjelajahan Web

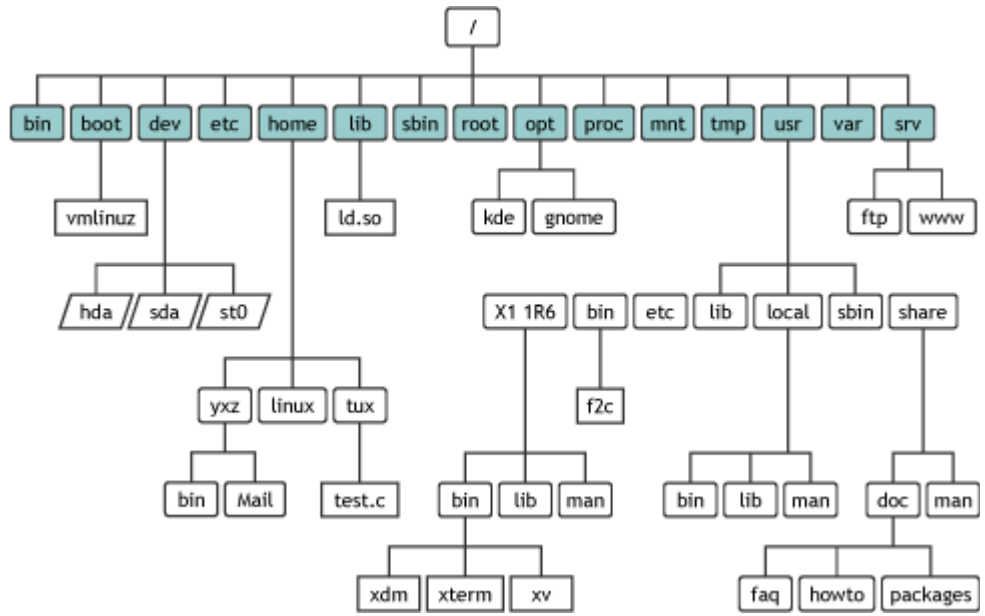


http://introcs.cs.princeton.edu/java/16pagerank/

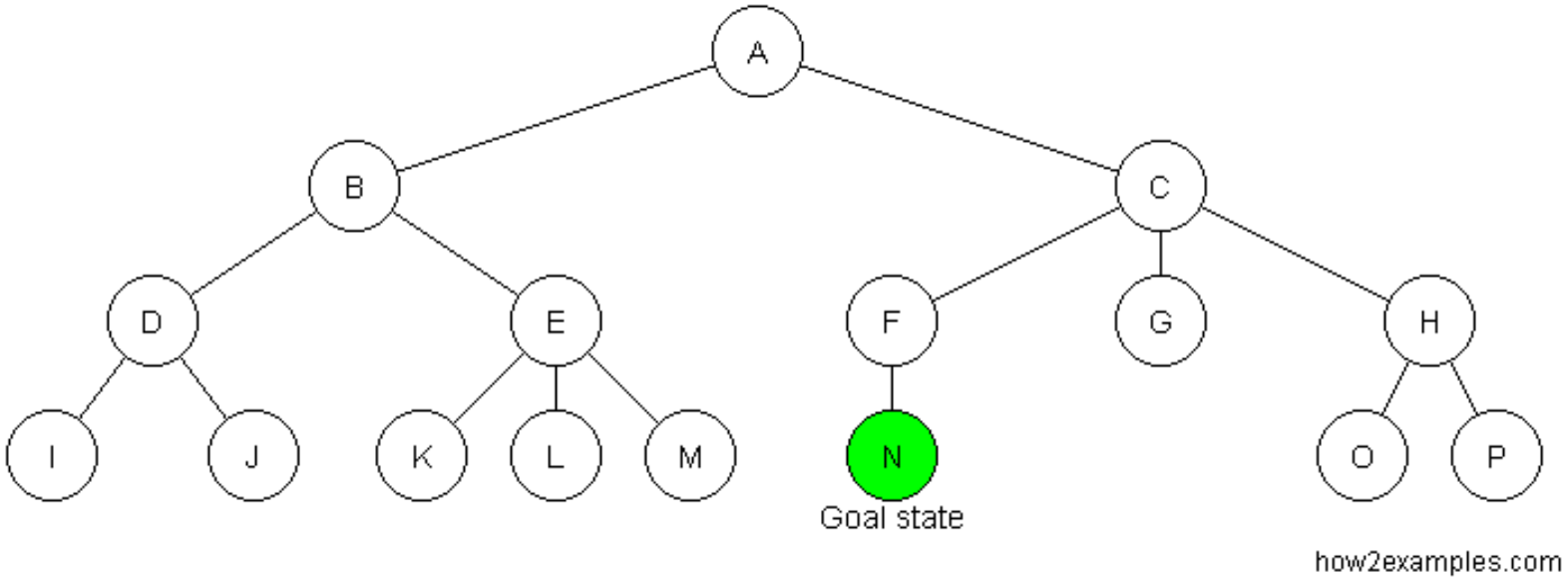
- Halaman web dimodelkan sebagai graf berarah
  - Simpul menyatakan halaman web (web page)
  - Sisi menyatakan link ke halaman web
- Bagaimana teknik menjelajahi web? Secara DFS atau BFS
- Dimulai dari web page awal, lalu setiap link ditelusuri secara DFS sampai setiap web page tidak mengandung link.

DFS dan BFS untuk penelusuran direktori (folder)

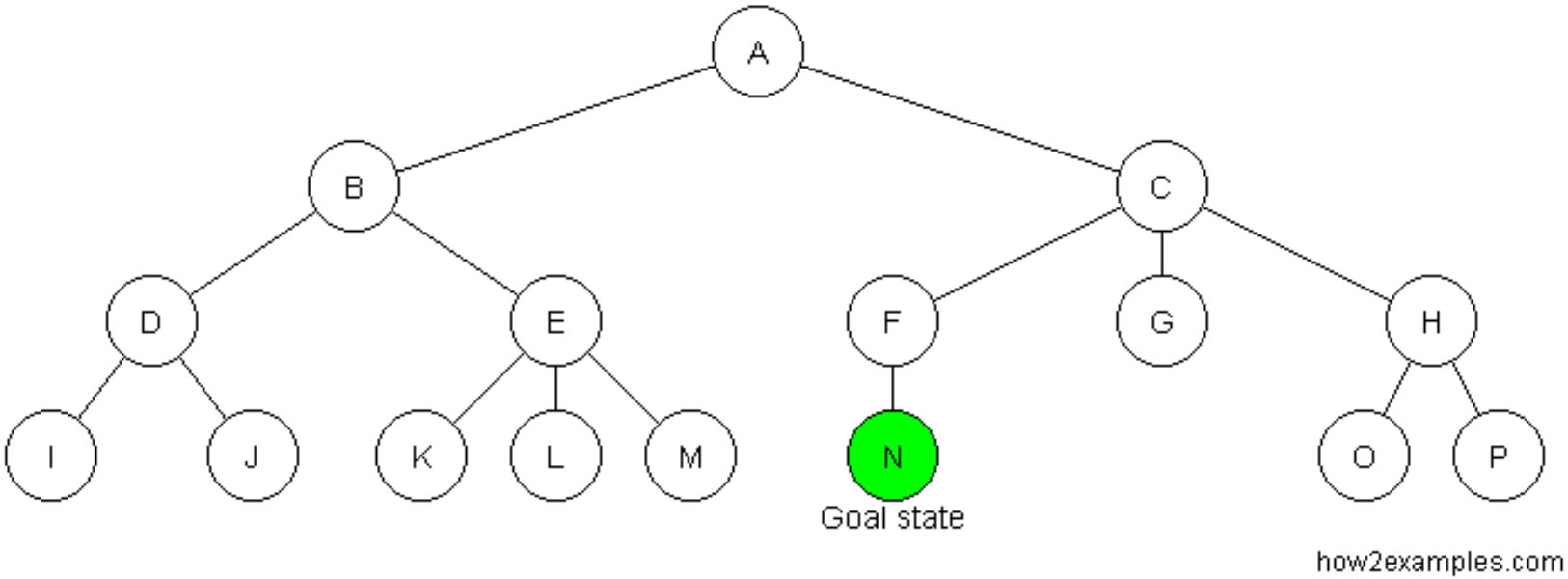




Pencarian dokumen di dalam direktori (folder) secara BFS



Pencarian dokumen di dalam direktori (folder) secara DFS



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