

Cryptanalysis of the Vigenère Cipher

The keyword of a Vigenère cipher describes the rotation among the Caesar cipher alphabets that are used. That rotation leads to patterns that can be exploited by a cryptanalyst. If we know the length of the keyword, we can often determine the keyword and, hence, decrypt all messages encrypted with that keyword.

Here is a ciphertext message that has been encrypted with a Vigenère cipher.

```
nifon aicum niswt luvet vxshk nissx wsstb husle chsnv ytsro  
cdsoy nisgx lnona chvch gnonw yndlh sfrnh npblr yowgf unoca  
cossu ouoll iuvef issoe xgosa cpbew uormh lftaf cmwak bbbdv  
cqvek muvil qbgnh ntiri ljgig atwnv yuvev iorim cpbsb hxviv  
buvet vxshk uorim mjbdb pjrut fbueg ntgof yuwmx mio dm ipdek  
uuswx lfjek sewfy yssnm zscmm bpgeb huvez ysaag usaew mffvb  
wfgim qpilw bbjeu yfbef vbftr mtwnz uorig wpbvx hjsnm zpfag  
uhsnm npglb jbqrh mttrh huwek mpfak ljjen hbbnh ooqew vzdak  
udvum yucbx yoquf vffew vzonx hjumt lfgef vmwnz uxsiz bumag  
xbbtb kvotx xumpx qswtx l
```

Assume that, somehow, we have discovered that the keyword has length five (which is conveniently the same as the size of the blocks). Then the first letter of each block is encrypted with the same row of the Vigenère square – they are encrypted with the same Caesar cipher. Similarly, the second letter of each block is encrypted with the same row – the same Caesar cipher. The third letters with the same Caesar cipher. The fourth letters with the same Caesar cipher. And, the fifth letters with the same Caesar cipher.

Because Caesar ciphers are easily broken by frequency analysis, we can discover the letters of the keyword. Here is how we can proceed.

Strip off the first letters of each block and do a frequency analysis on the result. They should have all been encrypted with the same Caesar cipher.

Alphabet number one – first letters of each block

A	11
B	11111
C	111111111
D	
E	
F	1
G	1
H	1111111
I	1111
J	1
K	1
L	111111111
M	1111111
N	111111111
O	11
P	1
Q	111
R	
S	11
T	
U	1111111111
V	1111111
W	111
X	111
Y	11111111111
Z	11

It appears that ciphertext Y corresponds to plaintext e. (Not just because it is the most frequent letter but because all the high frequency letter patterns fit – U would correspond to a; C would correspond to i; H and I would correspond to n and o; and L, M, and N would correspond to r, s, and t.)

Now recall that when we are encrypting using a Vigenère square plaintext a corresponds to the first letter of the row being used – the letter of the keyword being used. So, it appears that (because U corresponds to a) the first letter of the keyword is u.

The keyword is u _ _ _ _.

Alphabet number two – second letters of each block

A	
B	11111111
C	
D	11
E	1
F	11111111
G	1
H	111
I	1111111
J	11111
K	
L	
M	11
N	1111
O	11111111
P	1111111111
Q	1
R	
S	1111111
T	111111
U	11111111111111
V	1
W	
X	1111
Y	
Z	11

It appears that ciphertext F corresponds to plaintext e.

So, it appears that (because B corresponds to a) the second letter of the keyword is b.

The keyword is u b _ _ _.

Alphabet number three – third letters of each block

A	11
B	111111111
C	111
D	111
E	
F	111111
G	1111111
H	
I	11
J	111
K	
L	
M	11
N	
O	111111111
P	
Q	111
R	111111
S	111111111111111111
T	11
U	11
V	1111111111
W	111111111
X	
Y	
Z	

It appears that ciphertext *S* corresponds to plaintext *e*.

So, it appears that the third letter of the keyword is *o*.

The keyword is *u b o _ _*. (Perhaps, you can already guess the keyword.)

Alphabet number four – fourth letters of each block

A	1111111
B	1
C	11
D	111
E	11111111111111111111
F	1
G	11
H	11
I	11111111
J	
K	
L	111111
M	1111
N	11111111111111
O	1111
P	1
Q	
R	11111
S	1111
T	1111
U	1111
V	11
W	11
X	
Y	
Z	

It appears that ciphertext E corresponds to plaintext e.

So, it appears that the third letter of the keyword is a.

The keyword is u b o a _.

Alphabet number five – fifth letters of each block

A	11
B	11111111
C	
D	
E	11
F	11111111
G	111111
H	11111111
I	1
J	
K	1111111111
L	11
M	1111111111
N	11
O	1
P	
Q	
R	1
S	
T	111111
U	11
V	11111
W	111111
X	1111111111
Y	11
Z	1111

It appears that ciphertext X corresponds to plaintext e.

So, it appears that the last letter of the keyword is t.

The keyword is u b o a t.

So, knowing just the length of the keyword, we were able to determine the keyword.

Two methods give us information about the length of the keyword of a Vigenère cipher – the Kasiski test and the Friedman test. We will discuss the first in this section and the second in the next section.

First, some history.

The Cryptanalysts

The Vigenère cipher might first have been broken by the English mathematician Charles Babbage (1792 – 1871); Kahn quotes Babbage as saying “an indistinct glimpse of defeating it presented itself vaguely to my imagination.” But, if Babbage had a solution, he never published it. Babbage apparently had the tendency to never be satisfied with a work and to continue to refine things; so, he might never have been satisfied enough with his solution to publish it.

Friedrich Kasiski (1805 – 1881) is credited with breaking the Vigenère cipher in 1863. From the Sixteenth Century until the Nineteenth Century the cipher was generally considered to be secure. We will use Kasiski’s technique to determine the length of the keyword.

In the Twentieth Century, William Frederick Friedman (1891 – 1969), the dean of American cryptologists, developed a statistical method to estimate the length of the keyword.

Friedrich Kasiski

“Friedrich Kasiski was born in November 1805 in a western Prussian town and enlisted in an East Prussian infantry regiment at the age of 17.

He moved up through the ranks to become a company commander and retired in 1852 as a major. Although he had become interested in cryptology during his military career, it was not until the 1860s that he put his ideas on paper. In 1863 his 95-page text *Die Geheimschriften und die Dechiffirkunst* (*Secret Writing and the Art of Deciphering*) was published. A large part of its contents addressed the solution of polyalphabetic ciphers with repeating keywords, a problem that had tormented cryptanalysts for centuries.

Disappointed by the lack of interest in his findings, Kasiski turned his attention to other activities including anthropology. He took part in artifacts searches and excavations and wrote numerous archeological articles for scholarly journals. He died in May 1881 not realizing the significance of his cryptanalytic findings.” Wrixon, Fred B., *Codes, Ciphers & other Cryptic & Clandestine Communication: Making and breaking secret messages from hieroglyphs to the internet*, Black Dog & Leventhal Publishers.

The Kasiski Test (or the Kasiski Attack)

Here is a message enciphered with a Vigenère cipher. (It is taken from: Beutelspacher, Albrecht, *Cryptology: An introduction to the Art and Science of Enciphering, Encrypting, Concealing, Hiding and Safeguarding Described Without any Arcane Skullduggery but not Without Cunning Wagery for the Delectation and Instruction of the General Public*, Mathematical Association of America, 1996.)

DBZMG	AOIYS	OPVFH	OWKBW	XZPJL	VVRFG	NBKIX
DVUIM	OPFQL	VVPUD	KPRVW	OARLW	DVLMW	AWINZ
DAKBW	MMRLW	QIICG	PAKYU	CVZKM	ZARPS	DTRVD
ZWEYG	ABYYE	YMGYF	YAFHL	CMWLW	LCVHL	MMGYL
DBZIF	JNCYL	OMIAJ	JCGMA	IBVRL	OPVFW	OBVLK
OPVUJ	ZDVLQ	XWDGG	IQEYF	BTZMZ	DVRMM	ANZWA
ZVKFQ	GWEAL	ZFKNZ	ZZVCK	VDVLQ	BWFXU	CIEWW
OPRMU	JZIYK	KWEXA	IOIYH	ZIKYV	GMKNW	MOIIM
KADUQ	WMWIM	ILZHL	CMTCH	CMINW	SBRHV	OPVSO
DTCMG	HMKCE	ZASYD	JKRNW	YIKCF	OMIPS	GAFZK
JUVGM	GBZJD	ZWWNZ	ZVLGT	ZZFZS	GXYUT	ZBJCF
PAVNZ	ZAVWS	IJVZG	PVUVQ	NKRHF	DVXNZ	ZKZJZ
ZZKYP	OIEXX	MWDNZ	ZQIMH	VKZHY	DVKYD	GQXYF
OOLYK	NMJGS	YMRML	JBYYF	PUSYJ	JNRFH	CISYL

N

We begin the attack by frequency analysis.

A	11111111111111111111		19
B	1111111111111111		14
C	1111111111111111		16
D	11111111111111111111	20	
E	11111111		8
F	11111111111111111111		19
G	11111111111111111111	20	
H	111111111111		12
I	111111111111111111111111111111		26
J	1111111111111111		16
K	1111111111111111111111111111	25	
L	11111111111111111111		22
M	1111111111111111111111111111111111		32
N	1111111111111111		16
O	11111111111111111111		18
P	1111111111111111		16
Q	1111111111	10	
R	1111111111111111		14
S	111111111111		11
T	111111		6
U	111111111111		11
V	111111111111111111111111111111111111		34
W	11111111111111111111111111111111		28
X	1111111111	10	
Y	1111111111111111111111111111		27
Z	11		<u>41</u>
			491

The "relatively equal" frequencies suggest multiple alphabets – a polyalphabetic cipher, which, for us, would suggest a Vigenère cipher.

Here's the idea behind the Kasiski test. Consider a Vigenère cipher with keyword *Galois*. (My favorite mathematician.)

abcdefghijklmnopqrstuvwxyz
GHIJKLMNOPQRSTUVWXYZABCDEF
ABCDEFGHIJKLMNOPQRSTUVWXYZ
LMNOPQRSTUVWXYZABCDEFGHIJK
OPQRSTUVWXYZABCDEFGHIJKLMN
IJKLMNOPQRSTUVWXYZABCDEFGHI
STUVWXYZABCDEFGHIJKLMN

Think of a common trigraph – say, the – and assume that it appears twice in the plaintext message.

If the is not encrypted by the same three alphabets at both locations, the two ciphertexts of the would be different.

GALOISGALOISGALOISGALOISGALOIS . . . GALOISGALOISGALOIS
the the
ZHP TSS

But, if we are lucky and the is encrypted by the same three alphabets, we would see a duplicate trigraph.

GALOISGALOISGALOISGALOISGALOIS . . . GALOISGALOISGALOIS
the the
ZHP ZHP

What is important to notice is that the distance between the beginnings of the ZHP trigraphs is a multiple of the length of the keyword. This provides information about the length of the keyword.

So, we search through the ciphertext for trigraphs (or strings of other lengths), and we look for repetitions. Sometimes, of course, the repetitions are just accidental – two different strings of three letters are encrypted into the same three-letter string by different alphabets, but sometimes the repetitions correspond to the same three-letter string being encrypted by the same three alphabets. These are the occurrences that we would like to discover.

Here are the trigraphs of the ciphertext with the number of repetitions shown in ():

AOI ARL AWI AKB AKY ARP ABY AFH AJJ AIB ANZ AZV ALZ AIO ADU
ASY AFZ AVN AVW

BZM BWX BKI BWM BYY(2) BZI BVR BVL BTZ BWF BRH BZJ BJC

CGP CVZ CMW CVH CYL CGM CKV CIE CMT CHC CMI CMG CEZ CFO CFP
CIS

DBZ(2) DVU DKP DVL(3) DAK DTR DZW DGG DVR DUG DTC DJK DZW
DVX DNZ DVK DGQ

EYG EYM EYF EAL EWW EXA EZA EXX

GAO GNB GPA GAB GYF GYL GMA GGI GIQ GWE GMK GHM GAF GMG GBZ
GTZ GXY GPV GQX GSY

HOW HLC(2) HLM HZI HCM HVO HMK HFD HVK HYD HCI

IYS IXD IMO INZ IIC ICG IFJ IAJ IBV IQE IEW IYK IOI IYH IKY
IIM IMK IMI ILZ INW IKC IPS IJV IEX IMH ISY

JLV JNC JJC JCG JZD JZI JKR JUV JDZ JCF JVZ JZZ JGS JBY JJN
JNR

KBW(2) KIX KPR KYU KMZ KOP KFQ KNZ KVD KKW KWE KYV KNW KAD
KCE KRN KCF KJU KRH KZJ KYP KZH KYD KNM

LVV(2) LWD LMW LWQ LCM(2) LWL LCV LMM LDB LOM LOP LKO LQX
LZF LQB LZH LGT LYK LJB

MGA MOP MWA MMR MRL MZA MGY(2) MWL MMG MIA MAI MZD MMA MAN
MUJ MKN MOI MKA MWI MIL MTC MIN MGH MKC MIF MGB MWD MHV MJG
MRM MLJ

NBK NZD NCY NZW NWM NWS NWY NZZ(5) NKR NMJ NRF

OIY OPV(4) OWK OPF OAR OMI(2) OBV OPR OIY OII ODT OIE OCL
OLY

PVF(2) PJL PFQ PUD PRV PAK PSD PVU(2) PRM PVS PSG PAV POI
PUS

QLV QII QXW QEY QGW QBW QWM QNK QIM QXY

RFG RVW RLW(2)RPS RVD RLO RMM RMU RHV RNW RHF RML RFH

SOP SDT SBR SOD SYD SGA SGX SIJ SYM SYJ SYL

TRV TZM TCH TCM TZZ TZB

UIM UDK UCV UJZ(2) UCI UQW UVG UTZ UVQ USY

VFH VVR VRF VUI VVP VPU VWO VLM VZK VDZ VHL VRL VFW VLK VUJ
VLQ(2) VRM VKF VCK VDV VGM VOF VSO VGM VLG VNZ VWS VZG VUV
VQN VXN VKZ VKY

WKB WXZ WOA WDV WAW WIN WMM WQI WEY WLW WLC WOB WDG WAZ WEA
WFX WWO WOP WEX WMO WMW WIM WSB WYI WVN WNZ WSI WDN

XZP XDV XWD XUC XAI XYU XNZ XXM XMW XYF

YSO YUC YGA YYE YEY YMG YFY YAF YLD YLO YFB YKK YMZ YVG YDJ
YIK YUT YPO YDV YDG YFO YKN YMR YFV YFP YJJ YLN

ZMG ZPJ ZDA ZKM ZAR ZWE ZIF ZDV(2) ZMZ ZWA ZVK ZFK ZZZ(2)
ZZV(2) ZVC ZIY ZIK ZHL ZAS ZKJ ZJD ZWW ZVL ZZF ZFZ ZSG ZBJ
ZZA ZAV ZGP ZZK(2) ZKZ ZJZ ZKY ZZQ ZQI ZHY

Whew!

After identifying the repeated trigraphs, we look at their spacing.

BYY	360		BYY				
DBZ	140		DBZ				
DVL	121		DVL	50		DVL	
HLC	170		HLC				
KBW	55		KBW				
LVV	20		LVV				
LCM	170		LCM				
MGY	20		MGY				
NZZ	140		NZZ	25		NZZ	25
	NZZ	20		NZZ	10		NZZ
OPV	155		OPV			OPV	135
	OPV						
OMI	190		OMI				
PVF	155		PVF				
PVU	224		PVU				
RLW	20		RLW				
UJZ	71		UJZ				
VLQ	50		VLQ				
ZZV	139		ZZV				
ZZK	6		ZZK				
ZDV	19		ZDV				
ZZZ	195		ZZZ				

Remember that we are looking for a length that is a common divisor of "all" of these lengths – well, not “all” because some repetitions are accidental – but most. The bolded portions of the table seem to indicate that the length of the keyword might be five.

Now we return to the ciphertext and separate it into its five alphabets. We begin with the first letter and take every fifth letter after it. Then take the second letter and every fifth letter after it. Then take the third letter and every fifth after it. Etc.

If we determined the length of the keyword correctly, we should have partitioned the ciphertext into five sets of ciphertext letters each of which was encrypted with a Caesar cipher. Then we proceed as we did for the first example of this section.

Let us look at each alphabet separately.

Alphabet number one

A	1111
B	11
C	111111
D	1111111111
E	
F	
G	111111
H	1
I	11111
J	1111111
K	111
L	1
M	1111
N	1111
O	11111111111111
P	1111
Q	1
R	
S	1
T	
U	
V	1111
W	1
X	11
Y	1111
Z	1111111111111111

It appears that Z might correspond to e; that would make V correspond to a.
The first letter of the keyword would be v. v _ _ _ _

Alphabet number two

A	1111111111
B	1111111111
C	11
D	11
E	
F	1
G	
H	
I	111111
J	1
K	1111
L	1
M	11111111111111
N	111
O	1111
P	1111111
Q	111
R	
S	
T	111
U	11
V	111111111111
W	111111111
X	1
Y	
Z	11111

It appears that M might correspond to e; that would make I correspond to a.
The second letter of the keyword would be i. v i _ _ _ (Guess?)

Alphabet number three

A	
B	
C	11
D	111
E	111111
F	11111
G	111
H	
I	1111111111
J	11
K	111111111111
L	111
M	
N	
O	
P	11
Q	
R	11111111111111
S	111
T	1
U	11
V	11111111111111
W	111
X	11
Y	111
Z	111111111

It appears that V might correspond to e; that would make R correspond to a.
The third letter of the keyword would be r. v i r _ _ (Guess?)

Alphabet number four

A	11
B	11
C	111111
D	
E	
F	11111
G	1111
H	111111
I	11111
J	111
K	1
L	111111
M	111111111
N	111111111
O	
P	11
Q	1
R	1
S	1
T	
U	1111
V	111
W	111
X	111
Y	11111111111111111111
Z	111

It appears that Y might correspond to e; that would make U correspond to a. The fourth letter of the keyword would be u. v i r u _ (Not many possibilities.)

Alphabet number five

A	111
B	
C	
D	11111
E	11
F	11111111
G	1111111
H	11111
I	
J	111
K	11111
L	111111111111
M	111111
N	
O	1
P	1
Q	11111
R	
S	111111
T	11
U	111
V	11
W	111111111111
X	11
Y	1
Z	11111111

It appears that W might correspond to e; that would make S correspond to a. The fifth letter of the keyword would be s. The keyword would be v i r u s. Notice that we know the keyword, but we have not yet deciphered the message.

Friedman Attack (or Friedman Test)

Of course, for the Kasiski attack to work, it is necessary for the keyword to be repeated. In fact, what we depended upon was that we had a very long message and relatively short keyword so that the keyword was repeated many times and that when we stripped off the various Caesar cipher alphabets each alphabet contained enough letters to enable us to spot the shift.

In the next section, there is a discussion of a statistical attack on the Vigenère cipher that was developed by William Friedman (1891 – 1969). Friedman retired from the National Security Agency in 1955 after 35 years

of service with U.S. cryptological activities. Friedman transformed the methods and approaches of cryptology from the traditional into the modern. His wife Elizebeth was also a cryptologist and served at one point with the Coast Guard; she cryptanalyzed messages of the rumrunners. The two of them effectively debunked the theory that Francis Bacon used steganography to conceal and reveal that he was the author of Shakespeare's works (*The Shakespearean Cipher Examined*, 1957).

Friedman's statistical test is based upon frequency. One calculation is to determine the **index of coincidence** I . (Because Friedman denoted this number by the Greek letter kappa κ , it is sometimes called the Kappa Test.) I varies between approximately 0.038 and 0.065. A value of I near 0.065 would indicate that a monoalphabetic cipher (like a simple substitution cipher, a Caesar cipher, a multiplicative cipher, an affine cipher, or a keyword cipher) was used, and a value of I near 0.038 would indicate that a polyalphabetic cipher (like the Vigenère cipher) was used.

The other calculation is an **approximation to the length of the keyword** l .

The formulas for these calculations are developed in the next section.

For the example on which we used the Kasiski test, $I \approx 0.044$, which would indicate that this is probably a polyalphabetic cipher (for the example, we determined this by noting the even distribution of frequencies in the frequency analysis); and the approximate length of the keyword $l \approx 4.468$ (for the example, we used the Kasiski test to determine that the length was 5). Once these numbers are known, we proceed as we did in above – separate the ciphertext into alphabets and analyze each Caesar cipher to determine the letters of the keyword. The Kasiski test and the Friedman test, when used together, should give us a good guess at the length of the keyword.

For the exercises which follow, software written by Robert Lewand was used to encrypt the messages, determine letter and trigraph frequencies, calculate I , and calculate l . (Lewand's software will do these calculations. His software was written to accompany Lewand, Robert Edward, *Cryptological Mathematics*, Mathematical Association of America, 2000. It may be freely downloaded from

<http://faculty.goucher.edu/blewand/cryptomath/>

The software also encrypts and decrypts other ciphers and performs useful calculations.)

Exercises

1. Decrypt the message above. (There are a couple of errors in the plaintext.)

2. Here is a message that was encrypted with a Vigenère cipher with a keyword of length 6.

```
wgixf irtnx amwpz gfcln bztef roozn maour tlrno dsxjw
xxdan zhdix nqтта hogcm rwrvj numyb gxavt mgzdt ewlqs
wwwtm lgblk nrins ozgif bgnlm fpsqn xhvja ufgmj xyxum
hqsxv vztea bzrpt lrijy ivnto fywew uyfse beiaw vbimm
igwhq ceyth ppien udmiq nkmtw bnidy tgitm lcfqy fhegp
ghewv viqbi pwsqл itmtp avlzk mdmao gxmsf bgxls sokdm
eagyz azntg zdhvz rameg qifre snood yeqts tlreg dirpt
apirt bnqfe zwæz mзukd meavz qlitz gytln bxqvi ntkpg
ieugz ywczu bowrl gxlmn viqwm gpsqx mpwgs amaaz fhihv
ofehf bgfew nvjih sfmju sgywy grium rbehc zubep nukdi
gnqtf oxumc mr
```

2a. Find the first letter of the keyword.

2b. Find the second letter of the keyword.

2c. ... the third letter

2d. ...the fourth letter

2e. ... the fifth letter

2f. ... the sixth letter

2g. Find the keyword.

2h. Decrypt the message.

3. Here is a cipher. The results of the Friedman test are: $I \approx 0.0429$ and $l \approx 5.4572$.

3a. Use a Kasiski test to determine the length of the keyword.

```
tfrvg akceo ekiii brjgy obqgr nfbuk zimme tfyeb puwyr vqibj
ymeyv bfwyc actpu gwvvm akout cnzxx zvnaz ojbgu tpzkg ukcrv
punhk zlsth jqbtu fvbpn eypxn xdvcm giafv gvzly cnjgl ujunr
enfea uyiil vtthp lhreh vafgu lzkxh nccbh xuuel vymlz kgogn
ymoxb wbnvk exjws hnwbq amaud auoky scgom frgnz mbvor ufykz
vivye brxhz zvgke fvkga tfvvt rthue ukkyk prstc eznoe qrgsx
hgcwa jhhkw gnxfh zgnuc jmpzx xkprh kueku rbhvn eufio nbxwn
fknsu lzltk cojbg umbvv bxmbn mfzhh kprxt ccene coekg ohhfv
nyecx pgnbf coegv yujlg guekv kgntp hxvbr vquoy itbud ceogn
xwcil vbnjw szaym iyrrs jbbuw vcmgi afvgc gke
```

Here is a list of trigraphs that occur more than once:

Trigraph	Frequency	Trigraph	Frequency
kpr	3	kgo	2
afv	2	lzk	2
bgv	2	mbv	2
ceo	2	ngi	2
cmg	2	oek	2
coe	2	ogn	2
fvv	2	ojb	2
gia	2	rvq	2
gke	2	uek	2
gnx	2	ulz	2
iaf	2	vcm	2
ilv	2	vkg	2
jbg	2	yeb	2
jws	2	zkg	2
		zxx	2

3b. Find the keyword.

3c. Decrypt the message.

Good luck!

4a. The word `the` is encrypted exactly the same way twice in a ciphertext, and the distance between the two appearances is 24. What are the possible lengths of the keyword?

4b. The word `the` is encrypted exactly the same way twice in a ciphertext, and the distance between the two appearances is 15. What are the possible lengths of the keyword?

4c. The word `the` is encrypted exactly the same way twice in a ciphertext, and the distance between the two appearances is 7. What are the possible lengths of the keyword?

4d. The word `the` is encrypted exactly the same way twice in a ciphertext, and the distance between the two appearances is 6. What are the possible lengths of the keyword?

5. The following are the intervals between repeated trigraphs in a ciphertext. For each, what do you suspect the length of the keyword to be?

5a. 6, 12, 48, 7.

5b. 11, 32, 56, 3, 8, 16.

5c. 7, 35, 105, 2, 7, 42.

6. If the keyword of a Vigenère cipher has repeated letters, what problems might this cause for the Kasiski test? (It causes the same problems for the Friedman test.)

7. In the section “Cryptography of the Vigenère Cipher,” exercises 3, 6, 7, 8, and 9 describe variants of the Vigenère cipher. For each of these variants, describe how successful the Kasiski attack would be and how you might modify the attack.

8. Vigenère suggested using long keyphrases. Why is this a good idea?

9. If a short message were encrypted with a Vigenère cipher, how likely is it that we could successfully attack it?