

# 22 - Segmentasi Citra

(Bagian 1)

IF4073 Interpretasi dan Pengolahan Citra

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2021

# Segmentasi Citra

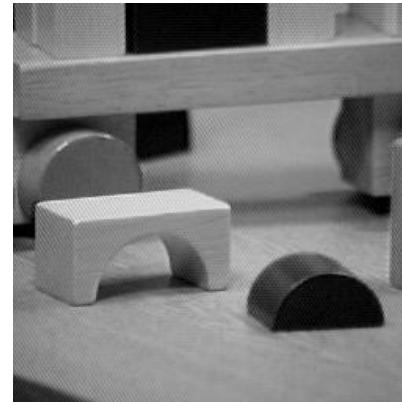
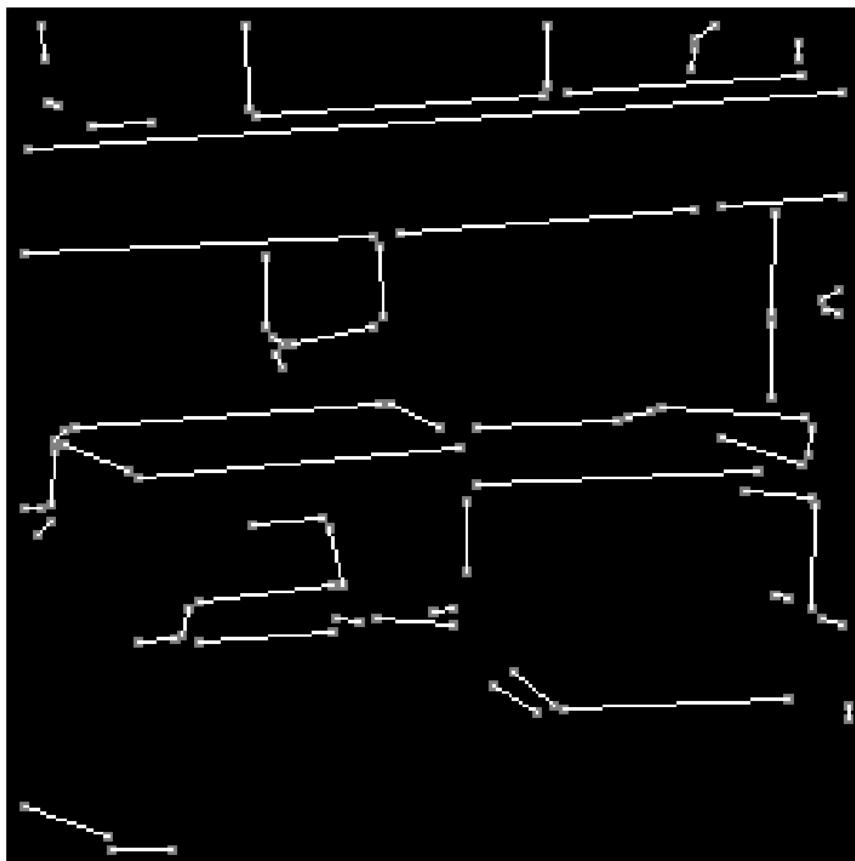
Segmentasi citra adalah operasi mempartisi citra menjadi sebuah koleksi yang terdiri dari sekumpulan pixel yang terhubung satu sama lain

1. menjadi **region-region**, yang biasanya mencakup keseluruhan citra
2. menjadi **struktur linier**, seperti
  - segmen garis
  - segmen kurva
3. Menjadi **bentuk-bentuk 2D**, seperti
  - lingkaran
  - elips
  - kotak, dll

# Contoh 1: Region



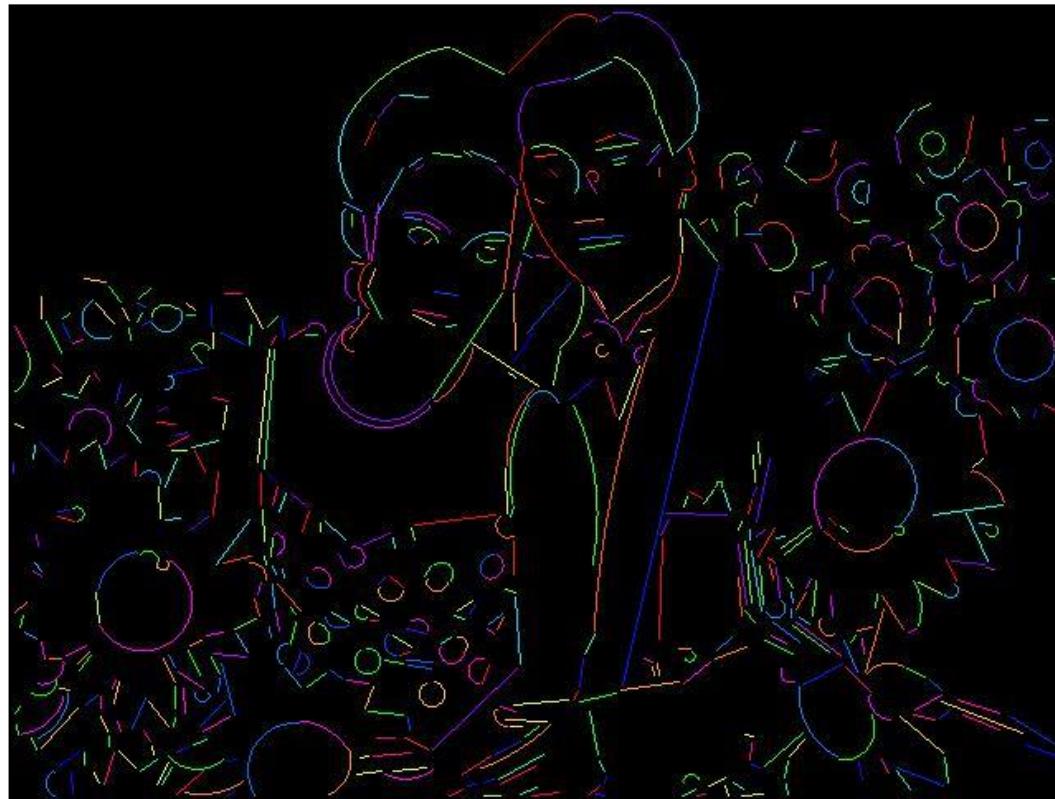
## Contoh 2: Garis lurus



Metode:

- Edge detection
- Hough transformation

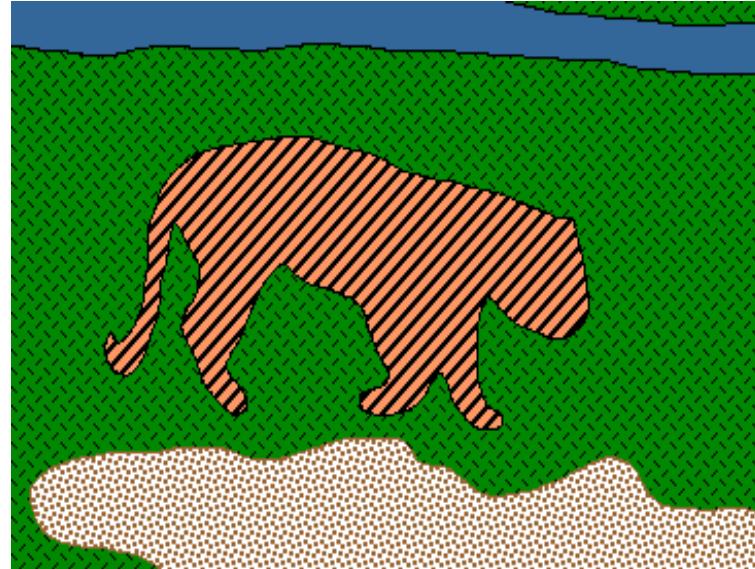
## Contoh 2: Garis dan lingkaran



Metode:

- Edge detection
- Hough transformation

- Segmentasi citra (*image segmentation*) menjadi sejumlah region bertujuan untuk:
  1. membagi citra menjadi semen-semen atau objek-objek yang berbeda.
  2. memisahkan objek dengan latar belakang



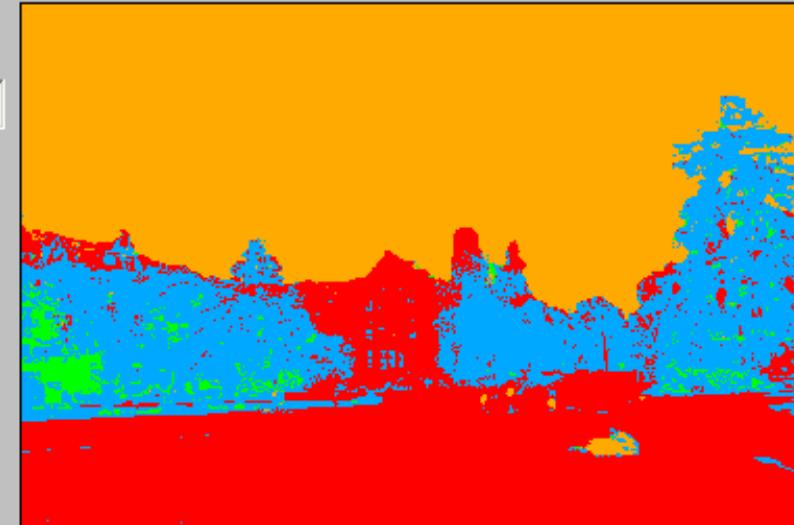
- Dengan membagi citra menjadi sejumlah segmen, kita dapat memproses hanya segmen penting atau segmen tertentu di dalam citra daripada memproses seluruh bagian citra

- Goal segmentasi citra adalah menemukan bagian citra yang koheren atau objek spesifik.
- Citra disegmentasi berdasarkan properti yang dipilih seperti kecerahan, warna, tekstur, dan sebagainya.
- Segmentasi membagi citra menjadi sejumlah region yang terhubung, tiap region bersifat homogen berdasarkan properti yang dipilih.
- Segmentasi citra merupakan tahapan sebelum melakukan *image/object recognition, image understanding*, dll.

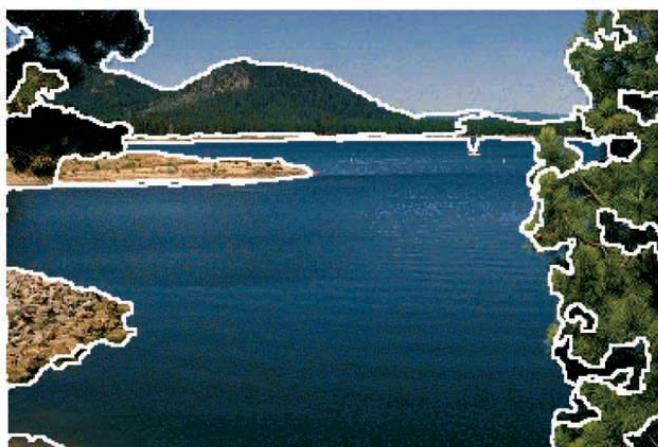


**1. Select an image:**  **2. Select a processor:**  **3. Click**

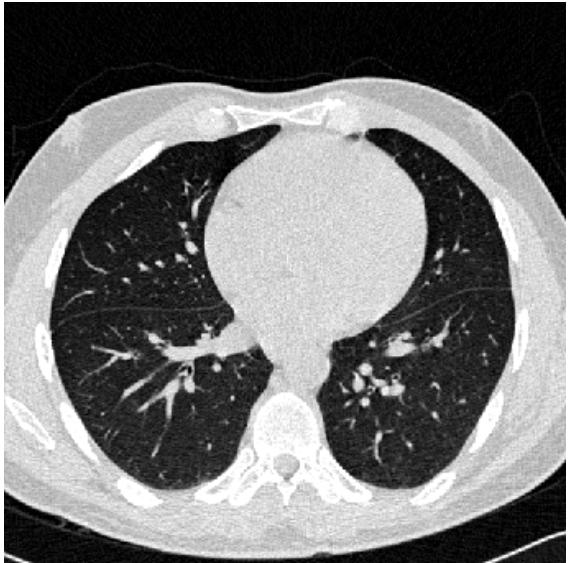
Options:  
Init Method



640\*480      (607,118): RGB(20,22,1)      Process done!      (228,26): RGB(255,170,0)



Sumber: CS 4487/9587 Algorithms for Image Analysis: Basic Image Segmentation



Citra medis



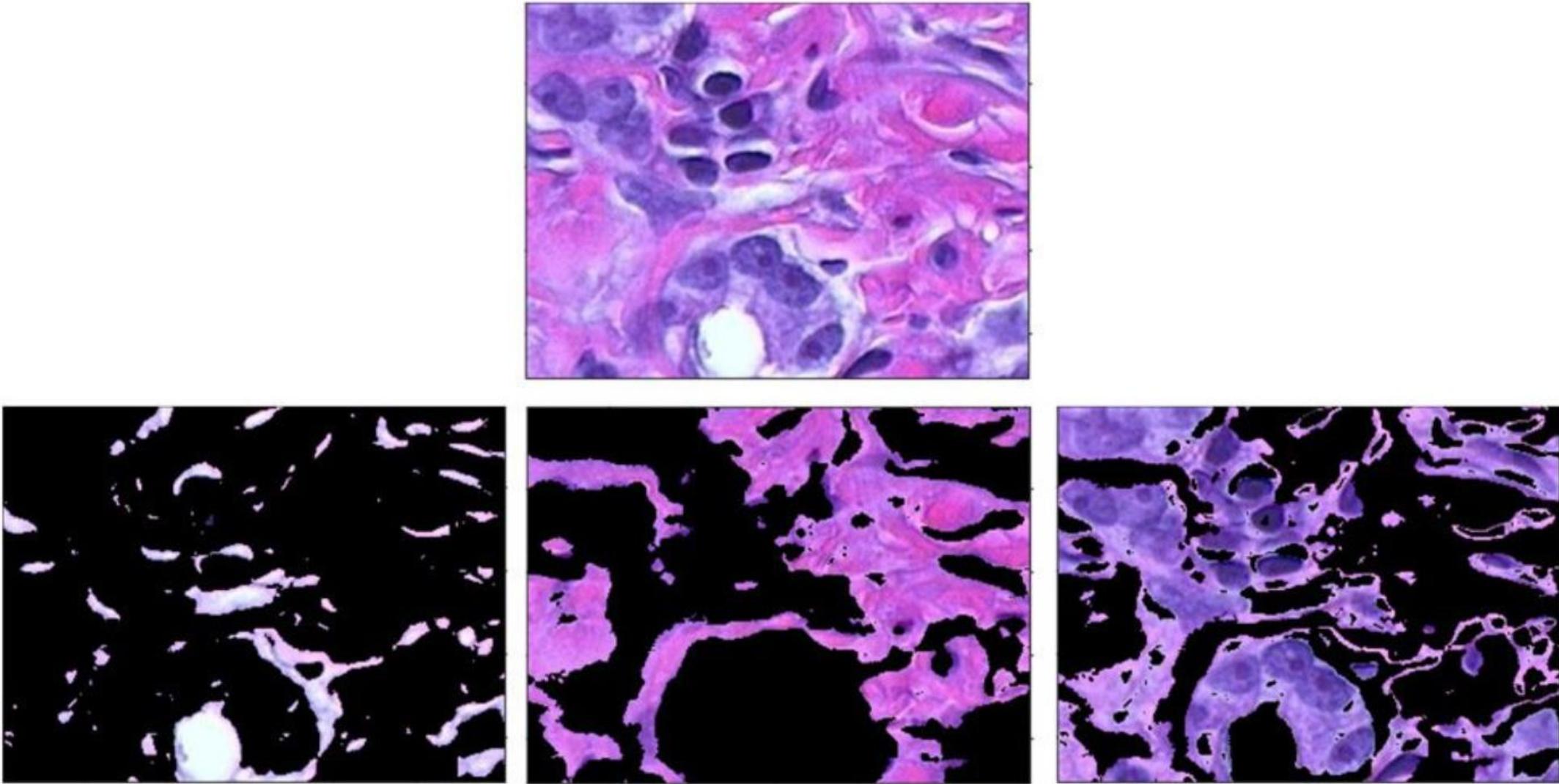
Hasil  
segmentasi

# Beberapa aplikasi segmentasi citra

## 1. Medical imaging

Selama diagnosis medis untuk kanker, ahli patologi menginjeksi jaringan tubuh dengan hematoxylin dan eosin (H&E) untuk membedakan jenis jaringan.

Mereka kemudian menggunakan teknik segmentasi gambar yang disebut clustering untuk mengidentifikasi jenis jaringan tersebut dalam gambar mereka.



Menggunakan clustering untuk membedakan jenis jaringan (bawah) pada citra jaringan tubuh (atas) yang diwarnai dengan hematoxylin dan eosin (H&E).

Sumber: <https://www.mathworks.com/discovery/image-segmentation.html>

## 2. Autonomous Vehicle

Saat merancang persepsi untuk kendaraan otonom, seperti mobil self-driving, segmentasi citra digunakan untuk membantu sistem mengidentifikasi dan menemukan kendaraan dan objek lain di jalan.



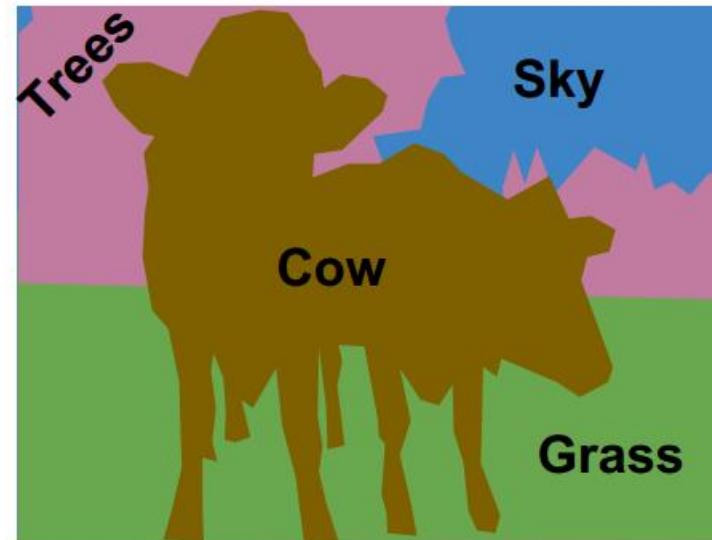
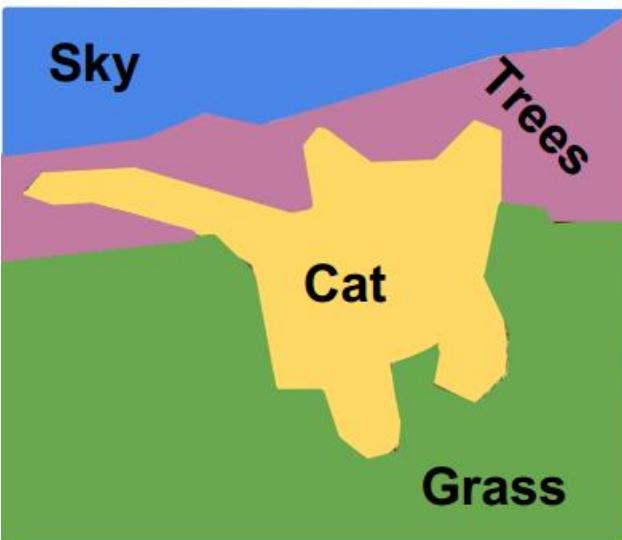
Menggunakan segmentasi citra untuk mengaitkan setiap piksel gambar dengan label kelas (seperti mobil, jalan, langit, pejalan kaki, atau sepeda).

Sumber: <https://www.mathworks.com/discovery/image-segmentation.html>

### 3. Object recognition



[This image is CC0 public domain](#)



### 3. Scene understanding

Mesin dapat memahami apa yang “dilihatnya”



# Kriteria Segmentasi

- Menurut Pavlidis:

Segmentasi adalah partisi citra  $I$  menjadi sejumlah region  $S_1, S_2, \dots S_m$  yang memenuhi persyaratan:

1.  $\cup S_i = S$  Partisi mencakup keseluruhan *pixel* di dalam citra.
2.  $S_i \cap S_j = \emptyset, i \neq j$  Tidak ada region yang beririsan.
3.  $\forall S_i, P(S_i) = \text{true}$   $P$  = Predikat homogenitas, dipenuhi oleh setiap region
4.  $P(S_i \cup S_j) = \text{false}, i \neq j, S_i$  adjacent  $S_j$  Gabungan region bertetangga tidak memenuhi predikat

- Jadi, yang harus dilakukan adalah mendefinisikan dan mengimplementasikan predikat *similarity*.
- Misalnya, *similarity* didasarkan pada pixel-pixel di dalam rentang nilai yang sama.

# Metode segmentasi citra

Metode segmentasi citra umumnya dikelompokkan berdasarkan dua pendekatan:

1. *Diskontinuitas*

Mempartisi citra berdasarkan perubahan nilai intensitas *pixel* yang cepat seperti tepi (*edge detection*)

2. *Similarity*

Mempartisi citra berdasarkan kemiripan area menurut properti yang ditentukan  
Metode segmentasi citra yang termasuk ke dalam pendekatan ini:

- a) Pengambangan (*thresholding*)
- b) *Region growing*
- c) *Split and merge*
- d) *Clustering*

- Pendekripsi tepi dapat digunakan untuk melakukan segmentasi citra.
- Metode-metode deteksi tepi sudah dibahas pada materi sebelumnya, seperti metode berbasis gradien (Sobel, Prewit, Canny, Roberts, Laplacian, LoG, dll)

a	b
c	d

**FIGURE 10.10**

(a) Original image. (b)  $|G_x|$ , component of the gradient in the  $x$ -direction.  
 (c)  $|G_y|$ , component in the  $y$ -direction.  
 (d) Gradient image,  $|G_x| + |G_y|$ .







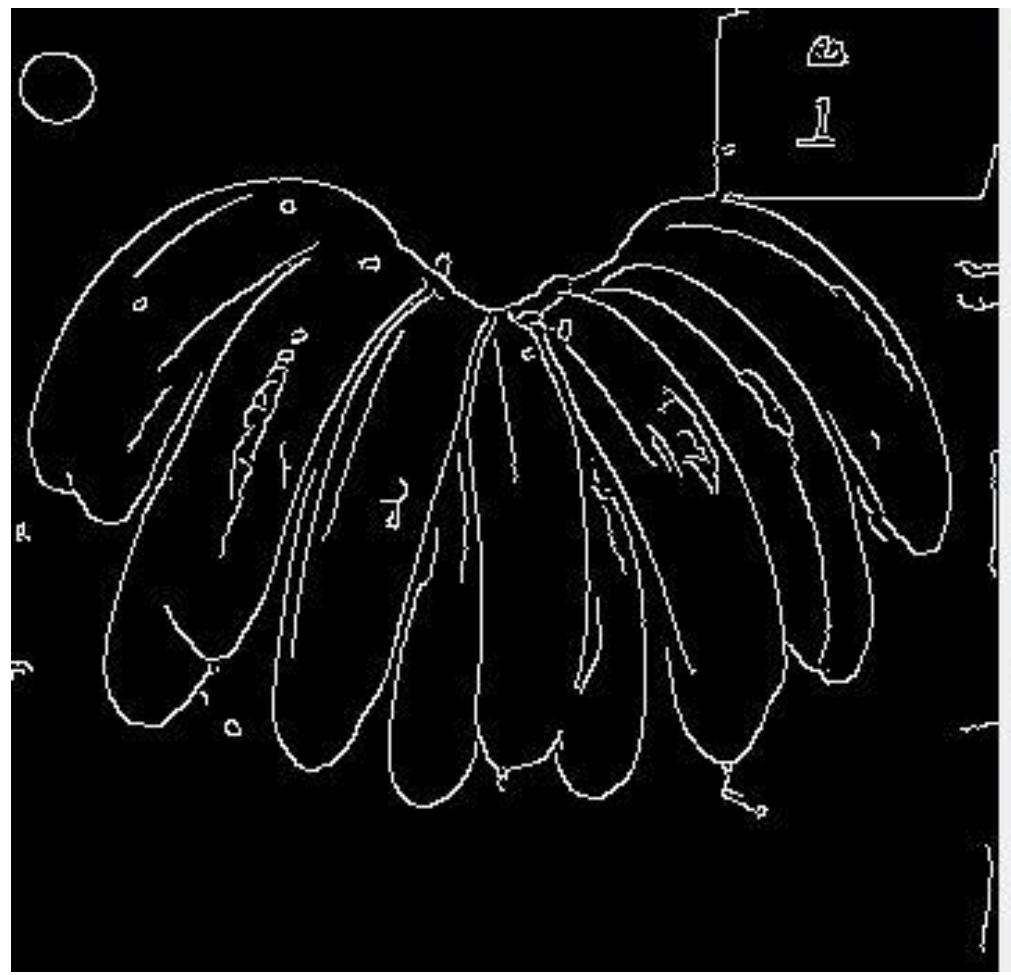
a) Complemented Image



b) Edged Image

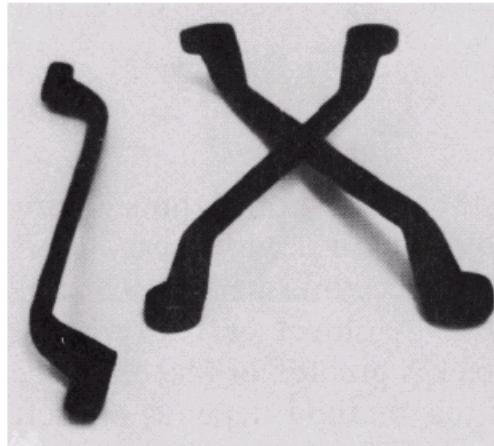
**Figure 3. Complemented Image and Edged Image**





# Segmentasi citra berdasarkan *similarity*

- Cara paling sederhana menemukan bagian citra yang koheren adalah berdasarkan nilai intensitas pixel atau warna



Perkakas menjadi bagian yang koheren

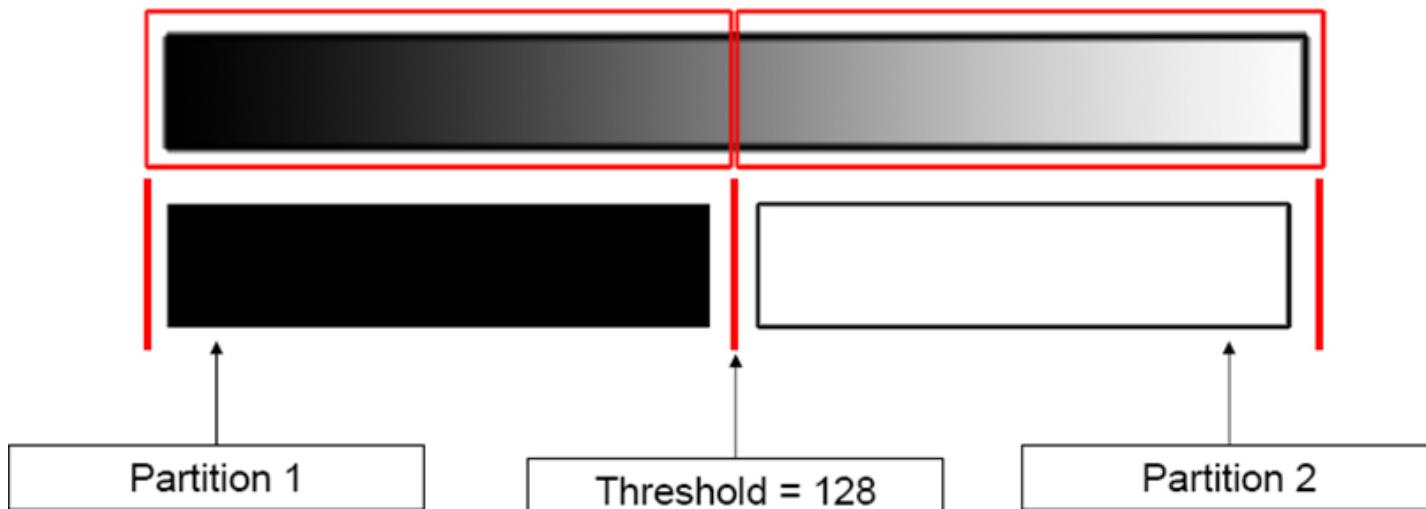


Rumah, rumput, dan langit membentuk bagian koheren yang berbeda

- Metode segmentasi berbasis *similarity*: pengambangan (*thresholding*), *region growing*, *split and merge*, dan *clustering*.

# 1. Pengambangan

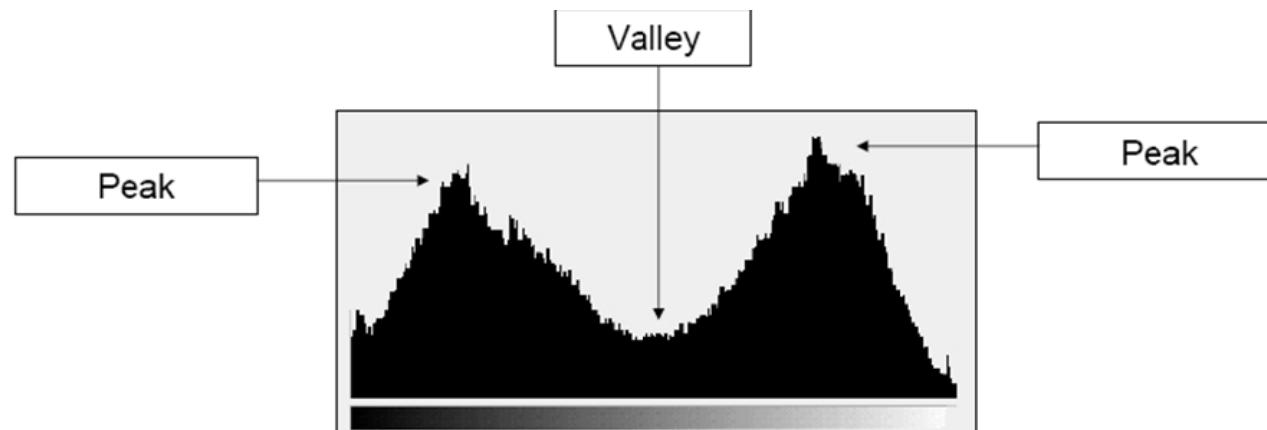
- Sudah dijelaskan pada materi sebelumnya (lihat materi Citra Biner)
- Segmentasi citra didasarkan pada nilai intensitas pixel-pixel dan nilai ambang  $T$ .
- Salah satu cara untuk mengekstrak objek dari latar belakang adalah dengan memilih ambang  $T$ .
- Setiap pixel  $(x, y)$  pada citra di mana  $f(x, y) > T$  disebut titik objek, jika tidak maka akan disebut latar belakang.
- Hasil segmentasi adalah berupa citra biner



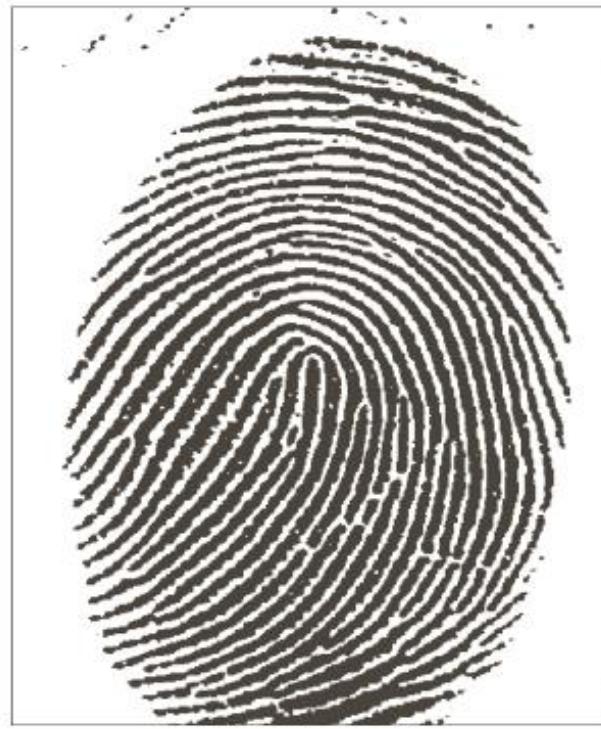
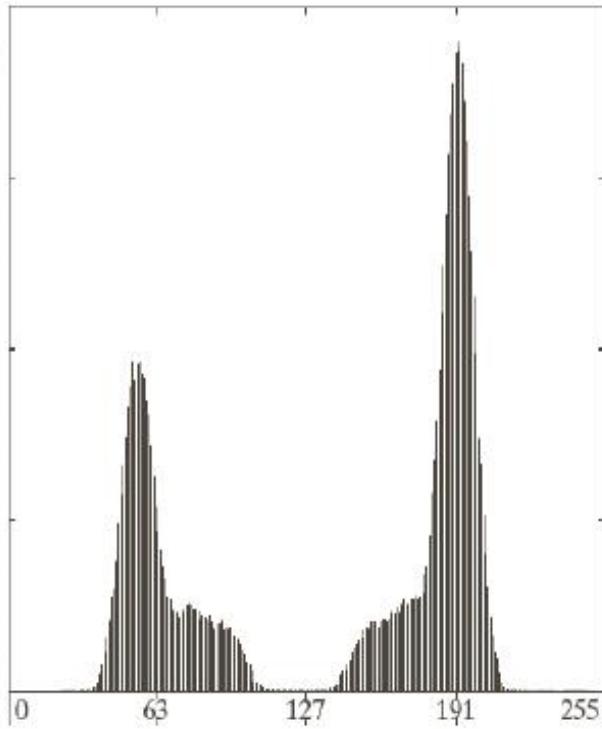
### Pilih nilai ambang T

1. Pixel-pixel di atas nilai ambang mendapatkan intensitas baru A.
2. Pixels di bawah nilai ambang mendapatkan intensitas baru B.

- Untuk mendapatkan nilai ambang  $T$ , analisis histogram citra lalu identifikasi puncak dan lembah.



- Nilai *grayscale* pada lembah terdalam di antara dua bukit menyatakan nilai  $T$ .



## What Is Image Filtering in the Spatial Domain?

Filtering is a technique for modifying or enhancing an image. For example, you can filter an image to emphasize certain features or remove other features. Image processing operations implemented with filtering include smoothing, sharpening, and edge enhancement.

Filtering is a *neighborhood operation*, in which the value of any given pixel in the output image is determined by applying some algorithm to the values of the pixels in the neighborhood of the corresponding input pixel. A pixel's neighborhood is a set of pixels, defined by their locations relative to that pixel. (See [Neighborhood](#) or [Block Processing: An Overview](#) for a general discussion of neighborhood operations.) *Linear filtering* is filtering in which the value of an output pixel is a linear combination of the values of all pixels in the input pixel's neighborhood.

### Convolution

Convolution of an image is accomplished through an operation called convolution. Convolution is a neighborhood operation in which each output pixel is the weighted sum of neighboring input pixels. The matrix of weights is called the *convolution kernel*, also known as the *filter*. A convolution kernel is a correlation kernel that has been rotated 180 degrees.

For example, suppose the image is

$$A = \begin{bmatrix} 17 & 24 & 1 & 8 & 15 \\ 23 & 5 & 7 & 14 & 16 \\ 4 & 6 & 13 & 20 & 22 \\ 10 & 12 & 19 & 21 & 3 \\ 11 & 18 & 25 & 2 & 19 \end{bmatrix}$$

## What Is Image Filtering in the Spatial Domain?

Filtering is a technique for modifying or enhancing an image. For example, you can filter an image to emphasize certain features or remove other features. Image processing operations implemented with filtering include smoothing, sharpening, and edge enhancement.

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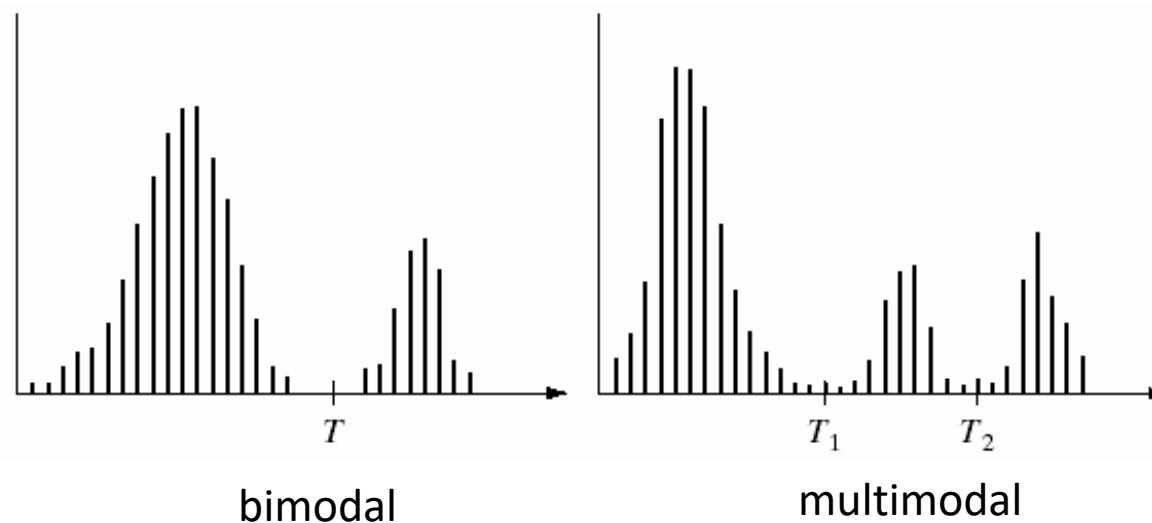
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$$A = \begin{bmatrix} 17 & 24 & 1 & 8 & 15 \\ 23 & 5 & 7 & 14 & 16 \\ 4 & 6 & 13 & 20 & 22 \\ 10 & 12 & 19 & 21 & 3 \\ 11 & 18 & 25 & 2 & 19 \end{bmatrix}$$

Menggunakan pengambangan untuk mengonversi ke gambar biner untuk meningkatkan keterbacaan teks dalam gambar.

Sumber: <https://www.mathworks.com/discovery/image-segmentation.html>

- Mencari nilai  $T$  dengan cara sederhana di atas hanya tepat jika histogram bersifat bimodal (mempunyai dua puncak dan satu lembah). Misalnya segmentasi teks dengan latar belakangnya.
- Jika terdapat multimodal di dalam citra, maka diperlukan beberapa nilai ambang.



- Teknik pengambangan dibagi menjadi:
  1. *Global thresholding*  
Nilai ambang bergantung pada keseluruhan nilai-nilai *pixel*
  2. *Local thresholding*  
Nilai ambang bergantung pada *pixel-pixel* bertetangga, hanya untuk sekelompok *pixel* saja.
  3. *Adaptive thresholding*  
Nilai ambang berubah secara dinamis bergantung pada perubahan pencahayaan di dalam citra

## Global thresholding

Sumber: Image segmentation  
Stefano Ferrari  
Universit`a degli Studi di Milano  
stefano.ferrari@unimi.it

A simple algorithm:

1. Initial estimate of  $T$
2. Segmentation using  $T$ :
  - ▶  $G_1$ , pixels brighter than  $T$ ;
  - ▶  $G_2$ , pixels darker than (or equal to)  $T$ .
3. Computation of the average intensities  $m_1$  and  $m_2$  of  $G_1$  and  $G_2$ .
4. New threshold value:

$$T_{\text{new}} = \frac{m_1 + m_2}{2}$$

5. If  $|T - T_{\text{new}}| > \Delta T$ , back to step 2, otherwise stop.

# Pengembangan dengan Metode Otsu

## Otsu's method

- ▶ Otsu's method is aimed in finding the optimal value for the global threshold.
- ▶ It is based on the interclass variance maximization.
  - ▶ Well thresholded classes have well discriminated intensity values.
- ▶  $M \times N$  image histogram:
  - ▶  $L$  intensity levels,  $[0, \dots, L - 1]$ ;
  - ▶  $n_i$  #pixels of intensity  $i$ :

$$MN = \sum_{i=0}^{L-1} n_i$$

- ▶ Normalized histogram:

$$p_i = \frac{n_i}{MN}$$

$$\sum_{i=0}^{L-1} p_i = 1, \quad p_i \geq 0$$

Sumber: *Image Segmentation*, by Stefano Ferrari

## Otsu's method (2)

- ▶ Using  $k$ ,  $0 < k < L - 1$ , as threshold,  $T = k$ :
  - ▶ two classes:  $C_1$  (pixels in  $[0, k]$ ) and  $C_2$  (pixels in  $[k + 1, L - 1]$ )
  - ▶  $P_1 = P(C_1) = \sum_{i=0}^k p_i$ , probability of the class  $C_1$ 
    - ▶  $P_2 = P(C_2) = \sum_{i=k+1}^{L-1} p_i = 1 - P_1$ , probability of the class  $C_2$
  - ▶  $m_1$ , mean intensity of the pixels in  $C_1$ :

$$\begin{aligned}m_1 &= \sum_{i=0}^k i \cdot P(i|C_1) \\&= \sum_{i=0}^k i \frac{P(C_1|i)P(i)}{P(C_1)} \\&= \frac{1}{P_1} \sum_{i=0}^k i \cdot p_i\end{aligned}$$

where  $P(C_1|i) = 1$ ,  $P(i) = p_i$  e  $P(C_1) = P_1$ .

## Otsu's method (3)

- ▶ Similarly,  $m_2$ , mean intensity of the pixels in  $C_2$ :

$$m_2 = \frac{1}{P_2} \sum_{i=k+1}^{L-1} i \cdot p_i$$

- ▶ Mean global intensity,  $m_G$ :

$$m_G = \sum_{i=0}^{L-1} i \cdot p_i$$

- ▶ while the mean intensity up to the  $k$  level,  $m$ :

$$m = \sum_{i=0}^k i \cdot p_i$$

- ▶ Hence:

$$P_1 m_1 + P_2 m_2 = m_G$$

$$P_1 + P_2 = 1$$

## Otsu's method (4)

- ▶ The global variance  $\sigma_G^2$ :

$$\sigma_G^2 = \sum_{i=0}^{L-1} (i - m_G)^2 \cdot p_i$$

- ▶ The *between-class variance*,  $\sigma_B$ , can be defined as:

$$\begin{aligned}\sigma_B^2 &= P_1(m_1 - m_G)^2 + P_2(m_2 - m_G)^2 \\ &= P_1 P_2 (m_1 - m_2)^2 \\ &= \frac{(m_G P_1 - m)^2}{P_1(1 - P_1)}\end{aligned}$$

- ▶ The *goodness* of the choice  $T = k$  can be estimated as the ratio  $\eta$ :

$$\eta = \frac{\sigma_B^2}{\sigma_G^2}$$

## Otsu's method (5)

- ▶ The quantities required for the computation of  $\eta$ , can be obtained from the histogram:
- ▶ Hence, for each value of  $k$ ,  $\eta(k)$  can be computed:

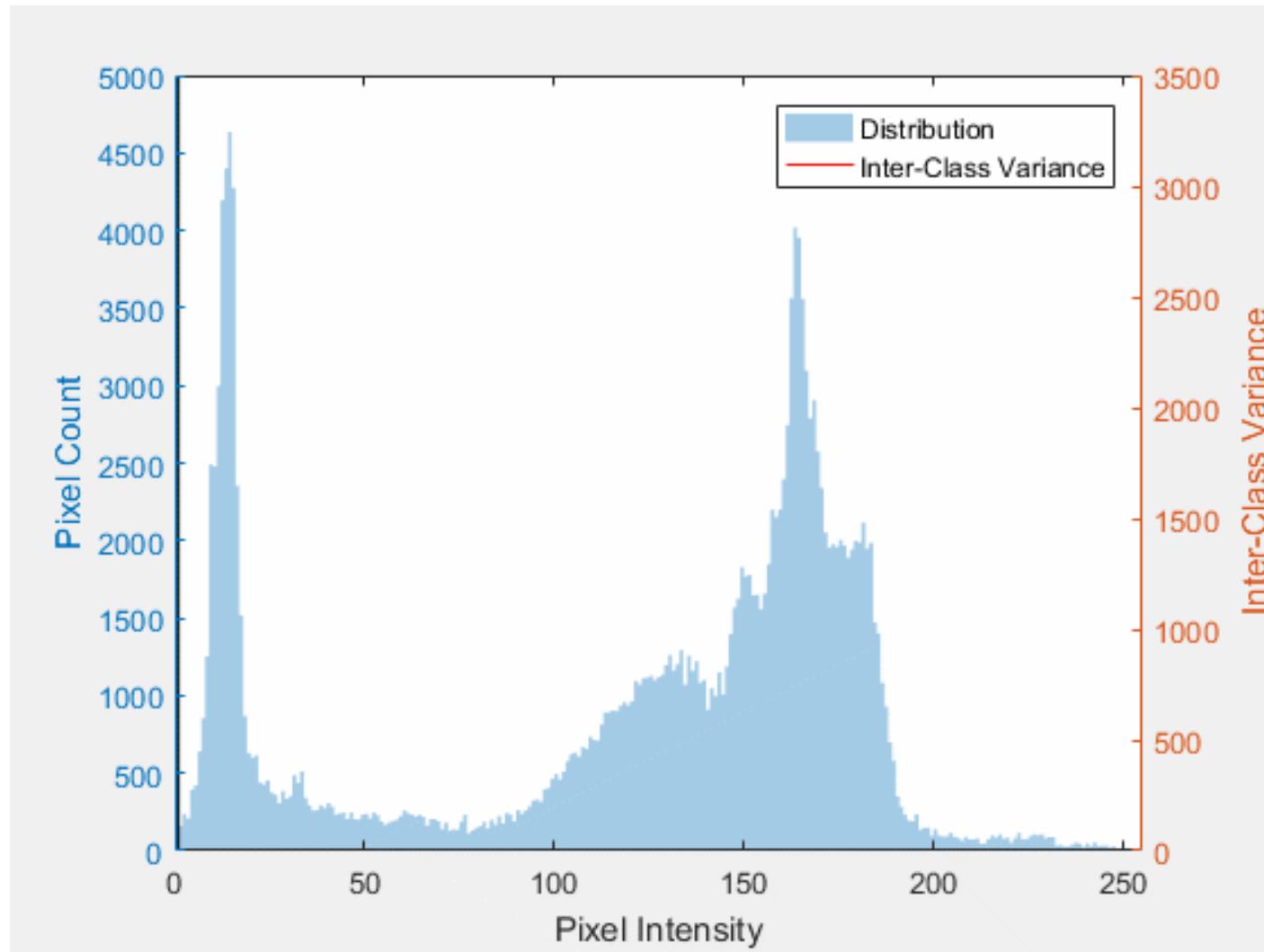
$$\eta(k) = \frac{\sigma_B^2(k)}{\sigma_G^2}$$

where

$$\sigma_B^2(k) = \frac{(m_G P_1(k) - m(k))^2}{P_1(k)(1 - P_1(k))}$$

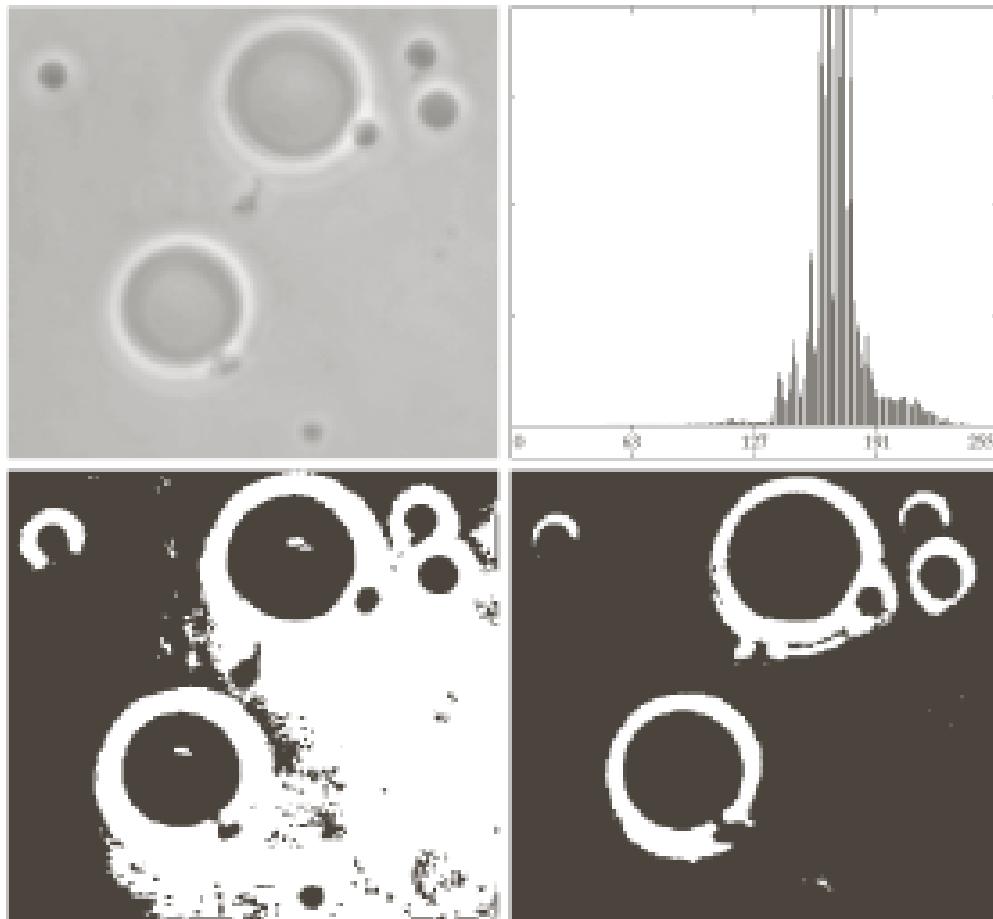
- ▶ The optimal threshold value,  $k^*$ , satisfies:

$$\sigma_B^2(k^*) = \max_{0 < k < L-1} \sigma_B^2(k)$$



Visualisasi metode Otsu (Sumber: Wikipedia)

## Otsu's method: an example



a	b
c	d

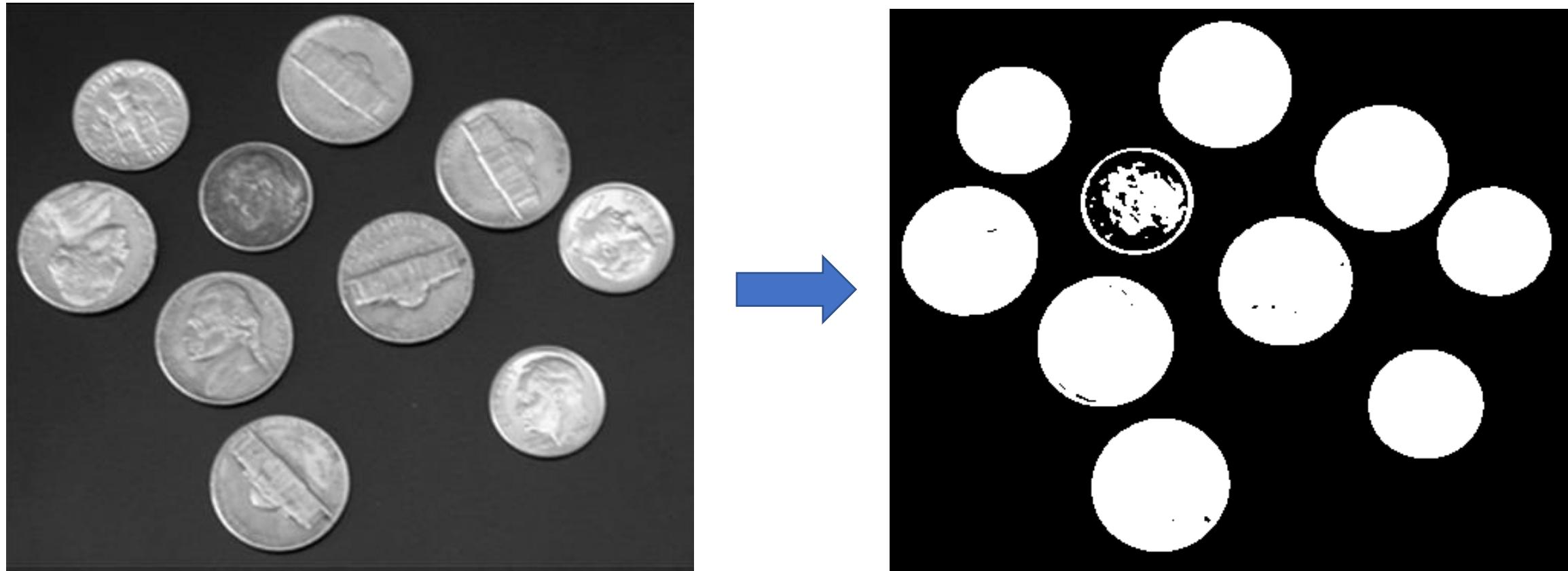
- (a) original image;
- (b) histogram of (a);
- (c) global threshold:  
 $T = 169,$   
 $\eta = 0.467;$
- (d) Otsu's method:  
 $T = 181,$   
 $\eta = 0.944.$

- Matlab memiliki fungsi graythresh () untuk melakukan pengambangan dengan metode Otsu.

```
I = imread('house.jpg');  
T = graythresh(I);  
BW = im2bw(I, T);  
imshow(I);  
figure; imshow(BW)
```

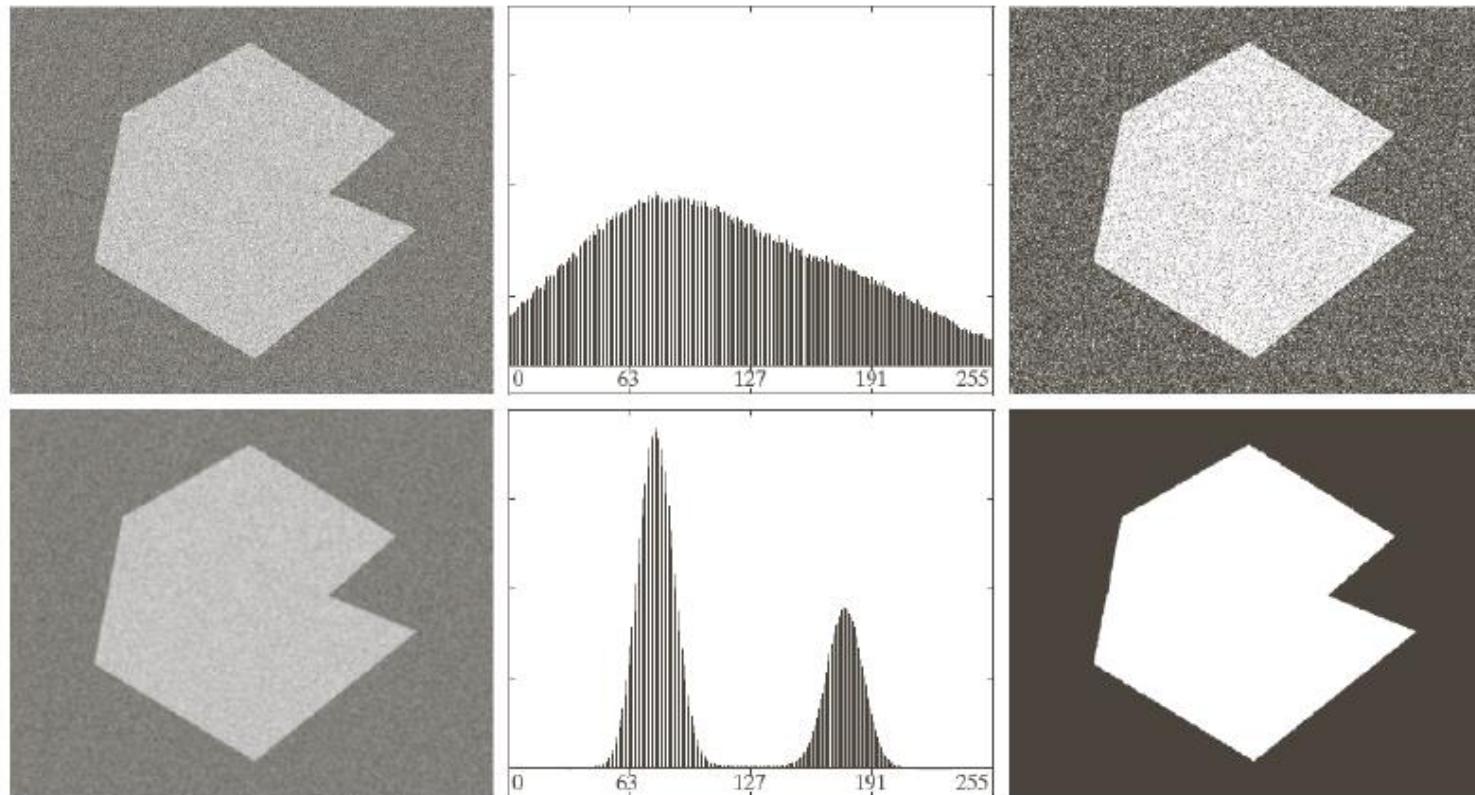


```
I = imread('coins.bmp');  
T = graythresh(I);  
BW = im2bw(I, T);  
imshow(I);  
figure; imshow(BW)
```



Hasil pengambangan dengan metode Otsu

## Smoothing



- ▶ Otsu's method may not work in presence of noise.
- ▶ Smoothing can produce a histogram with separated peaks.

## Multiple thresholds Otsu's method

- ▶ The Otsu's method can be applied also for the multiple thresholds segmentation (generally, double threshold).
- ▶ Between-class variance:

$$\sigma_B^2(k_1, k_2) = P_1(m_1 - m_G)^2 + P_2(m_2 - m_G)^2 + P_3(m_3 - m_G)^2$$

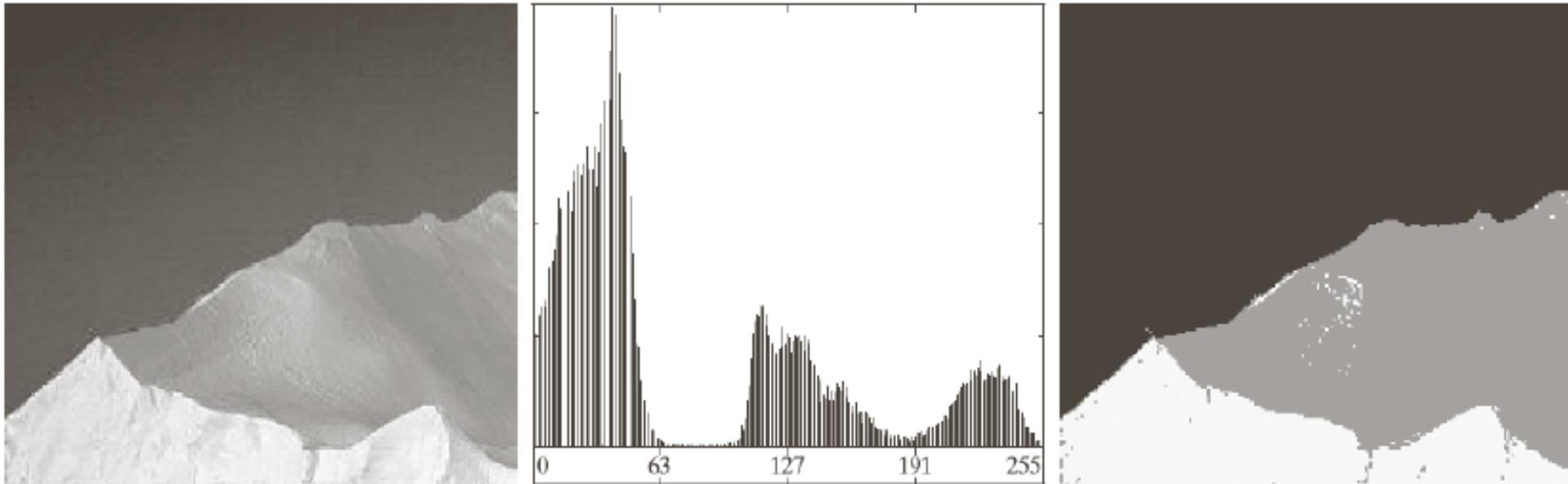
- ▶ The optimal thresholds  $k_1^*$  and  $k_2^*$  can be computed as:

$$\sigma_B^2(k_1^*, k_2^*) = \max_{0 < k_1 < k_2 < L-1} \sigma_B^2(k_1, k_2)$$

- ▶ The separability degree can be measured as:

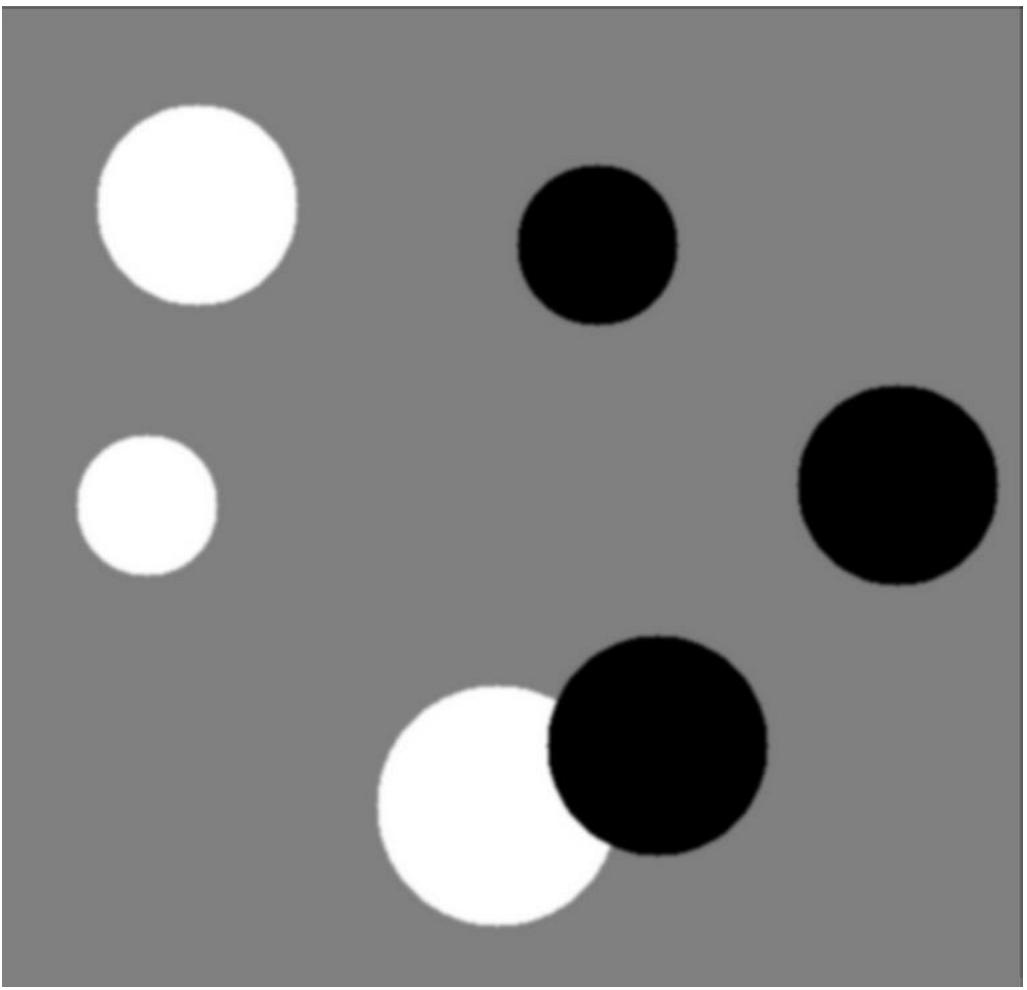
$$\eta(k_1^*, k_2^*) = \frac{\sigma_B^2(k_1^*, k_2^*)}{\sigma_G^2}$$

## Multiple thresholds Otsu's method: an example

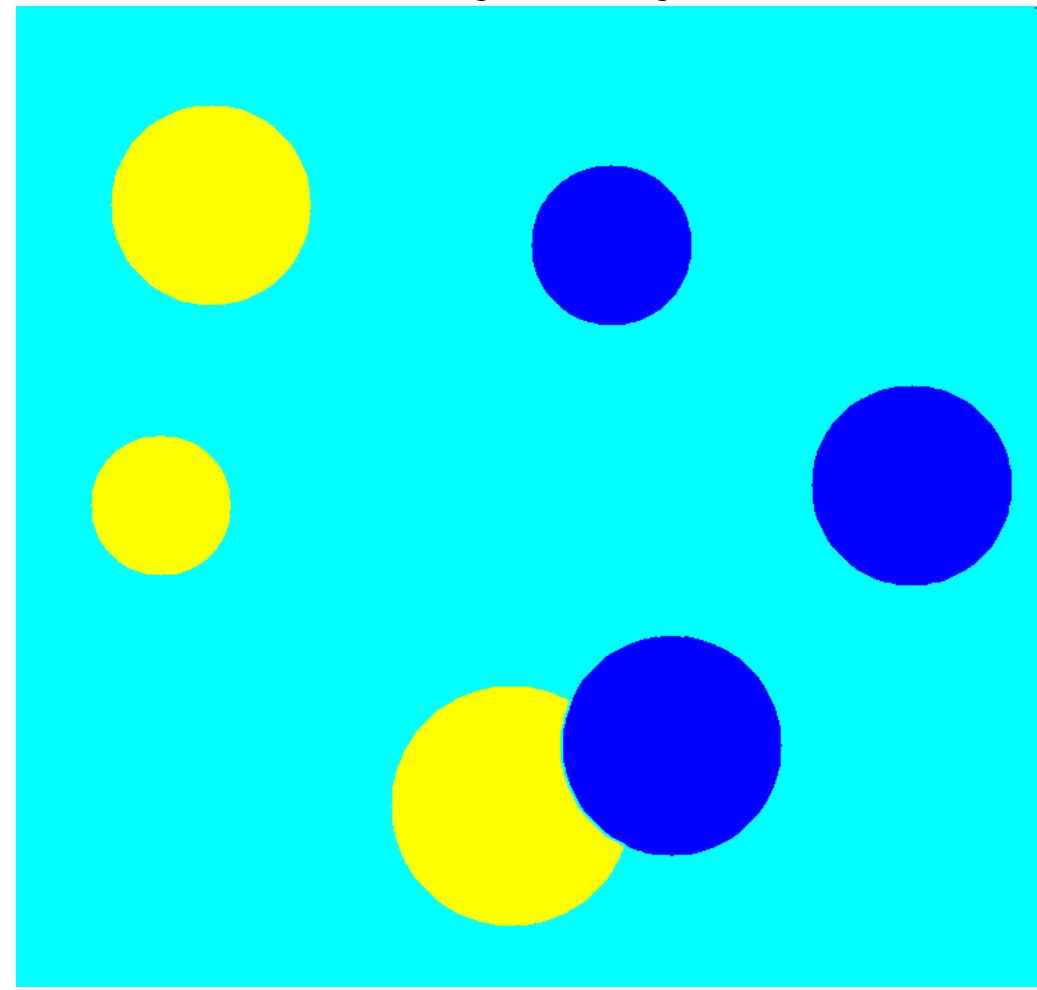


- Di dalam Matlab, fungsi multithresh () digunakan untuk melakukan *multiple threshold* dengan metode Otsu.

```
% Baca citra  
I = imread('circle.jpg');  
  
% Tampilkan citra  
imshow(I);  
  
% Hitung dua buah nilai ambang  
thresh = multithresh(I, 2);  
  
% Segmentasi citra menjadi tiga level dengan fungsi imquantize  
seg_I = imquantize(I, thresh);  
  
% Konversi citra yang disegmentasi menjadi citra berwarna dengan  
% menggunakan fungsi label2rgb dan tampilkan  
RGB = label2rgb(seg_I);  
figure; imshow(RGB)  
axis off  
title('RGB Segmented Image')
```

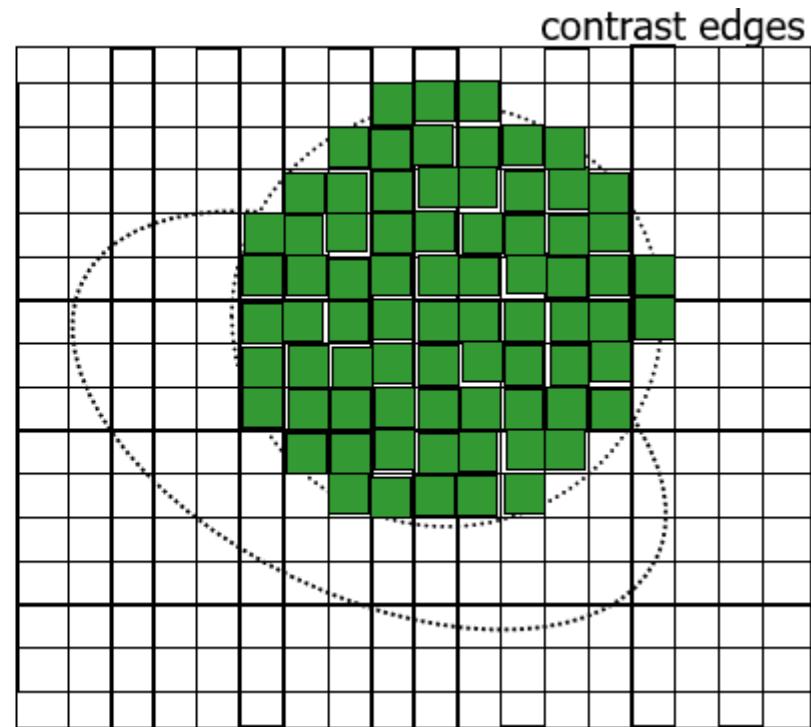


RGB Segmented Image



## 2. Region Growing

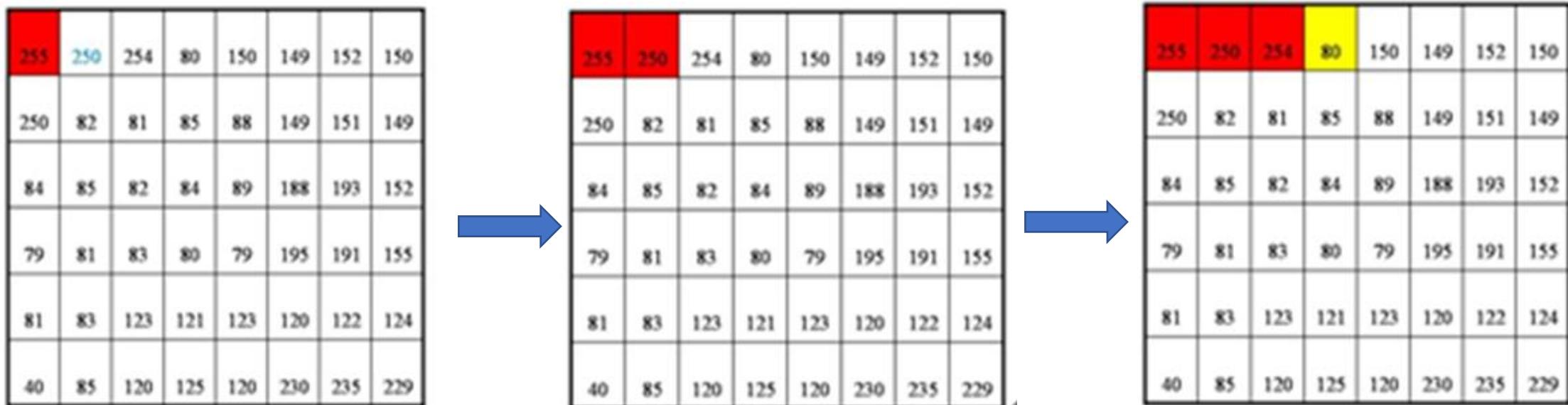
- *Region growing*: kelompok *pixel* atau sub-region yang tumbuh menjadi region yang lebih besar.
- Algoritma: Mulai dengan “umpan (*seed*)” yang berisi himpunan beranggota satu atau lebih *pixel* dari region yang potensial, dan dari sini *region* berkembang dengan menambahkan pada umpan *pixel-pixel* tetangga yang memiliki properti yang mirip dengan umpan, lalu berhenti jika *pixel-pixel* tetangga tidak mirip lagi.
- Biasanya uji statistik digunakan untuk memutuskan apakah sebuah *pixel* dapat digabungkan ke dalam region atau tidak.
- Keuntungan: memiliki keterhubungan yang bagus antar pixel di dalam region
- Kelemahan:
  - pemilihan umpan yang tepat
  - kriteria berhenti
  - mengkonsumsi waktu yang lama



Sumber: CS 4487/9587 Algorithms for Image Analysis: Basic Image Segmentation

# Unseeded Region Growing

- Metode *region growing* tanpa spesifikasi umpan
- Menggunakan algoritma *fast scanning*



255	250	254	80	150	149	152	150
250	82	81	85	88	149	151	149
84	85	82	84	89	188	193	152
79	81	83	80	79	195	191	155
81	83	123	121	123	120	122	124
40	85	120	125	120	230	235	229



255	250	254	80	150	149	152	150
250	82	81	85	88	149	151	149
84	85	82	84	89	188	193	152
79	81	83	80	79	195	191	155
81	83	123	121	123	120	122	124
40	85	120	125	120	230	235	229



255	250	254	80	150	149	152	150
250	82	81	85	88	188	193	152
84	85	82	84	89	188	193	152
79	81	83	80	79	195	191	155
81	83	123	121	123	120	122	124
40	85	120	125	120	230	235	229

Langkah terakhir:

Gabungkan (*merge*) region kecil menjadi region besar

255	250	254	80	150	149	152	150
250	82	81	85	88	188	193	152
84	85	82	84	89	188	193	152
79	81	83	80	79	81	191	155
81	83	123	121	123	120	122	124
40	85	120	125	250	230	235	229



255	250	254	80	150	149	152	150
250	82	81	85	88	188	193	152
84	85	82	84	89	188	193	152
79	81	83	80	79	81	191	155
81	83	123	121	123	120	122	124
40	85	120	125	250	230	235	229

# Seeded Region Growing

(segmentasi.m)

```
% read image
reg_maxdist = 0.2;
I = im2double(imread('lada-gray.bmp')) ;
subplot(121);
imshow(I);
% let the user pick one point
[x,y] = ginput(1);
% round to integer to match required input by regiongrowing function
x = round(x);
y = round(y);
% plot point on original image
hold on;
plot(x,y,'xg','MarkerSize',20,'LineWidth',2);
hold off;
% get region from seed point
J = regiongrowing(I,y,x,reg_maxdist);
% plot region
subplot(122);
imshow(J);
```

Sumber: <https://stackoverflow.com/questions/44234856/region-growing-in-matlab>

```
function J=regiongrowing(I,x,y,reg_maxdist)
% This function performs "region growing" in an image from a specified
% seedpoint (x,y)
%
% J = regiongrowing(I,x,y,t)
% % I : input image
% J : logical output image of region
% x,y : the position of the seedpoint (if not given uses function getpts)
% t : maximum intensity distance (defaults to 0.2)
%
% The region is iteratively grown by comparing all unallocated neighbouring pixels to
% the region.
% The difference between a pixel's intensity value and the region's mean,
% is used as a measure of similarity. The pixel with the smallest difference
% measured this way is allocated to the respective region.
% This process stops when the intensity difference between region mean and
% new pixel become larger than a certain threshold (t)
%
% Example:
%
% I = im2double(imread('medtest.png'));
% x=198; y=359;
% J = regiongrowing(I,x,y,0.2);
% figure, imshow(I+J);
%
% Author: D. Kroon, University of Twente
```

```

if(exist('reg_maxdist','var')==0), reg_maxdist=0.2; end
if(exist('y','var')==0), figure, imshow(I,[]); [y,x]=getpts;
y=round(y(1)); x=round(x(1)); end
J = zeros(size(I)); % Output
Isizes = size(I); % Dimensions of input image
reg_mean = I(x,y); % The mean of the segmented region
reg_size = 1; % Number of pixels in region
% Free memory to store neighbours of the (segmented) region
neg_free = 10000; neg_pos=0;
neg_list = zeros(neg_free,3);
pixdist=0; % Distance of the region newest pixel to the regio mean
% Neighbor locations (footprint)
neighb=[-1 0; 1 0; 0 -1;0 1];
% Start regiogrowing until distance between regio and possible new
pixels become
% higher than a certain treshold

```

```

while(pixdist<reg_maxdist&&reg_size<numel(I))
    % Add new neighbors pixels
    for j=1:4,
        % Calculate the neighbour coordinate
        xn = x +neigb(j,1); yn = y +neigb(j,2);

        % Check if neighbour is inside or outside the image
        ins=(xn>=1) && (yn>=1) && (xn<=Isizes(1)) && (yn<=Isizes(2));

        % Add neighbor if inside and not already part of the segmented area
        if(ins&&(J(xn,yn)==0))
            neg_pos = neg_pos+1;
            neg_list(neg_pos,:)= [xn yn I(xn,yn)]; J(xn,yn)=1;
        end
    end
    % Add a new block of free memory
    if(neg_pos+10>neg_free), neg_free=neg_free+10000;
    neg_list((neg_pos+1):neg_free,:)=0; end

```

```

% Add pixel with intensity nearest to the mean of the region, to the region
dist = abs(neg_list(1:neg_pos,3)-reg_mean);
[pixdist, index] = min(dist);
J(x,y)=2; reg_size=reg_size+1;

% Calculate the new mean of the region
reg_mean= (reg_mean*reg_size + neg_list(index,3))/(reg_size+1);

% Save the x and y coordinates of the pixel (for the neighbour add
process)
x = neg_list(index,1); y = neg_list(index,2);

% Remove the pixel from the neighbour (check) list
neg_list(index,:)=neg_list(neg_pos,:); neg_pos=neg_pos-1;
end
% Return the segmented area as logical matrix
J=J>1;

```

Sumber: <https://www.mathworks.com/matlabcentral/fileexchange/19084-region-growing>



Figure 1

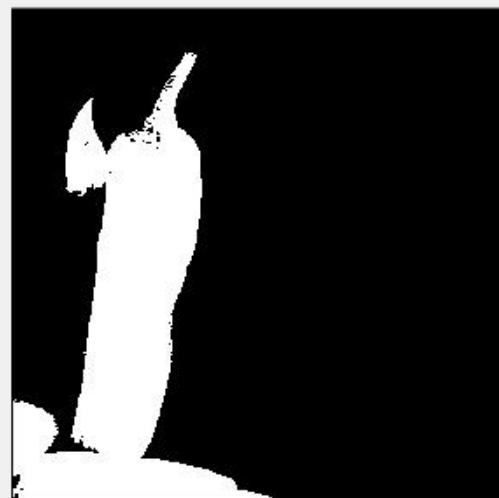
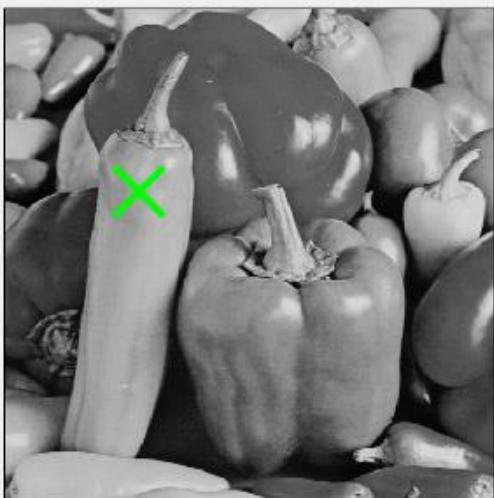


File Edit View Insert Tools Desktop Window Help



Figure 1

File Edit View Insert Tools Desktop Window Help

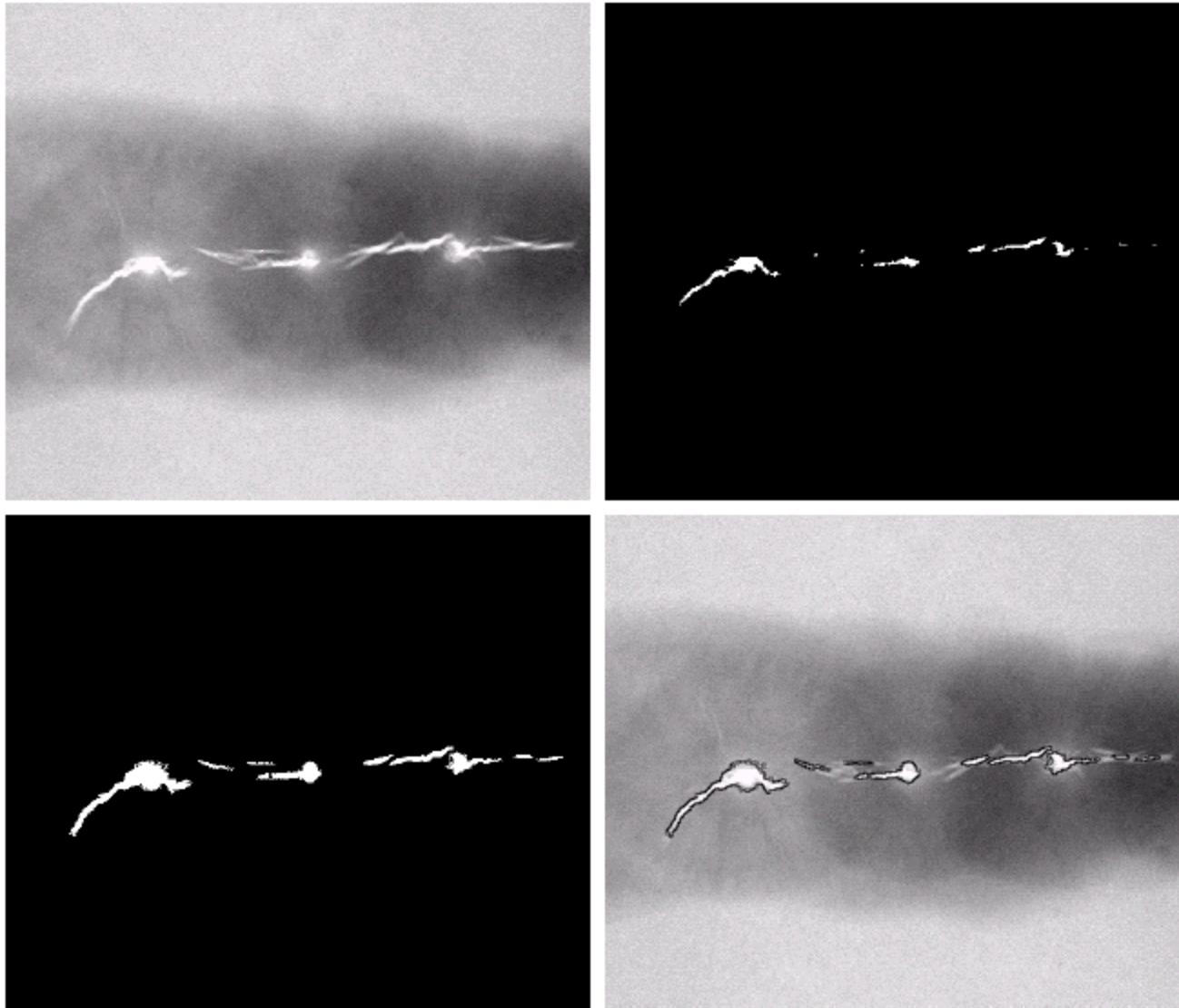


a b  
c d

**FIGURE 10.40**

(a) Image showing defective welds. (b) Seed points. (c) Result of region growing. (d) Boundaries of segmented defective welds (in black). (Original image courtesy of X-TEK Systems, Ltd.).

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