

19 - Pendeksiian Tepi (Bagian 2)

IF4073 Interpretasi dan Pengolahan Citra

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Operator gradien lainnya

- Oparator Sobel
- Operator Roberts
- Operator Prewitt
- Opreator Canny

Operator Sobel

- Tinjau pengaturan *pixel* di sekitar *pixel* (x,y) :

$$\begin{bmatrix} a_0 & a_1 & a_2 \\ a_7 & (x, y) & a_3 \\ a_6 & a_5 & a_4 \end{bmatrix}$$

- Operator Sobel adalah magnitudo dari gradien yang dihitung dengan rumus

$$M = \sqrt{s_x^2 + s_y^2}$$

yang dalam hal ini, turunan parsial dihitung dengan

$$s_x = (a_2 + ca_3 + a_4) - (a_0 + ca_7 + a_6)$$

$$s_y = (a_0 + ca_1 + a_2) - (a_6 + ca_5 + a_4)$$

- Dengan konstanta $c = 2$, maka

$$s_x = (a_2 + 2a_3 + a_4) - (a_0 + 2a_7 + a_6)$$

$$s_y = (a_0 + 2a_1 + a_2) - (a_6 + 2a_5 + a_4)$$

$$\begin{bmatrix} a_0 & a_1 & a_2 \\ a_7 & (x, y) & a_3 \\ a_6 & a_5 & a_4 \end{bmatrix}$$

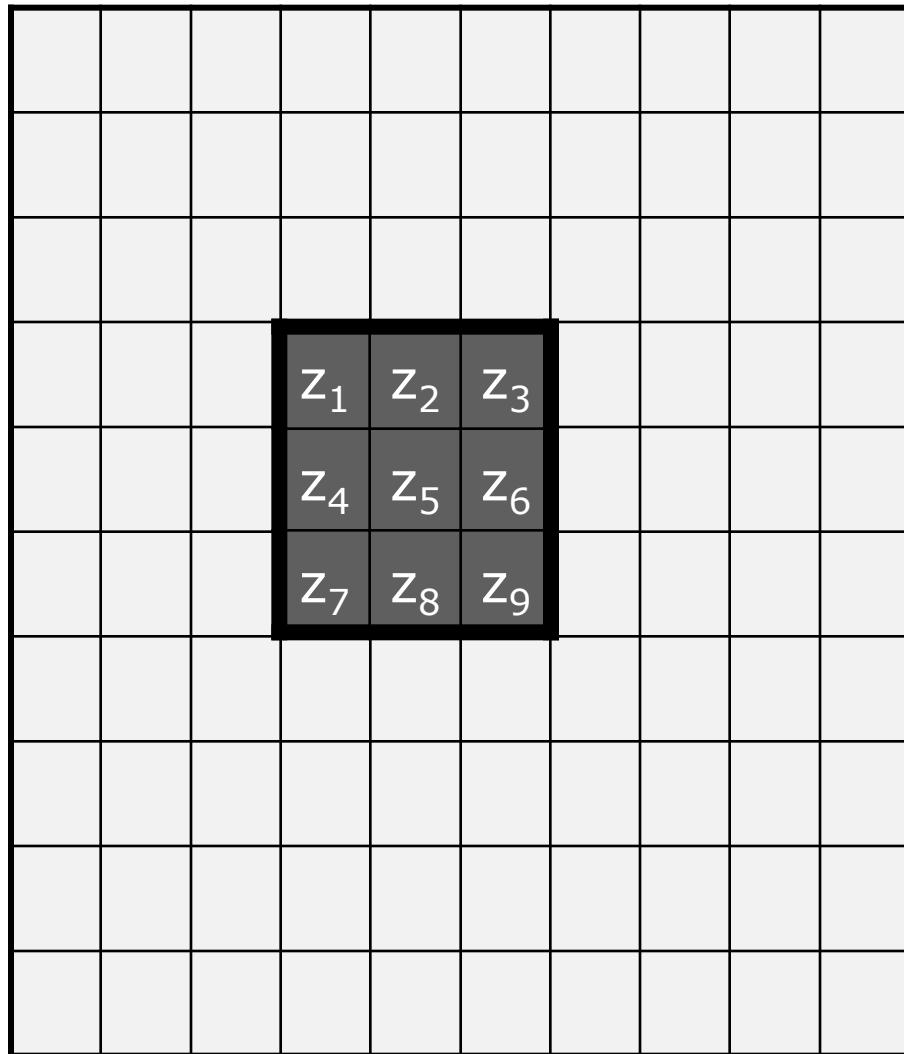
- Dalam bentuk *mask*, s_x dan s_y dapat dinyatakan sebagai

$$S_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix} \quad \text{dan} \quad S_y = \begin{bmatrix} 1 & 2 & 1 \\ 0 & 0 & 0 \\ -1 & -2 & -1 \end{bmatrix}$$

- Arah tepi dihitung dengan persamaan

$$\alpha(x,y) = \tan^{-1} \left(\frac{S_y}{S_x} \right)$$

Catatan: Beberapa literatur menggunakan penomoran pixel sebagai berikut sehingga matriks *mask* Sobel berbeda susunan nilainya dengan slide sebelumnya:



-1	-2	-1
0	0	0
1	2	1

$$G_x \approx (z_7 + 2z_8 + z_9) - (z_1 + 2z_2 + z_3)$$

-1	0	1
-2	0	2
-1	0	1

$$G_y \approx (z_3 + 2z_6 + z_9) - (z_1 + 2z_4 + z_7)$$

- Contoh:

$$\begin{bmatrix} 3 & 4 & 2 & 5 & 1 \\ 2 & 1 & 6 & 4 & 2 \\ 3 & 5 & 7 & 1 & 3 \\ 4 & 2 & 5 & 7 & 1 \\ 2 & 5 & 1 & 3 & 2 \end{bmatrix}$$

(i) citra semula

$$\begin{bmatrix} * & * & * & * & * \\ * & 18 \end{bmatrix}$$

(ii) hasil konvolusi

Nilai 18 pada citra hasil konvolusi diperoleh dengan perhitungan berikut:

$$S_x = (3)(-1) + (2)(-2) + (3)(-1) + (2)(1) + (6)(2) + (7)(1) = 11$$

$$S_y = (3)(1) + (4)(2) + (2)(1) + (3)(-1) + (5)(-2) + (7)(-1) = -7$$

$$M = \sqrt{s_x^2 + s_y^2} = \sqrt{11^2 + (-7)^2} \cong |S_x| + |S_y| = |11| + |-7| = 18$$

Pada contoh ini, nilai $M = \sqrt{s_x^2 + s_y^2}$ dihampiri dengan menghitung

$$M \cong |S_x| + |S_y|.$$

■

- Di bawah ini contoh lain pendeksiian tepi dengan operator Sobel, dimana hasil konvolusi diambil (thresholding) dengan $T = 12$.

Citra:

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 2 & 0 & 3 & 3 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 2 & 4 & 3 \\ 0 & 0 & 2 & 0 & 2 & 4 & 3 & 3 & 2 & 3 \\ 0 & 0 & 1 & 3 & 3 & 4 & 3 & 3 & 3 & 3 \\ 0 & 1 & 0 & 4 & 3 & 3 & 2 & 4 & 3 & 2 \\ 0 & 0 & 1 & 2 & 3 & 3 & 4 & 4 & 4 & 3 \end{bmatrix}$$

$|gradien - x| + |gradien - y| :$

Hasil pengambangan dengan $T = 12$:

```
%Sobel  
I = imread('bird.bmp');  
Sx = [-1 0 1; -2 0 2; -1 0 1];  
Sy = [1 2 1; 0 0 0; -1 -2 -1];  
Jx = conv2(double(I), double(Sx), 'same');  
Jy = conv2(double(I), double(Sy), 'same');  
Jedge = sqrt(Jx.^2 + Jy.^2);  
imshow(I);  
figure, imshow(uint8(Jedge));
```



Citra masukan



Hasil operator Sobel

Operator Prewitt

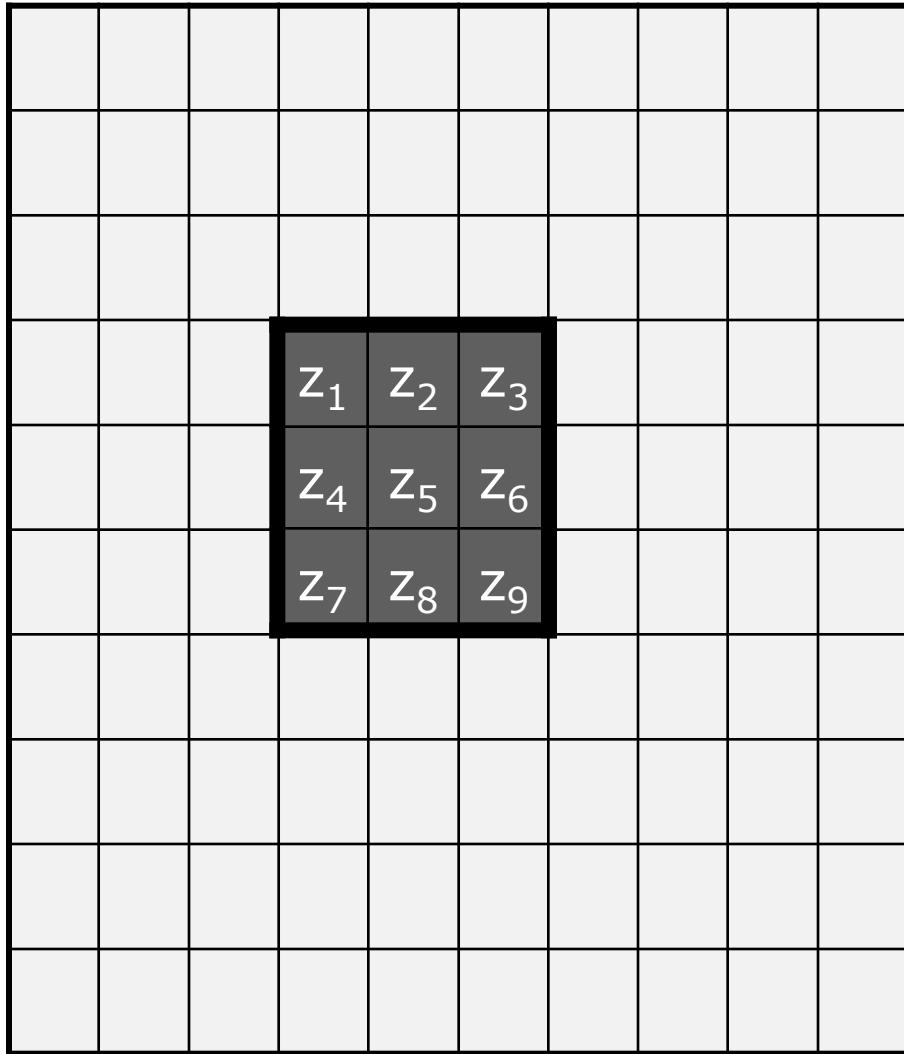
- Persamaan gradien pada operator Prewitt sama seperti operator Sobel, tetapi menggunakan nilai $c = 1$:

$$P_x = \begin{bmatrix} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{bmatrix} \quad \text{dan} \quad P_y = \begin{bmatrix} 1 & 1 & 1 \\ 0 & 0 & 0 \\ -1 & -1 & -1 \end{bmatrix}$$

- Kekuatan tepi dan arah tepi dihitung dengan rumus:

$$G(f(x,y)) = \sqrt{P_x^2 + P_y^2} \quad \alpha(x,y) = \tan^{-1} \left(\frac{P_y}{P_x} \right)$$

Catatan: Beberapa literatur menggunakan penomoran pixel sebagai berikut sehingga matriks *mask* Prewitt berbeda susunan nilainya dengan slide sebelumnya:



-1	-1	-1
0	0	0
1	1	1

$$G_x \approx (z_7 + z_8 + z_9) - (z_1 + z_2 + z_3)$$

-1	0	1
-1	0	1
-1	0	1

$$G_y \approx (z_3 + z_6 + z_9) - (z_1 + z_4 + z_7)$$

```
I = imread('bird.bmp');  
Px = [-1 0 1; -1 0 1; -1 0 1];  
Py = [-1 -1 -1; 0 0 0; 1 1 1];  
Jx = conv2(double(I), double(Px), 'same');  
Jy = conv2(double(I), double(Py), 'same');  
Jedge = sqrt(Jx.^2 + Jy.^2);  
imshow(I);  
figure, imshow(uint8(Jedge));
```



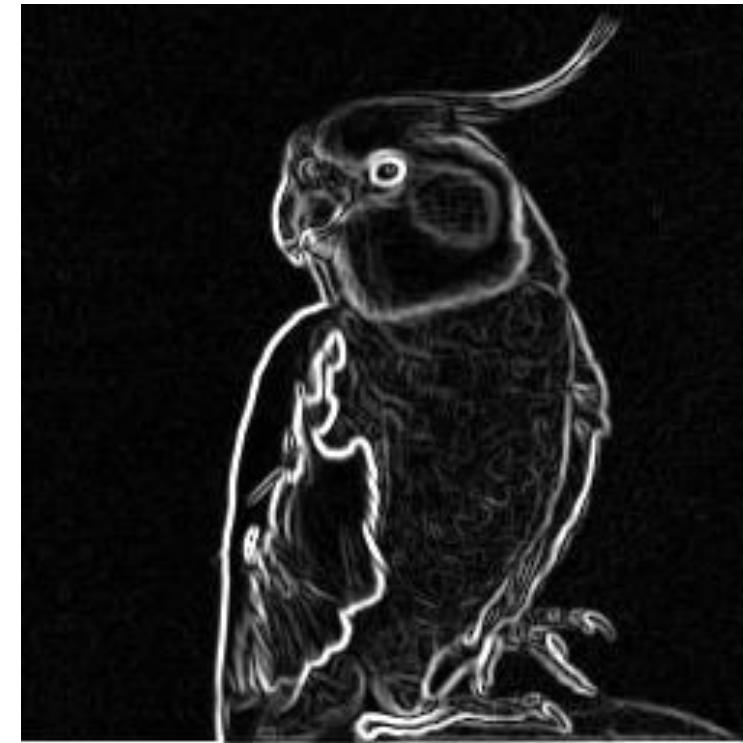
Citra masukan



Hasil operator Prewitt



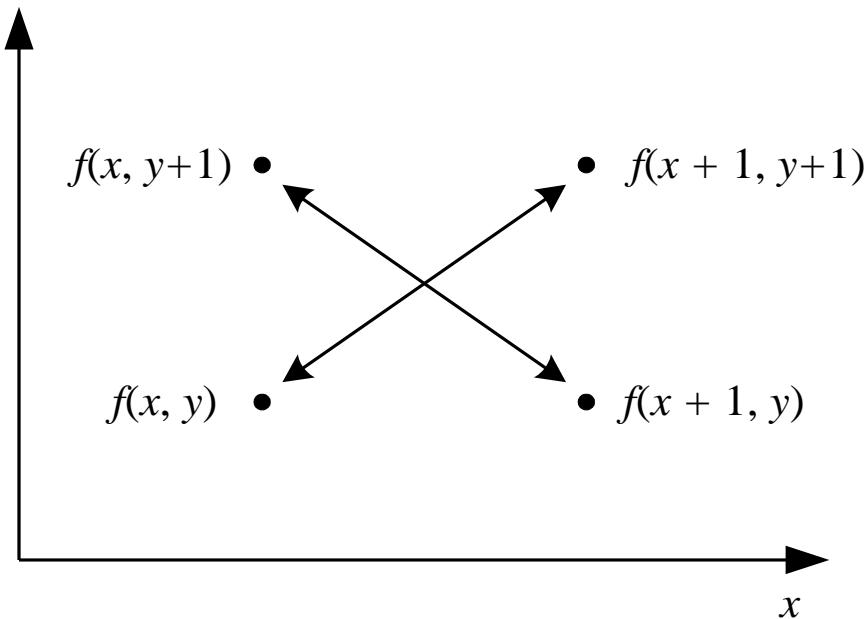
Hasil operator Sobel



Hasil operator Prewitt

Operator Roberts

- Operator Roberts sering disebut juga operator silang



Arah tepi dihitung dengan rumus:

$$\alpha(x, y) = \frac{\pi}{4} + \tan^{-1}\left(\frac{R_-}{R_+}\right)$$

Gradien Roberts dalam arah-x dan arah-y dihitung dengan rumus:

$$R_+(x, y) = f(x + 1, y + 1) - f(x, y)$$

$$R_-(x, y) = f(x, y + 1) - f(x + 1, y)$$

Dalam bentuk *mask* konvolusi:

$$R_+ = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \quad \text{dan} \quad R_- = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$$

Kekuatan tepi dihitung dengan rumus $G[f(x, y)] = |R_+| + |R_-|$

- Contoh berikut ini memperlihatkan pendekripsi tepi dengan operator Roberts:

$$\begin{bmatrix} 3 & 4 & 2 & 5 & 1 \\ 2 & 1 & 6 & 4 & 2 \\ 3 & 5 & 7 & 1 & 3 \\ 4 & 2 & 5 & 7 & 1 \\ 2 & 5 & 1 & 3 & 2 \end{bmatrix}$$

(i) citra semula

$$\begin{bmatrix} 4 & 3 & 3 & 6 & * \\ 5 & 7 & 8 & 2 & * \\ 2 & 5 & 4 & 4 & * \\ 1 & 1 & 8 & 7 & * \\ * & * & * & * & * \end{bmatrix}$$

(ii) hasil konvolusi

Nilai 4 pada pojok kiri atas pada citra hasil konvolusi diperoleh dengan perhitungan sebagai berikut:

$$f'[0,0] = |3 - 1| + |4 - 2| = 4$$

```
I = imread('bird.bmp');  
Rx = [1 0; 0 -1];  
Ry = [0 1; -1 0];  
Jx = conv2(double(I), double(Rx), 'same');  
Jy = conv2(double(I), double(Ry), 'same');  
Jedge = sqrt(Jx.^2 + Jy.^2);  
imshow(I);  
figure, imshow(uint8(Jedge));
```



Citra masukan



Hasil operator Roberts

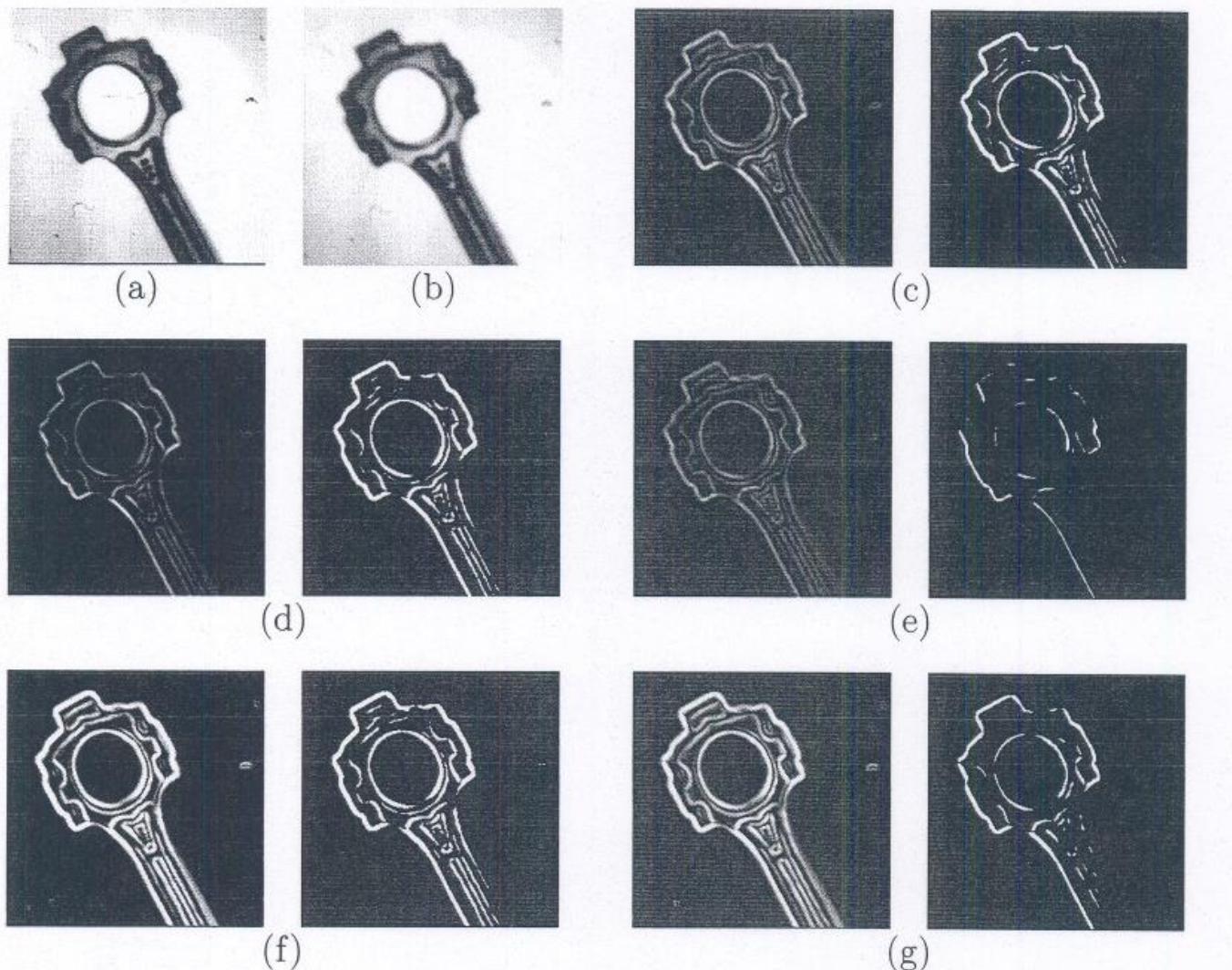


Figure 5.4: A comparison of various edge detectors. (a) Original image. (b) Filtered image. (c) Simple gradient using 1×2 and 2×1 masks, $T = 32$. (d) Gradient using 2×2 masks, $T = 64$. (e) Roberts cross operator, $T = 64$. (f) Sobel operator, $T = 225$. (g) Prewitt operator, $T = 225$.

Operator Canny

- Operator deteksi tepi yang terkenal karena dapat menghasilkan tepi dengan ketebalan 1 *pixel*



Langkah-langkah operator Canny:

1. Haluskan citra I menggunakan penapis Gaussian G (dengan standard deviasi σ yang dispesifikasikan): $G * I$
2. Hitung gradien dan arah gradien setiap pixel dengan salah satu dari empat operator sebelumnya (misalnya operator Sobel)
3. Jika nilai mutlak (magnitude) gradien suatu pixel melebihi nilai ambang T , maka pixel tersebut termasuk pixel tepi.

- Operator Canny menggunakan dua nilai ambang, T_1 dan T_2 ($T_1 < T_2$), sehingga memungkinkan deteksi dua jenis tepi: tepi kuat (*strong edges*) dan tepi lemah (*weak edges*).
- Jika magnitudo pixel ddi alam citra gradien (hasil Langkah 2) melebihi nilai ambang T_2 , maka pixel tersebut bersesuaian dengan tepi kuat.
- Setiap pixel yang terhubung ke tepi yang kuat dan memiliki magnitudo lebih besar dari nilai ambang T_1 , maka pixel tersebut bersesuaian dengan tepi lemah.

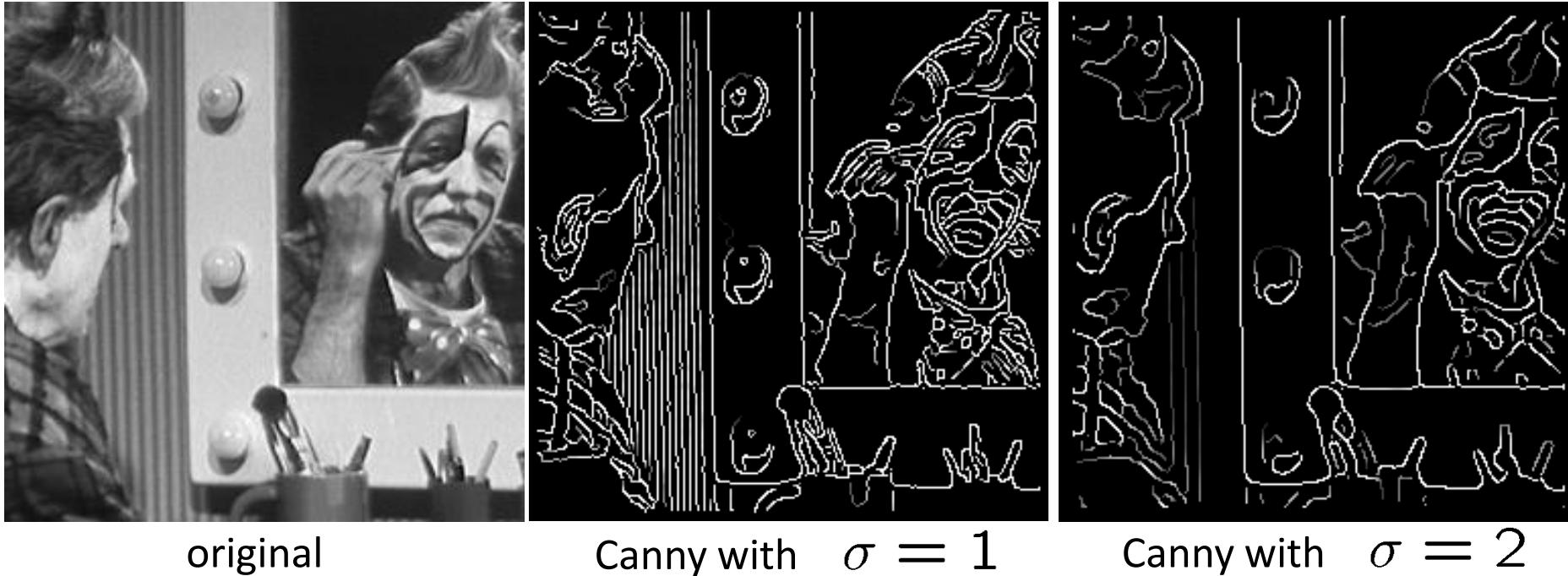


original image (Lena)



magnitude of the gradient





- The choice of σ depends on desired behavior
 - large σ detects large scale edges
 - small σ detects fine features

Original
image



Strong
edges
only



Strong +
connected
weak edges



Weak
edges



courtesy of G. Loy

Deteksi Tepi dengan Menggunakan Matlab

- Di dalam Matlab, selain menggunakan fungsi `conv2` untuk melakukan konvolusi dengan filter Sobel, Prewitt, Roberts, dan Canny, juga terdapat fungsi `edge` untuk mendeteksi tepi secara langsung dengan pilihan berbagai metode.

`BW = edge(I)` *returns a binary image BW containing 1s where the function finds edges in the grayscale or binary image I and 0s elsewhere. By default, edge uses the Sobel edge detection method.*

`BW = edge(I, method)` *detects edges in image I using the edge-detection algorithm specified by method.* Pilihan method: *Sobel* (default), *Prewitt*, *Roberts*, *Canny*, *log*

`BW = edge(I, method, threshold)` *returns all edges that are stronger than threshold.*

Sobel



Original image



```
I = imread('boat.bmp');
imshow(I)
BW = edge(I, 'Sobel');
figure, imshow(BW)
```

Prewitt



Original image



```
I = imread('boat.bmp');
imshow(I)
BW = edge(I, 'Prewitt');
figure, imshow(BW)
```

Roberts



Original image

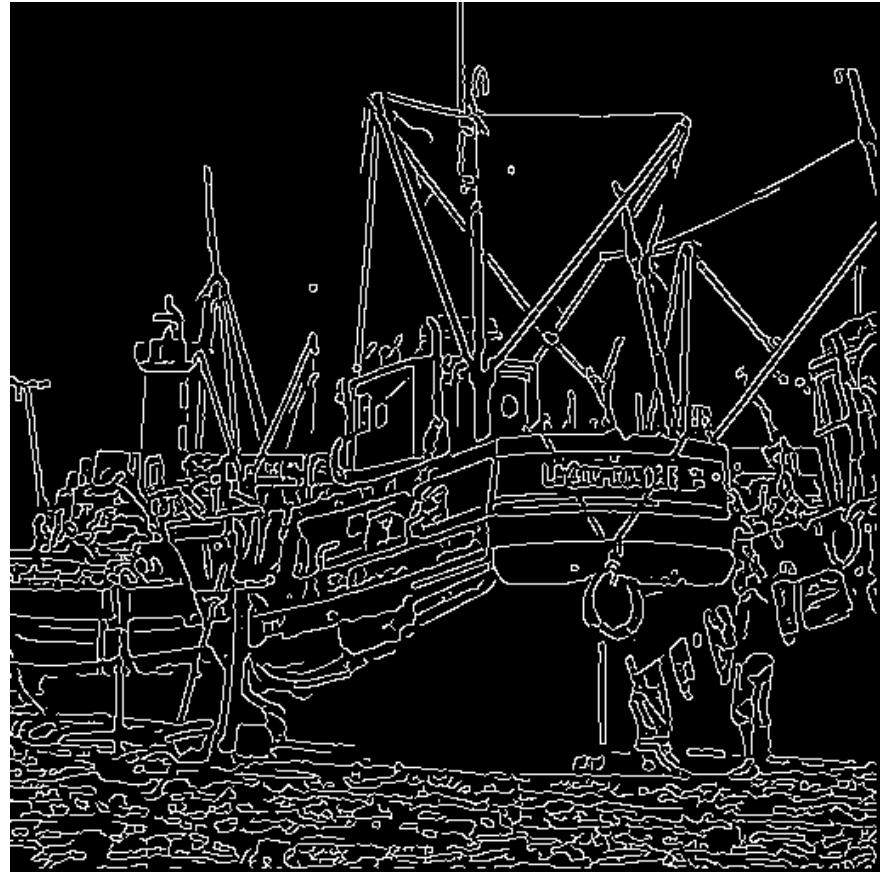


```
I = imread('boat.bmp');
imshow(I)
BW = edge(I, 'Roberts');
figure, imshow(BW)
```

Canny



Original image

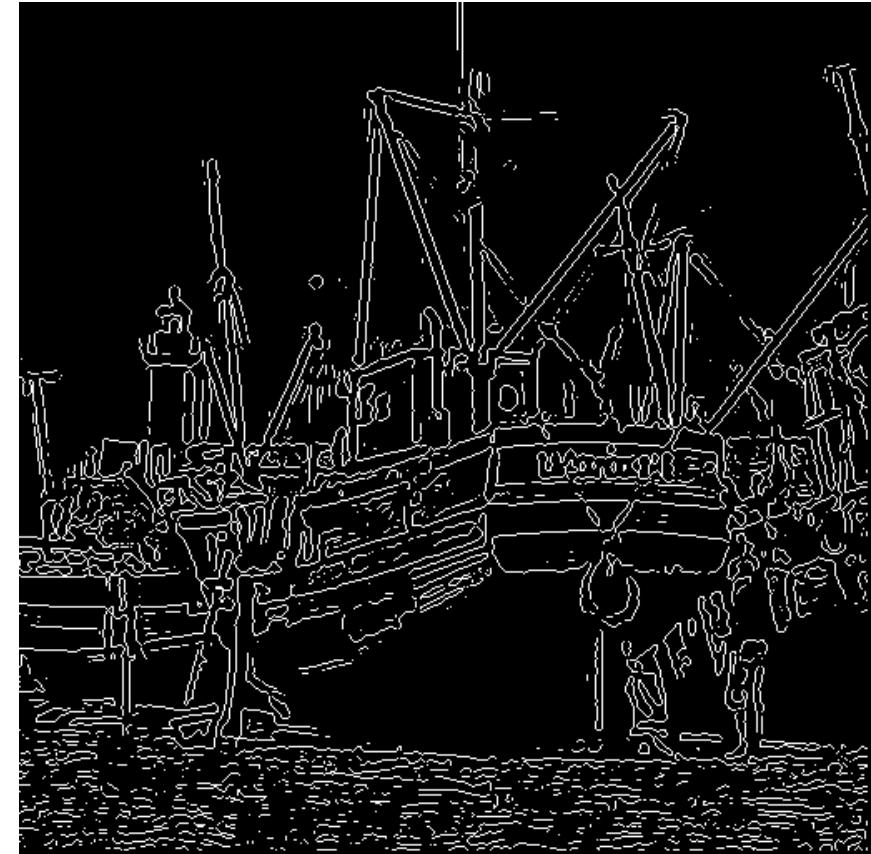


```
I = imread('boat.bmp');
imshow(I)
BW = edge(I, 'Canny');
figure, imshow(BW)
```

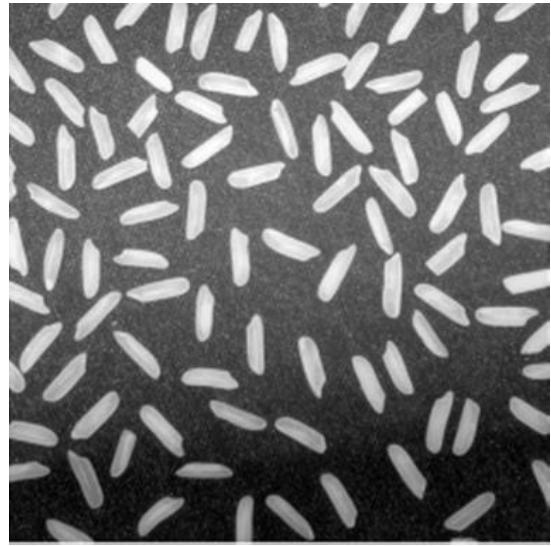
log (Laplacian of Gaussian)



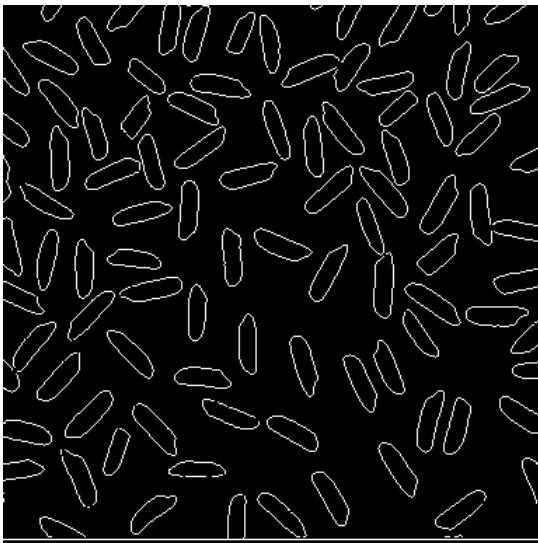
Original image



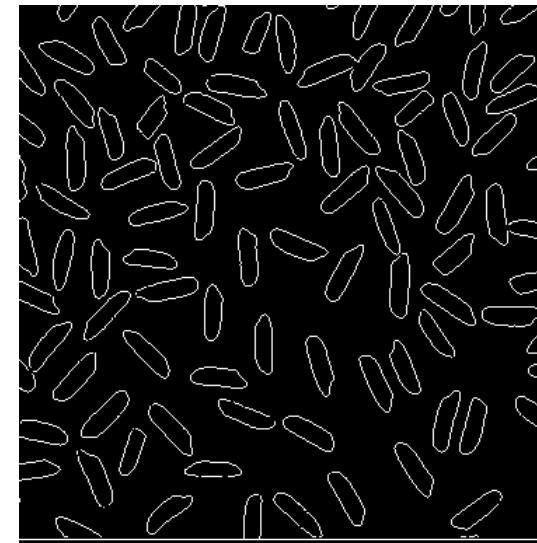
```
I = imread('boat.bmp');
imshow(I)
BW = edge(I, 'log');
figure, imshow(BW)
```



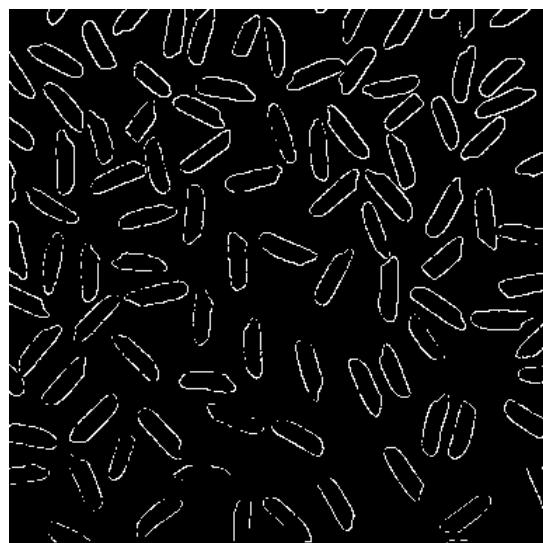
Original image



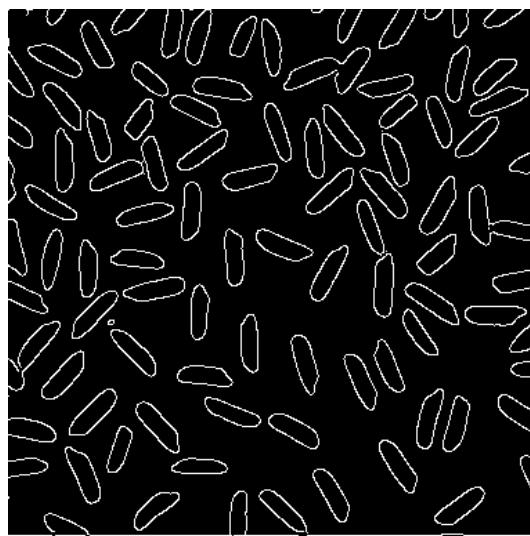
Sobel



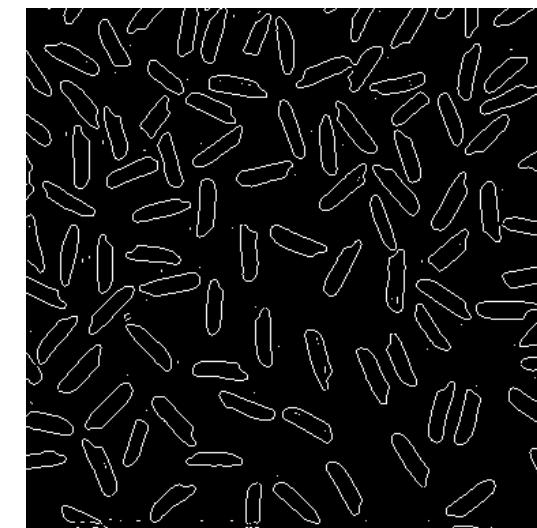
Prewitt



Roberts



Canny



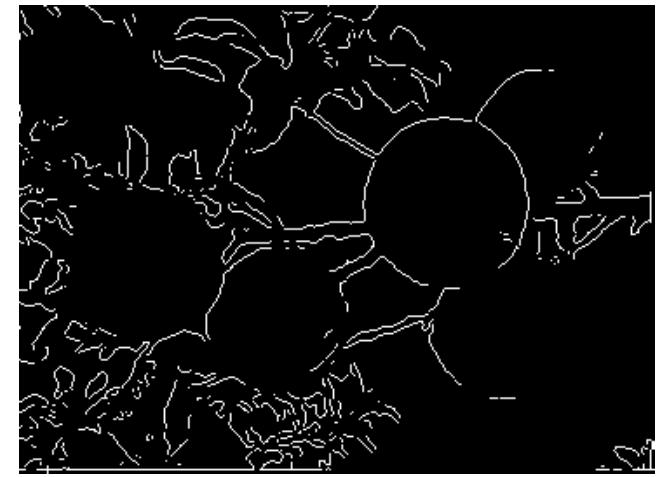
log



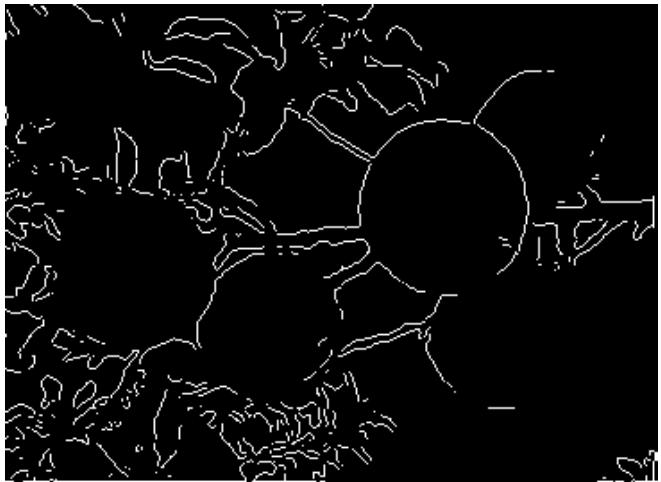
Original image



Gray image



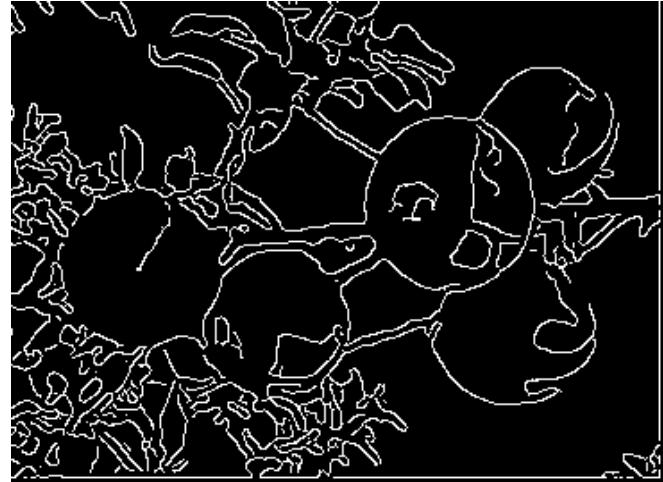
Sobel



Prewitt



Roberts



Canny

Deteksi tepi pada citra yang mengandung derau

```
clear all
close all
clc
Im = imread('lada-gray.bmp');
figure(1),imshow(Im);title('Original image');

Im_noise = imnoise(Im,'salt & pepper', 0.05);
figure(2),imshow(Im_noise);title('salt &
pepper');

%1 CANNY method
Im_edge_1 = edge(Im_noise, 'Canny');
figure(3),imshow(Im_edge_1);title('Edge
detection using Canny');

%2 PREWITT method
Im_edge_2 = edge(Im_noise, 'prewitt');
figure(4),imshow(Im_edge_2);title('Edge
detection using Prewitt');

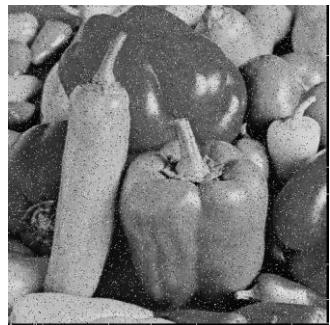
%3 ZERO CROSS method
Im_edge_3 = edge(Im_noise, 'zerocross');
figure(5),imshow(Im_edge_3); title('Edge
detection using Zerocross');
```

```
%4 Roberts method
Im_edge_4 = edge(Im_noise, 'Roberts');
figure(6),imshow(Im_edge_4); title('Edge
detection using roberts');

%5 Sobel method
Im_edge_5 = edge(Im_noise, 'Sobel');
figure(7),imshow(Im_edge_5); title('Edge
detection using Sobel');

figure(8),
    subplot(2,3,1), imshow(Im_noise);title('Noise
Image');
    subplot(2,3,2),
    imshow(Im_edge_1);title('Canny');
    subplot(2,3,3),
    imshow(Im_edge_2);title('Prewitt');
    subplot(2,3,4), imshow(Im_edge_3);
    title('Zerocross');
    subplot(2,3,5), imshow(Im_edge_4);
    title('Roberts');
    subplot(2,3,6), imshow(Im_edge_5);
    title('Sobel');
```

Noise Image



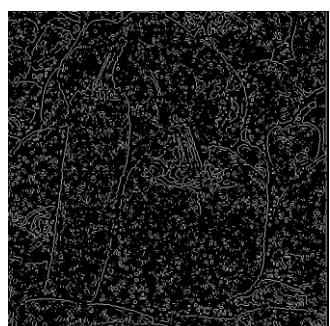
Canny



Prewitt



Zerocross



Roberts



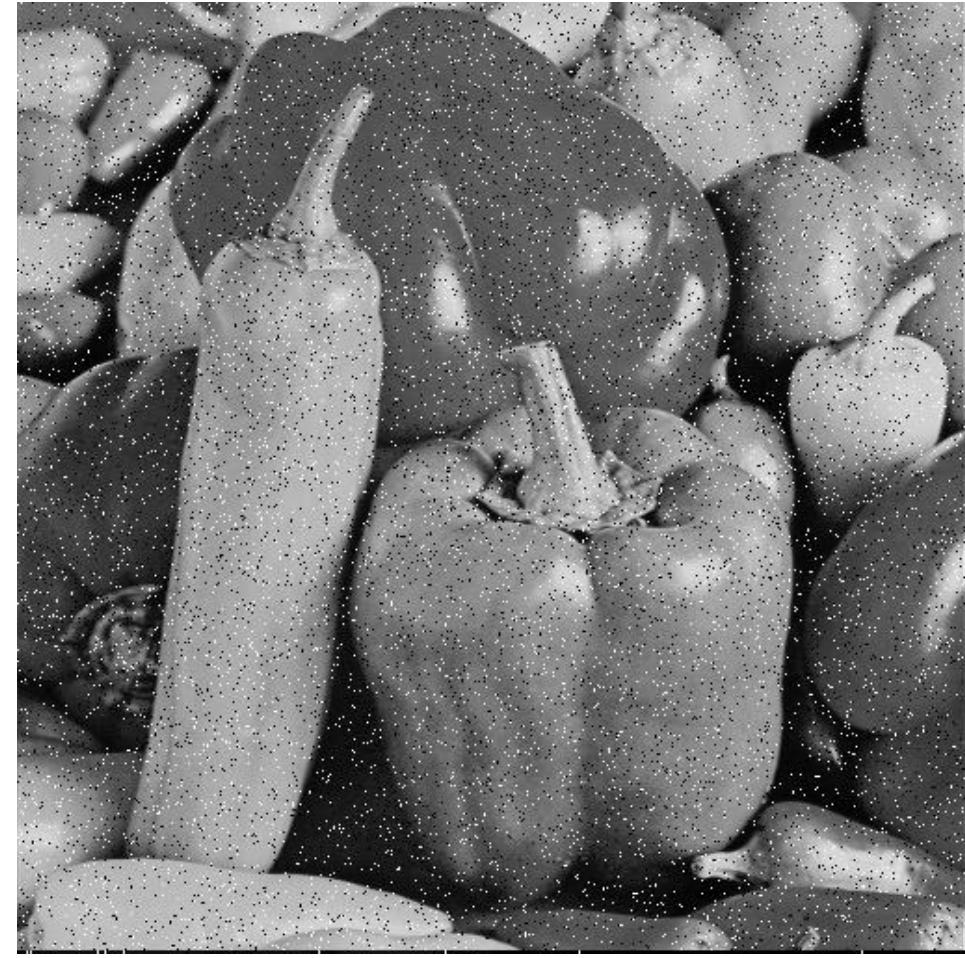
Sobel



Original image



salt & pepper



Edge detection using Canny



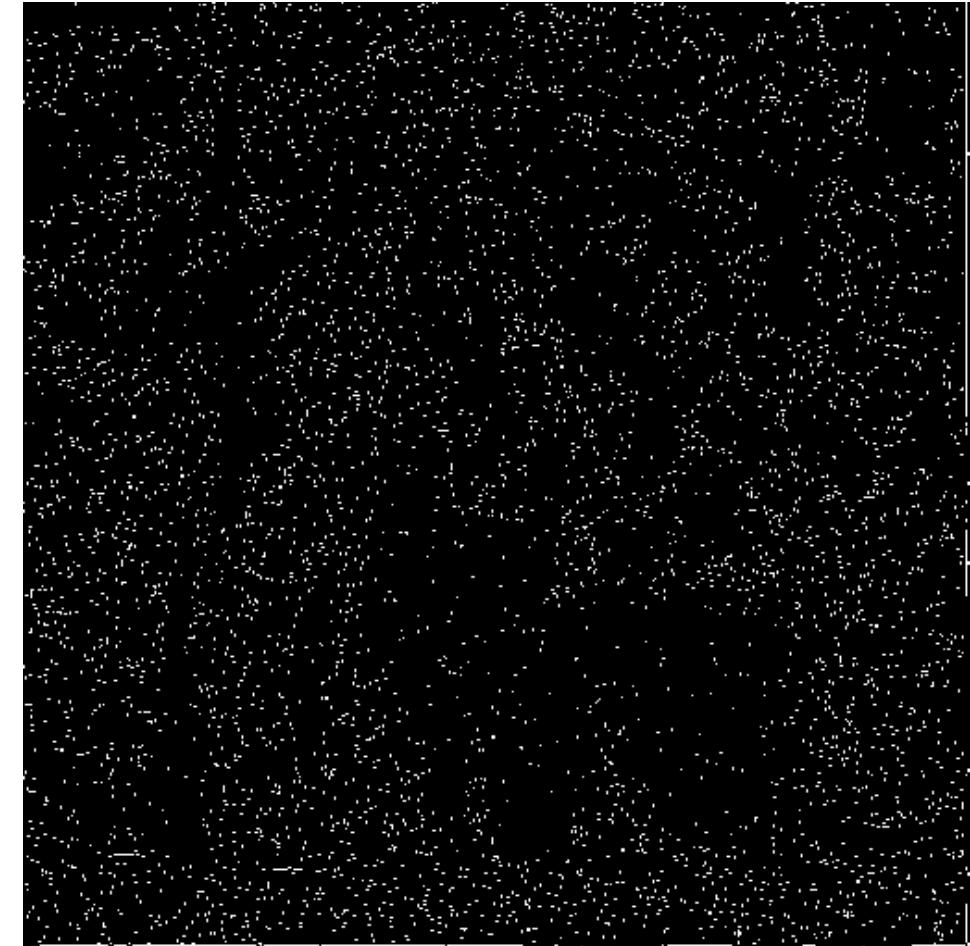
Edge detection using Prewitt



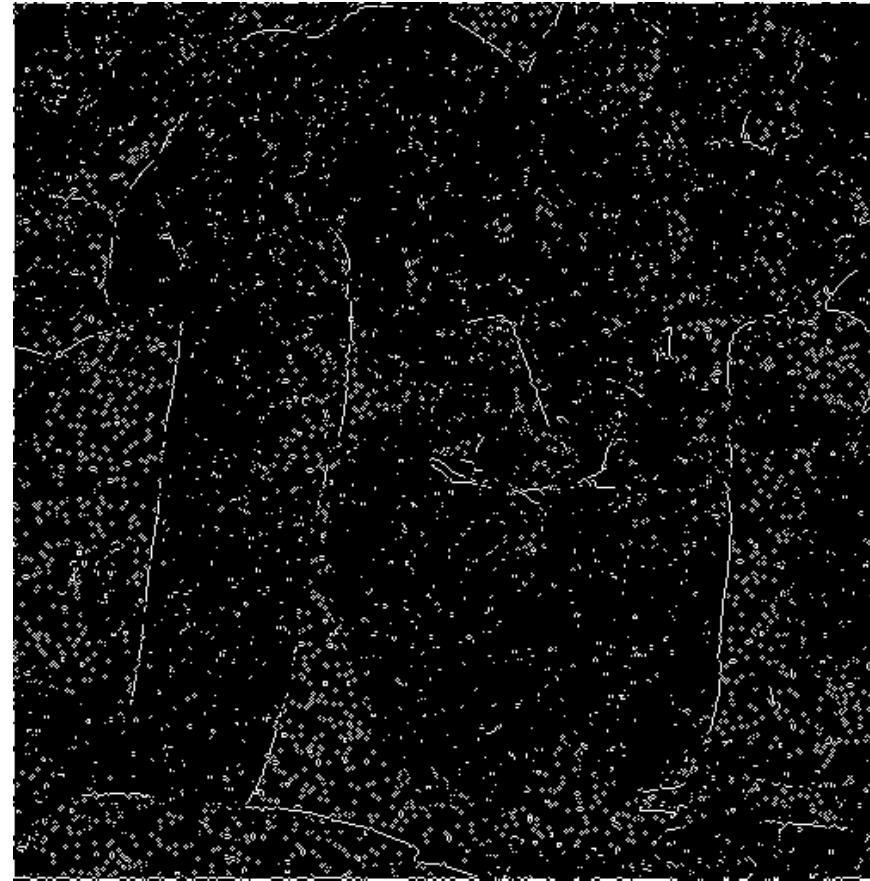
Edge detection using Zerocross



Edge detection using roberts

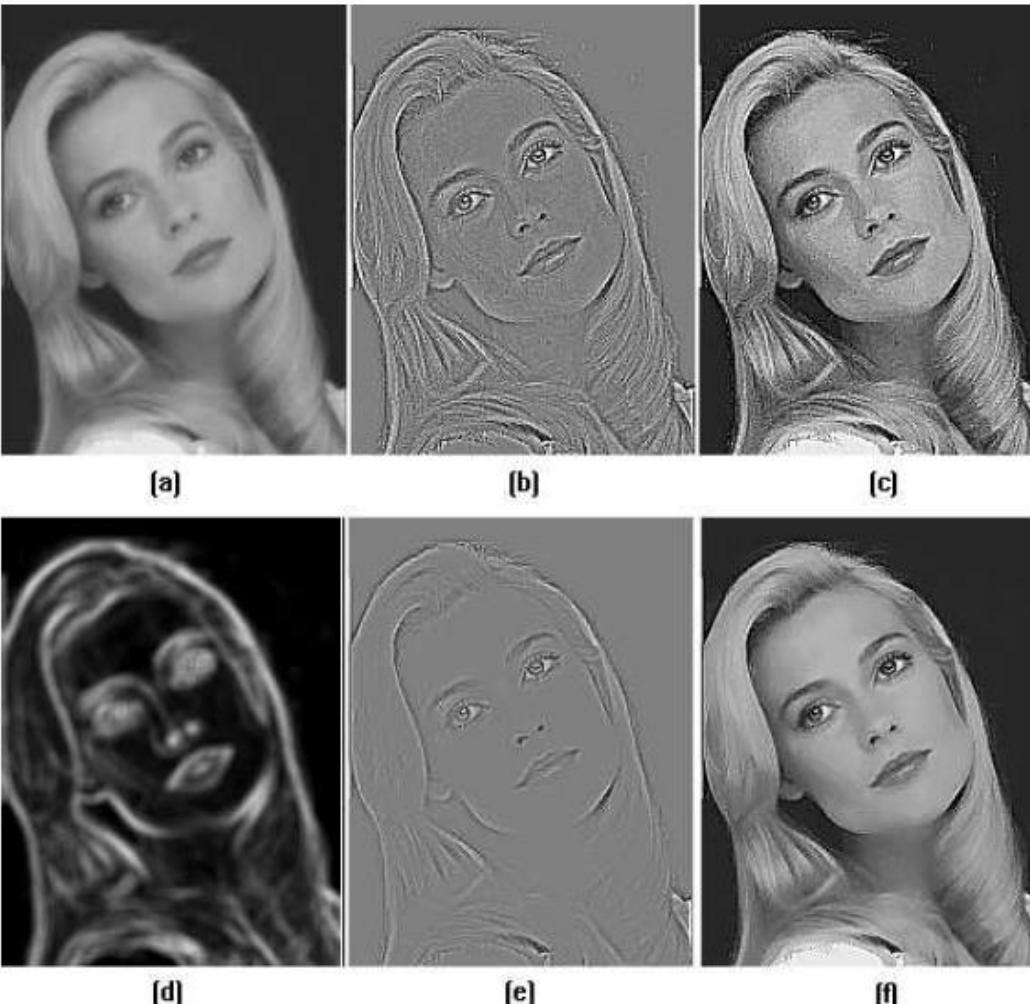


Edge detection using Sobel



Moral dari contoh ini: untuk mendapatkan hasil deteksi tepi yang optimal, maka citra yang mengandung derau seharusnya ditapis terlebih dahulu untuk menghilangkan deraunya (image enhancement)

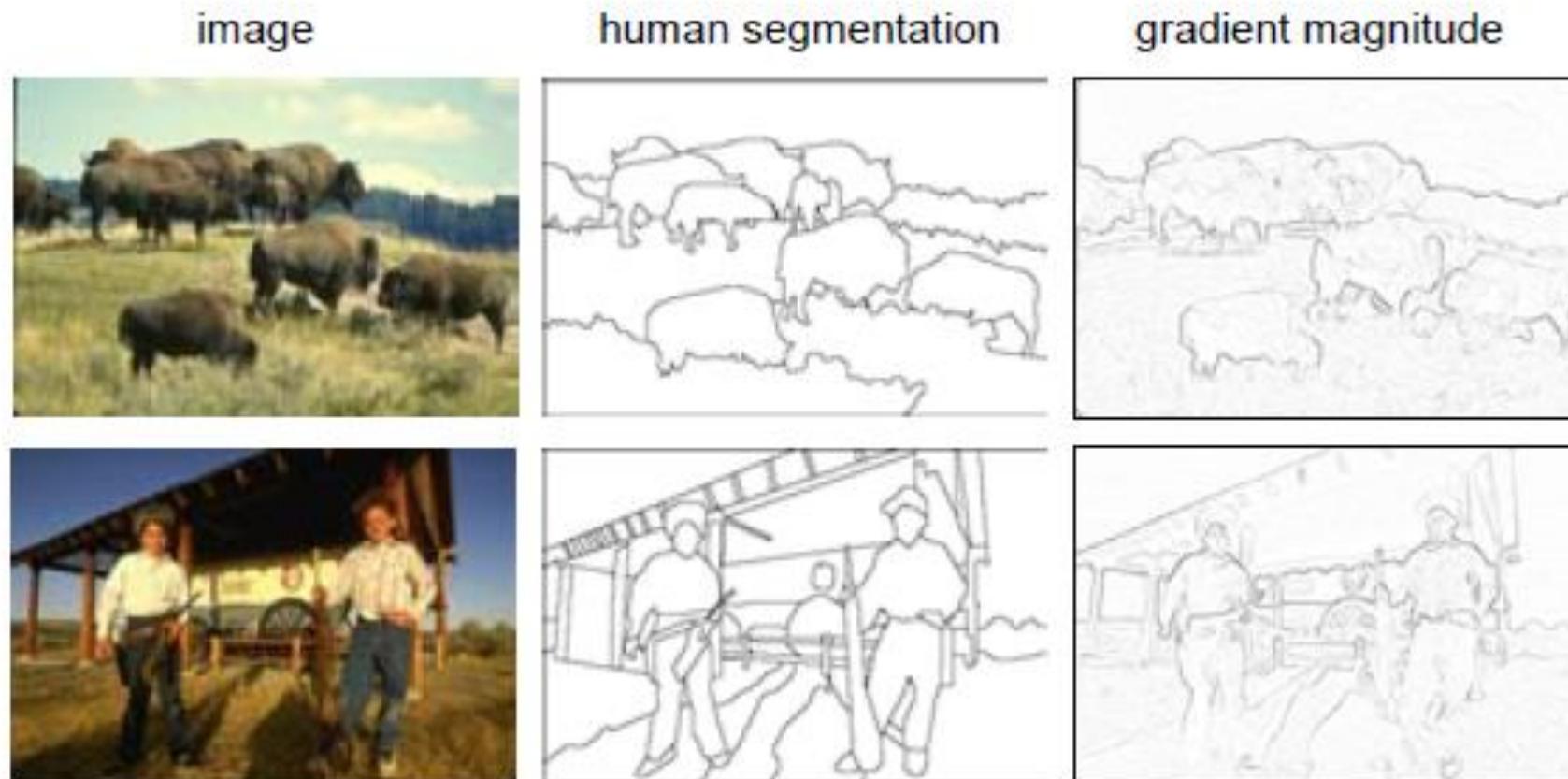
Aplikasi deteksi tepi untuk *image enhancement*



(a) Input image; (b) Laplacian of (a); (c) Spatially invariant high-pass filtering [sum of (a) and (b)]; (d) Mask image [Sobel gradient of (a) smoothed by a 5x5 box filter]; (e) Product of (b) and (d); (f) Space-variant enhancement [sum of (a) and (e)].

Sumber: Edge detection, Digital Image Processing, K. Pratt, Chapter 15

Edge detection is just the beginning...



- Berkeley segmentation database:

<http://www.eecs.berkeley.edu/Research/Projects/CS/vision/grouping/segbench/>